



$$I(J^P) = \frac{1}{2}(0^-)$$

K_S^0 MEAN LIFE

For earlier measurements, beginning with BOLDT 58B, see our 1986 edition, Physics Letters **170B** 130 (1986).

OUR FIT is described in the note on “*CP* violation in K_L^0 decays” in the K_L^0 Particle Listings. The result labeled “OUR FIT Assuming *CPT*” [“OUR FIT Not assuming *CPT*”] includes all measurements except those with the comment “Not assuming *CPT*” [“Assuming *CPT*”]. Measurements with neither comment do not assume *CPT* and enter both fits.

| VALUE (10^{-10} s) | EVTS | DOCUMENT ID | TECN | COMMENT |
|---|-------|-----------------------------|------|---|
| 0.8954 ± 0.0004 OUR FIT | | | | Error includes scale factor of 1.1. Assuming <i>CPT</i> |
| 0.89564 ± 0.00033 OUR FIT | | | | Not assuming <i>CPT</i> |
| 0.89589 ± 0.00070 | | ^{1,2} ABOUZAID | 11 | KTEV Not assuming <i>CPT</i> |
| 0.89623 ± 0.00047 | | ^{1,3} ABOUZAID | 11 | KTEV Assuming <i>CPT</i> |
| 0.89562 ± 0.00029 ± 0.00043 | 20M | ⁴ AMBROSINO | 11 | KLOE Not assuming <i>CPT</i> |
| 0.89598 ± 0.00048 ± 0.00051 | 16M | LAI | 02C | NA48 |
| 0.8971 ± 0.0021 | | BERTANZA | 97 | NA31 |
| 0.8941 ± 0.0014 ± 0.0009 | | SCHWINGEN... | 95 | E773 Assuming <i>CPT</i> |
| 0.8929 ± 0.0016 | | GIBBONS | 93 | E731 Assuming <i>CPT</i> |
| ● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ● | | | | |
| 0.8965 ± 0.0007 | | ⁵ ALAVI-HARATI03 | KTEV | Assuming <i>CPT</i> |
| 0.8958 ± 0.0013 | | ⁶ ALAVI-HARATI03 | KTEV | Not assuming <i>CPT</i> |
| 0.8920 ± 0.0044 | 214k | GROSSMAN | 87 | SPEC |
| 0.905 ± 0.007 | | ⁷ ARONSON | 82B | SPEC |
| 0.881 ± 0.009 | 26k | ARONSON | 76 | SPEC |
| 0.8926 ± 0.0032 ± 0.0002 | | ⁸ CARITHERS | 75 | SPEC |
| 0.8937 ± 0.0048 | 6M | GEWENIGER | 74B | ASPK |
| 0.8958 ± 0.0045 | 50k | ⁹ SKJEGGEST... | 72 | HBC |
| 0.856 ± 0.008 | 19994 | ¹⁰ DONALD | 68B | HBC |
| 0.872 ± 0.009 | 20000 | ^{9,10} HILL | 68 | DBC |

¹ The two ABOUZAID 11 values use the same full KTeV dataset from 1996, 1997, and 1999. The first enters the “assuming *CPT*” fit and the second enters the “not assuming *CPT*” fit.

² ABOUZAID 11 fit has Δm , τ_S , ϕ_ϵ , $\text{Re}(\epsilon'/\epsilon)$, and $\text{Im}(\epsilon'/\epsilon)$ as free parameters. See $\text{Im}(\epsilon'/\epsilon)$ in the “ K_L^0 *CP* violation” section for correlation information.

³ ABOUZAID 11 fit has Δm and τ_S free but constrains ϕ_ϵ to the Superweak value, i.e. assumes *CPT*. This τ_S value is correlated with their $\Delta m = m_{K_L^0} - m_{K_S^0}$ measurement in the K_L^0 listings. The correlation coefficient $\rho(\tau_S, \Delta m) = -0.670$.

⁴ Fit to the proper time distribution.

⁵ This ALAVI-HARATI 03 fit has Δm and τ_S free but constrains ϕ_{+-} to the Superweak value, i.e. assumes *CPT*. This τ_S value is correlated with their $\Delta m = m_{K_L^0} - m_{K_S^0}$ measurement in the K_L^0 listings. The correlation coefficient $\rho(\tau_S, \Delta m) = -0.396$. Superseded by ABOUZAID 11.

⁶This ALAVI-HARATI 03 fit has Δm , ϕ_{+-} , and τ_{K_S} free. See ϕ_{+-} in the “ K_L CP violation” section for correlation information. Superseded by ABOUZAIID 11.

⁷ARONSON 82 find that K_S^0 mean life may depend on the kaon energy.

⁸CARITHERS 75 measures the Δm dependence of the total decay rate (inverse mean life) to be $\Gamma(K_S^0) = [(1.122 \pm 0.004) + 0.16(\Delta m - 0.5348)/\Delta m] 10^{10}/s$, or, in terms of mean life, CARITHERS 75 measures $\tau_S = (0.8913 \pm 0.0032) - 0.238 [\Delta m - 0.5348] (10^{-10} s)$. We have adjusted the measurement to use our best values of ($\Delta m = 0.5293 \pm 0.0009$) ($10^{10} \hbar s^{-1}$). Our first error is their experiment's error and our second error is the systematic error from using our best values.

⁹HILL 68 has been changed by the authors from the published value (0.865 ± 0.009) because of a correction in the shift due to η_{+-} . SKJEGGESTAD 72 and HILL 68 give detailed discussions of systematics encountered in this type of experiment.

¹⁰Pre-1971 experiments are excluded from the average because of disagreement with later more precise experiments.

K_S^0 DECAY MODES

| Mode | Fraction (Γ_i/Γ) | Scale factor/ Confidence level |
|--|---|-----------------------------------|
| Hadronic modes | | |
| Γ_1 $\pi^0 \pi^0$ | $(30.69 \pm 0.05) \%$ | |
| Γ_2 $\pi^+ \pi^-$ | $(69.20 \pm 0.05) \%$ | |
| Γ_3 $\pi^+ \pi^- \pi^0$ | $(3.5^{+1.1}_{-0.9}) \times 10^{-7}$ | |
| Modes with photons or $\ell\bar{\ell}$ pairs | | |
| Γ_4 $\pi^+ \pi^- \gamma$ | [a,b] $(1.79 \pm 0.05) \times 10^{-3}$ | |
| Γ_5 $\pi^+ \pi^- e^+ e^-$ | $(4.79 \pm 0.15) \times 10^{-5}$ | |
| Γ_6 $\pi^0 \gamma \gamma$ | [a] $(4.9 \pm 1.8) \times 10^{-8}$ | |
| Γ_7 $\gamma \gamma$ | $(2.63 \pm 0.17) \times 10^{-6}$ | S=3.1 |
| Semileptonic modes | | |
| Γ_8 $\pi^\pm e^\mp \nu_e$ | [c] $(7.04 \pm 0.08) \times 10^{-4}$ | |
| Γ_9 $\pi^\pm \mu^\mp \nu_\mu$ | [c,d] $(4.56 \pm 0.20) \times 10^{-4}$ | |
| CP violating (CP) and $\Delta S = 1$ weak neutral current (S1) modes | | |
| Γ_{10} $3\pi^0$ | CP $< 2.6 \times 10^{-8}$ | CL=90% |
| Γ_{11} $\mu^+ \mu^-$ | S1 $< 2.1 \times 10^{-10}$ | CL=90% |
| Γ_{12} $e^+ e^-$ | S1 $< 9 \times 10^{-9}$ | CL=90% |
| Γ_{13} $\pi^0 e^+ e^-$ | S1 [a] $(3.0^{+1.5}_{-1.2}) \times 10^{-9}$ | |
| Γ_{14} $\pi^0 \mu^+ \mu^-$ | S1 $(2.9^{+1.5}_{-1.2}) \times 10^{-9}$ | |

[a] See the Particle Listings below for the energy limits used in this measurement.

[b] Most of this radiative mode, the low-momentum γ part, is also included in the parent mode listed without γ 's.

[c] The value is for the sum of the charge states or particle/antiparticle states indicated.

[d] Not a measurement. Calculated as $0.666 \cdot B(\pi^\pm e^\mp \nu_e)$.

CONSTRAINED FIT INFORMATION

An overall fit to 4 branching ratios uses 5 measurements and one constraint to determine 4 parameters. The overall fit has a $\chi^2 = 0.1$ for 2 degrees of freedom.

The following *off-diagonal* array elements are the correlation coefficients $\langle \delta x_i \delta x_j \rangle / (\delta x_i \cdot \delta x_j)$, in percent, from the fit to the branching fractions, $x_i \equiv \Gamma_i / \Gamma_{\text{total}}$. The fit constrains the x_i whose labels appear in this array to sum to one.

| | | | | |
|-------|------|-------|-------|-------|
| x_2 | -100 | | | |
| x_8 | -6 | 4 | | |
| x_9 | -1 | -3 | 0 | |
| | | x_1 | x_2 | x_8 |

K_S^0 DECAY RATES

$\Gamma(\pi^\pm e^\mp \nu_e)$

Γ_8

| <u>VALUE</u> (10^6 s^{-1}) | <u>EVTS</u> | <u>DOCUMENT ID</u> | <u>TECN</u> | <u>COMMENT</u> |
|---|-------------|----------------------------|-------------|---|
| ● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ● | | | | |
| 8.1 ± 1.6 | 75 | ¹ AKHMETSHIN 99 | CMD2 | Tagged K_S^0 using $\phi \rightarrow K_L^0 K_S^0$ |
| 7.50 ± 0.08 | | ² PDG | 98 | |
| seen | | BURGUN | 72 | HBC $K^+ p \rightarrow K^0 p \pi^+$ |
| 9.3 ± 2.5 | | AUBERT | 65 | HLBC $\Delta S = \Delta Q$, CP cons. not assumed |

¹ AKHMETSHIN 99 is from a measured branching ratio $B(K_S^0 \rightarrow \pi e \nu_e) = (7.2 \pm 1.4) \times 10^{-4}$ and $\tau_{K_S^0} = (0.8934 \pm 0.0008) \times 10^{-10}$ s. Not independent of measured branching ratio.

² PDG 98 from K_L^0 measurements, assuming that $\Delta S = \Delta Q$ in K^0 decay so that $\Gamma(K_S^0 \rightarrow \pi^\pm e^\mp \nu_e) = \Gamma(K_L^0 \rightarrow \pi^\pm e^\mp \nu_e)$.

$\Gamma(\pi^\pm \mu^\mp \nu_\mu)$

Γ_9

| <u>VALUE</u> (10^6 s^{-1}) | <u>DOCUMENT ID</u> |
|---|---------------------|
| ● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ● | |
| 5.25 ± 0.07 | ¹ PDG 98 |
| ¹ PDG 98 from K_L^0 measurements, assuming that $\Delta S = \Delta Q$ in K^0 decay so that $\Gamma(K_S^0 \rightarrow \pi^\pm \mu^\mp \nu_\mu) = \Gamma(K_L^0 \rightarrow \pi^\pm \mu^\mp \nu_\mu)$. | |

K_S^0 BRANCHING RATIOS**Hadronic modes** $\Gamma(\pi^0\pi^0)/\Gamma_{\text{total}}$ Γ_1/Γ VALUE EVTS DOCUMENT ID TECN**0.3069 ± 0.0005 OUR FIT**

• • • We do not use the following data for averages, fits, limits, etc. • • •

| | | | | |
|---------------|------|----------|----|------|
| 0.335 ± 0.014 | 1066 | BROWN | 63 | HLBC |
| 0.288 ± 0.021 | 198 | CHRETIEN | 63 | HLBC |
| 0.30 ± 0.035 | | BROWN | 61 | HLBC |

 $\Gamma(\pi^+\pi^-)/\Gamma_{\text{total}}$ Γ_2/Γ VALUE EVTS DOCUMENT ID TECN COMMENT**0.6920 ± 0.0005 OUR FIT**

• • • We do not use the following data for averages, fits, limits, etc. • • •

| | | | | | |
|---------------|------|-------|----|-----|-----------------------------------|
| 0.670 ± 0.010 | 3447 | DOYLE | 69 | HBC | $\pi^- p \rightarrow \Lambda K^0$ |
|---------------|------|-------|----|-----|-----------------------------------|

 $\Gamma(\pi^+\pi^-)/\Gamma(\pi^0\pi^0)$ Γ_2/Γ_1 VALUE EVTS DOCUMENT ID TECN COMMENT**2.255 ± 0.005 OUR FIT****2.2549 ± 0.0054**

• • • We do not use the following data for averages, fits, limits, etc. • • •

| | | | | | |
|--------------------------|------|------------------------|-----|------|--|
| | | ¹ AMBROSINO | 06c | KLOE | |
| 2.2555 ± 0.0012 ± 0.0054 | | ² AMBROSINO | 06c | KLOE | |
| 2.236 ± 0.003 ± 0.015 | 766k | ² ALOISIO | 02B | KLOE | |
| 2.11 ± 0.09 | 1315 | EVERHART | 76 | WIRE | $\pi^- p \rightarrow \Lambda K^0$ |
| 2.169 ± 0.094 | 16k | COWELL | 74 | OSPK | $\pi^- p \rightarrow \Lambda K^0$ |
| 2.16 ± 0.08 | 4799 | HILL | 73 | DBC | $K^+ d \rightarrow K^0 p p$ |
| 2.22 ± 0.10 | 3068 | ³ ALITTI | 72 | HBC | $K^+ p \rightarrow \pi^+ p K^0$ |
| 2.22 ± 0.08 | 6380 | MORSE | 72B | DBC | $K^+ n \rightarrow K^0 p$ |
| 2.10 ± 0.11 | 701 | ⁴ NAGY | 72 | HLBC | $K^+ n \rightarrow K^0 p$ |
| 2.22 ± 0.095 | 6150 | ⁵ BALTAY | 71 | HBC | $K p \rightarrow K^0 \text{ neutrals}$ |
| 2.282 ± 0.043 | 7944 | ⁶ MOFFETT | 70 | OSPK | $K^+ n \rightarrow K^0 p$ |
| 2.12 ± 0.17 | 267 | ⁴ BOZOKI | 69 | HLBC | |
| 2.285 ± 0.055 | 3016 | ⁶ GOBBI | 69 | OSPK | $K^+ n \rightarrow K^0 p$ |
| 2.10 ± 0.06 | 3700 | MORFIN | 69 | HLBC | $K^+ n \rightarrow K^0 p$ |

¹ This result combines AMBROSINO 06c KLOE 2001-02 data with ALOISIO 02B KLOE 2000 data. $K_S^0 \rightarrow \pi^+\pi^-$ fully inclusive.² Includes radiative decays $\pi^+\pi^-\gamma$.³ The directly measured quantity is $K_S^0 \rightarrow \pi^+\pi^-/\text{all } K^0 = 0.345 \pm 0.005$.⁴ NAGY 72 is a final result which includes BOZOKI 69.⁵ The directly measured quantity is $K_S^0 \rightarrow \pi^+\pi^-/\text{all } \bar{K}^0 = 0.345 \pm 0.005$.⁶ MOFFETT 70 is a final result which includes GOBBI 69.

$\Gamma(\pi^+\pi^-\pi^0)/\Gamma_{\text{total}}$ Γ_3/Γ

| <u>VALUE (units 10^{-7})</u> | <u>EVTS</u> | <u>DOCUMENT ID</u> | <u>TECN</u> | <u>COMMENT</u> |
|---|-------------|--------------------|-------------|----------------|
|---|-------------|--------------------|-------------|----------------|

 $3.5^{+1.1}_{-0.9}$ OUR AVERAGE

| | | | | |
|---|------|-----------|----------|-------------------|
| $4.7^{+2.2+1.7}_{-1.7-1.5}$ | | 1 BATLEY | 05 NA48 | |
| $2.5^{+1.3+0.5}_{-1.0-0.6}$ | 500k | 2 ADLER | 97B CPLR | |
| $4.8^{+2.2\pm 1.1}_{-1.6}$ | | 3 ZOU | 96 E621 | |
| ● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ● | | | | |
| $4.1^{+2.5+0.5}_{-1.9-0.6}$ | | 4 ADLER | 96E CPLR | Sup. by ADLER 97B |
| $3.9^{+5.4+0.9}_{-1.8-0.7}$ | | 5 THOMSON | 94 E621 | Sup. by ZOU 96 |

¹ BATLEY 05 is obtained by measuring the interference parameters in $K_S, K_L \rightarrow \pi^+\pi^-\pi^0$: $\text{Re}(\lambda) = 0.038 \pm 0.008 \pm 0.006$ and $\text{Im}(\lambda) = -0.013 \pm 0.005 \pm 0.004$; the correlation coeff. between $\text{Re}(\lambda)$ and $\text{Im}(\lambda)$ is 0.66 (statistical only).

² ADLER 97B find the CP -conserving parameters $\text{Re}(\lambda) = (28 \pm 7 \pm 3) \times 10^{-3}$, $\text{Im}(\lambda) = (-10 \pm 8 \pm 2) \times 10^{-3}$. They estimate $B(K_S^0 \rightarrow \pi^+\pi^-\pi^0)$ from $\text{Re}(\lambda)$ and the K_L^0 decay parameters. See also ANGELOPOULOS 98c.

³ ZOU 96 is from the the measured quantities $|\rho_{+-0}| = 0.039^{+0.009}_{-0.006} \pm 0.005$ and $\phi_\rho = (-9 \pm 18)^\circ$.

⁴ ADLER 96E is from the measured quantities $\text{Re}(\lambda) = 0.036 \pm 0.010^{+0.002}_{-0.003}$ and $\text{Im}(\lambda)$ consistent with zero. Note that the quantity λ is the same as ρ_{+-0} used in other footnotes.

⁵ THOMSON 94 calculates this branching ratio from their measurements $|\rho_{+-0}| = 0.035^{+0.019}_{-0.011} \pm 0.004$ and $\phi_\rho = (-59 \pm 48)^\circ$ where $|\rho_{+-0}|e^{i\phi_\rho} = A(K_S^0 \rightarrow \pi^+\pi^-\pi^0, I=2)/A(K_L^0 \rightarrow \pi^+\pi^-\pi^0)$.

———— Modes with photons or $\ell\bar{\ell}$ pairs ————

 $\Gamma(\pi^+\pi^-\gamma)/\Gamma(\pi^+\pi^-)$ Γ_4/Γ_2

| <u>VALUE (units 10^{-3})</u> | <u>EVTS</u> | <u>DOCUMENT ID</u> | <u>TECN</u> | <u>COMMENT</u> |
|---|-------------|--------------------|-------------|----------------|
|---|-------------|--------------------|-------------|----------------|

 2.59 ± 0.08 OUR AVERAGE

| | | | | |
|---|------|----------------------|---------|--------------------------|
| 2.56 ± 0.09 | 1286 | RAMBERG | 93 E731 | p _γ >50 MeV/c |
| 2.68 ± 0.15 | | ¹ TAUREG | 76 SPEC | p _γ >50 MeV/c |
| ● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ● | | | | |
| 7.10 ± 0.22 | 3723 | RAMBERG | 93 E731 | p _γ >20 MeV/c |
| 3.0 ± 0.6 | 29 | ² BOBISUT | 74 HLBC | p _γ >40 MeV/c |
| 2.8 ± 0.6 | | ³ BURGUN | 73 HBC | p _γ >50 MeV/c |

¹ TAUREG 76 find direct emission contribution <0.06, CL = 90%.

² BOBISUT 74 not included in average because p_γ cut differs. Estimates direct emission contribution to be 0.5 or less, CL = 95%.

³ BURGUN 73 estimates that direct emission contribution is 0.3 ± 0.6.

$\Gamma(\pi^+\pi^-e^+e^-)/\Gamma_{\text{total}}$ Γ_5/Γ

| VALUE (units 10^{-5}) | EVTS | DOCUMENT ID | TECN | COMMENT |
|--------------------------|------|-------------|------|---------|
|--------------------------|------|-------------|------|---------|

4.79 ± 0.15 OUR AVERAGE

| | | | | |
|--------------------|-----|---------------------|----------|----------------|
| 4.83 ± 0.11 ± 0.14 | 23k | ¹ BATLEY | 11 NA48 | 2002 data |
| 4.69 ± 0.30 | 676 | ² LAI | 03C NA48 | 1998+1999 data |

• • • We do not use the following data for averages, fits, limits, etc. • • •

| | | | | |
|--------------------|-----|--------------------|----------|-----------|
| 4.71 ± 0.23 ± 0.22 | 620 | ^{2,3} LAI | 03C NA48 | 1999 data |
|--------------------|-----|--------------------|----------|-----------|

| | | | | |
|-----------------|----|-----|----------|-----------|
| 4.5 ± 0.7 ± 0.4 | 56 | LAI | 00B NA48 | 1998 data |
|-----------------|----|-----|----------|-----------|

¹ BATLEY 11 reports $[\Gamma(K_S^0 \rightarrow \pi^+\pi^-e^+e^-)/\Gamma_{\text{total}}] / [B(K_L^0 \rightarrow \pi^+\pi^-\pi^0)] / [B(\pi^0 \rightarrow e^+e^-\gamma)] = (3.28 \pm 0.06 \pm 0.04) \times 10^{-2}$ which we multiply by our best values $B(K_L^0 \rightarrow \pi^+\pi^-\pi^0) = (12.54 \pm 0.05) \times 10^{-2}$, $B(\pi^0 \rightarrow e^+e^-\gamma) = (1.174 \pm 0.035) \times 10^{-2}$. Our first error is their experiment's error and our second error is the systematic error from using our best values. Also a limit on the absolute value of the interference between bremsstrahlung and E1 transition is given : $< 4 \times 10^{-7}$ at 90% C.L.

² Uses normalization $BR(K_L \rightarrow \pi^+\pi^-\pi^0) \cdot BR(\pi^0 \rightarrow e^+e^-) = (1.505 \pm 0.047) \times 10^{-3}$ from our 2000 Edition.

³ Second error is $0.16(\text{syst}) \pm 0.15(\text{norm})$ combined in quadrature.

 $\Gamma(\pi^0\gamma\gamma)/\Gamma_{\text{total}}$ Γ_6/Γ

| VALUE (units 10^{-8}) | CL% | EVTS | DOCUMENT ID | TECN | COMMENT |
|--------------------------|-----|------|-------------|------|---------|
|--------------------------|-----|------|-------------|------|---------|

| | | | | | |
|------------------------|--|----|------------------|---------|----------------------------------|
| 4.9 ± 1.6 ± 0.9 | | 17 | ¹ LAI | 04 NA48 | $m_{\gamma\gamma}^2/m_K^2 > 0.2$ |
|------------------------|--|----|------------------|---------|----------------------------------|

• • • We do not use the following data for averages, fits, limits, etc. • • •

| | | | | | |
|-----|----|--|-----|----------|----------------------------------|
| <33 | 90 | | LAI | 03B NA48 | $m_{\gamma\gamma}^2/m_K^2 > 0.2$ |
|-----|----|--|-----|----------|----------------------------------|

¹ Spectrum also measured and found consistent with the one generated by a constant matrix element.

 $\Gamma(\gamma\gamma)/\Gamma_{\text{total}}$ Γ_7/Γ

| VALUE (units 10^{-6}) | CL% | EVTS | DOCUMENT ID | TECN | COMMENT |
|--------------------------|-----|------|-------------|------|---------|
|--------------------------|-----|------|-------------|------|---------|

| | | | | | |
|--------------------------------|--|--|-------------------------------------|--|--|
| 2.63 ± 0.17 OUR AVERAGE | | | Error includes scale factor of 3.1. | | |
|--------------------------------|--|--|-------------------------------------|--|--|

| | | | | | |
|--------------------|--|-----|------------------------|----------|--------------------------------|
| 2.26 ± 0.12 ± 0.06 | | 711 | ¹ AMBROSINO | 08C KLOE | $\phi \rightarrow K_S^0 K_L^0$ |
|--------------------|--|-----|------------------------|----------|--------------------------------|

| | | | | | |
|-----------------------|--|------|------------------|---------|--|
| 2.713 ± 0.063 ± 0.005 | | 7.5k | ² LAI | 03 NA48 | |
|-----------------------|--|------|------------------|---------|--|

• • • We do not use the following data for averages, fits, limits, etc. • • •

| | | | | | |
|--------------------|--|-----|-----|---------|--|
| 2.58 ± 0.36 ± 0.22 | | 149 | LAI | 00 NA48 | |
|--------------------|--|-----|-----|---------|--|

| | | | | | |
|-----------|--|----|-------------------|----------|--|
| 2.2 ± 1.1 | | 16 | ³ BARR | 95B NA31 | |
|-----------|--|----|-------------------|----------|--|

| | | | | | |
|-----------|--|----|-------------------|----------|--|
| 2.4 ± 0.9 | | 35 | ⁴ BARR | 95B NA31 | |
|-----------|--|----|-------------------|----------|--|

| | | | | | |
|------|----|--|--------|---------|--|
| < 13 | 90 | | BALATS | 89 SPEC | |
|------|----|--|--------|---------|--|

| | | | | | |
|-----------|--|----|-----------|---------|--|
| 2.4 ± 1.2 | | 19 | BURKHARDT | 87 NA31 | |
|-----------|--|----|-----------|---------|--|

| | | | | | |
|------|----|--|--------|----------|--|
| <133 | 90 | | BARMIN | 86B XEBC | |
|------|----|--|--------|----------|--|

¹ AMBROSINO 08C reports $(2.26 \pm 0.12 \pm 0.06) \times 10^{-6}$ from a measurement of $[\Gamma(K_S^0 \rightarrow \gamma\gamma)/\Gamma_{\text{total}}] \times [B(K_S^0 \rightarrow \pi^0\pi^0)]$ assuming $B(K_S^0 \rightarrow \pi^0\pi^0) = (30.69 \pm 0.05) \times 10^{-2}$.

² LAI 03 reports $[\Gamma(K_S^0 \rightarrow \gamma\gamma)/\Gamma_{\text{total}}] / [B(K_S^0 \rightarrow \pi^0\pi^0)] = (8.84 \pm 0.18 \pm 0.10) \times 10^{-6}$ which we multiply by our best value $B(K_S^0 \rightarrow \pi^0\pi^0) = (30.69 \pm 0.05) \times 10^{-2}$. Our first error is their experiment's error and our second error is the systematic error from using our best value.

³ BARR 95B result is calculated using $B(K_L \rightarrow \gamma\gamma) = (5.86 \pm 0.17) \times 10^{-4}$.

⁴ BARR 95B quotes this as the combined BARR 95B + BURKHARDT 87 result after rescaling BURKHARDT 87 to use same branching ratios and lifetimes as BARR 95B.

————— **Semileptonic modes** —————

$\Gamma(\pi^\pm e^\mp \nu_e)/\Gamma_{\text{total}}$ Γ_8/Γ

| <u>VALUE (units 10⁻⁴)</u> | <u>EVTS</u> | <u>DOCUMENT ID</u> | <u>TECN</u> | <u>COMMENT</u> |
|--------------------------------------|-------------|--------------------|-------------|----------------|
|--------------------------------------|-------------|--------------------|-------------|----------------|

7.04 ± 0.08 OUR FIT

7.04 ± 0.08 OUR AVERAGE

| | | | | |
|---------------------|-----|----------------------|----------|--|
| 7.046 ± 0.18 ± 0.16 | | ¹ BATLEY | 07D NA48 | K ⁰ (\bar{K}^0)(t) → π e ν |
| 6.91 ± 0.34 ± 0.15 | 624 | ² ALOISIO | 02 KLOE | Tagged K _S ⁰ using φ → K _L ⁰ K _S ⁰ |

• • • We use the following data for averages but not for fits. • • •

| | | | | |
|-------------|-----|------------------------|----------|------------|
| 7.05 ± 0.09 | 13k | ³ AMBROSINO | 06E KLOE | Not fitted |
|-------------|-----|------------------------|----------|------------|

• • • We do not use the following data for averages, fits, limits, etc. • • •

| | | | | |
|-----------|----|------------|---------|--|
| 7.2 ± 1.4 | 75 | AKHMETSHIN | 99 CMD2 | Tagged K _S ⁰ using φ → K _L ⁰ K _S ⁰ |
|-----------|----|------------|---------|--|

¹ Reconstructed from K⁰(\bar{K}^0)(t) → π e ν distributions using PDG values of B(K_L⁰ → π e ν) = 0.4053 ± 0.0015, τ_L = (5.114 ± 0.021) × 10⁻⁸ s and τ_S = (0.8958 ± 0.0005) × 10⁻¹⁰ s.

² Uses the PDG 00 value for B(K_S⁰ → π⁺ π⁻).

³ Obtained by imposing Σ_i B(K_S⁰ → i) = 1, where i runs over all the four branching ratios π⁺ π⁻, π⁰ π⁰, π e ν, and π μ ν. Input value of B(K_S⁰ → π⁺ π⁻) / B(K_S⁰ → π⁰ π⁰) from AMBROSINO 06C is used. To derive Γ(K_S⁰ → π⁺ μ ν) / Γ(K_S⁰ → π⁺ e ν), lepton universality is assumed, radiative corrections from ANDRE 07 are used, and phase space integrals are taken from KTeV, ALEXOPOULOS 04A. This branching fraction enters our fit via their Γ(π[±] e[∓] ν_e) / Γ(π⁺ π⁻) branching ratio measurement.

$\Gamma(\pi^\pm \mu^\mp \nu_\mu)/\Gamma_{\text{total}}$ Γ_9/Γ

| <u>VALUE (units 10⁻⁴)</u> | <u>EVTS</u> | <u>DOCUMENT ID</u> | <u>TECN</u> | <u>COMMENT</u> |
|--------------------------------------|-------------|--------------------|-------------|----------------|
|--------------------------------------|-------------|--------------------|-------------|----------------|

4.56 ± 0.20 OUR FIT

| | | | | |
|--------------------|------|----------------------|---------|--------------------|
| 4.56 ± 0.11 ± 0.17 | 7223 | ¹ BABUSCI | 20 KLOE | direct measurement |
|--------------------|------|----------------------|---------|--------------------|

¹ Value obtained by normalizing to the KLOE measurement B(K_S⁰ → π⁺ π⁻) = (69.196 ± 0.051)%. Also comparison with the PDG 18 based derived value leads to a lepton flavor universality test $|V_{us} f_+(0)|_{K_S^0 \rightarrow \pi \mu \nu}^2 / |V_{us} f_+(0)|_{K_S^0 \rightarrow \pi e \nu}^2 = 0.975 \pm 0.044$.

$\Gamma(\pi^\pm e^\mp \nu_e)/\Gamma(\pi^+ \pi^-)$ Γ_8/Γ_2

| <u>VALUE (units 10⁻⁴)</u> | <u>EVTS</u> | <u>DOCUMENT ID</u> | <u>TECN</u> |
|--------------------------------------|-------------|--------------------|-------------|
|--------------------------------------|-------------|--------------------|-------------|

10.18 ± 0.12 OUR FIT

| | | | |
|---------------------|-----|-----------|----------|
| 10.19 ± 0.11 ± 0.07 | 13k | AMBROSINO | 06E KLOE |
|---------------------|-----|-----------|----------|

————— **CP violating (CP) and ΔS = 1 weak neutral current (S1) modes** —————

$\Gamma(3\pi^0)/\Gamma_{\text{total}}$ Γ_{10}/Γ

Violates CP conservation.

| <u>VALUE (units 10⁻⁷)</u> | <u>CL%</u> | <u>EVTS</u> | <u>DOCUMENT ID</u> | <u>TECN</u> | <u>COMMENT</u> |
|--------------------------------------|------------|-------------|--------------------|-------------|----------------|
|--------------------------------------|------------|-------------|--------------------|-------------|----------------|

| | | | | | |
|------------------|----|------|----------------------|----------|---|
| < 0.26 | 90 | 590M | ¹ BABUSCI | 13C KLOE | φ → K _L ⁰ K _S ⁰ |
|------------------|----|------|----------------------|----------|---|

• • • We do not use the following data for averages, fits, limits, etc. • • •

| | | | | |
|-------|----|-------|-----------|----------|
| < 1.2 | 90 | 37.8M | AMBROSINO | 05B KLOE |
|-------|----|-------|-----------|----------|

| | | | | |
|-------|----|------|------------------|----------|
| < 7.4 | 90 | 4.9M | ² LAI | 05A NA48 |
|-------|----|------|------------------|----------|

| | | | | |
|-------|----|----|---------|---------|
| < 140 | 90 | 7M | ACHASOV | 99D SND |
|-------|----|----|---------|---------|

| | | | | |
|-------|----|-------|--------------------------|----------|
| < 190 | 90 | 17300 | ³ ANGELOPO... | 98B CPLR |
|-------|----|-------|--------------------------|----------|

| | | | | |
|-------|----|--|--------|---------|
| < 370 | 90 | | BARMIN | 83 HLBC |
|-------|----|--|--------|---------|

¹ BABUSCI 13C uses 1.7 fb^{-1} of data of $\phi \rightarrow K_L^0 K_S^0$ decays with K_L^0 interaction in the calorimeter, collected from 2004 to 2005. No candidate events were found in the data with an expected background of $0.04^{+0.15}_{-0.03}$ events. Upper limit is obtained by normalizing to $K_S^0 \rightarrow 2\pi^0$ decays.

² LAI 05A value is obtained from their bound on $|\eta_{000}|$ (not assuming *CPT*) and $B(K_L^0 \rightarrow 3\pi^0) = 0.211 \pm 0.003$, and PDG 04 values for K_L^0 and K_S^0 lifetimes. If *CPT* is assumed then $B(K_S^0 \rightarrow 3\pi^0)_{CPT} < 2.3 \times 10^{-7}$ at 90% CL

³ ANGELOPOULOS 98B is from $\text{Im}(\eta_{000}) = -0.05 \pm 0.12 \pm 0.05$, assuming $\text{Re}(\eta_{000}) = \text{Re}(\epsilon) = 1.635 \times 10^{-3}$ and using the value $B(K_L^0 \rightarrow \pi^0 \pi^0 \pi^0) = 0.2112 \pm 0.0027$.

$\Gamma(\mu^+ \mu^-)/\Gamma_{\text{total}}$

Γ_{11}/Γ

Test for $\Delta S = 1$ weak neutral current. Allowed by first-order weak interaction combined with electromagnetic interaction.

| VALUE | CL% | DOCUMENT ID | TECN |
|--|-----|-------------------|-----------|
| $< 2.1 \times 10^{-10}$ | 90 | ¹ AAIJ | 20AE LHCB |
| $< 8 \times 10^{-10}$ | 90 | ² AAIJ | 17BQ LHCB |
| $< 9 \times 10^{-9}$ | 90 | ³ AAIJ | 13G LHCB |
| $< 3.2 \times 10^{-7}$ | 90 | GJESDAL | 73 ASPK |
| $< 7 \times 10^{-6}$ | 90 | HYAMS | 69B OSPK |

¹ AAIJ 20AE uses 8.6 fb^{-1} of LHCb data from 2011 to 2012 and 2016 to 2018. The result utilizes the normalization mode branching fraction $B(K_S^0 \rightarrow \pi^+ \pi^-) = (69.20 \pm 0.05) \times 10^{-2}$ from PDG 18. Supersedes AAIJ 17BQ.

² AAIJ 17BQ uses 3.0 fb^{-1} of pp collisions at $\sqrt{s} = 7$ and 8 TeV. The result utilizes the normalization mode branching fraction $B(K_S^0 \rightarrow \pi^+ \pi^-) = (69.20 \pm 0.05) \times 10^{-2}$ from PDG 16. Supersedes AAIJ 13G.

³ AAIJ 13G uses 1.0 fb^{-1} of pp collisions at $\sqrt{s} = 7$ TeV. They obtained $B(K_S^0 \rightarrow \mu^+ \mu^-) < 11 \times 10^{-9}$ at 95% C.L.

$\Gamma(e^+ e^-)/\Gamma_{\text{total}}$

Γ_{12}/Γ

Test for $\Delta S = 1$ weak neutral current. Allowed by first-order weak interaction combined with electromagnetic interaction.

| VALUE (units 10^{-7}) | CL% | DOCUMENT ID | TECN | COMMENT |
|-------------------------------|-----|----------------------------|------|--|
| < 0.09 | 90 | ¹ AMBROSINO 09A | KLOE | $e^+ e^- \rightarrow \phi \rightarrow K_S^0 K_L^0$ |
| < 1.4 | 90 | ANGELOPO... | 97 | CPLR |
| < 28 | 90 | BLICK | 94 | CNTR Hyperon facility |
| < 100 | 90 | BARMIN | 86 | XEBC |

¹ AMBROSINO 09A reports $< 0.09 \times 10^{-7}$ from a measurement of $[\Gamma(K_S^0 \rightarrow e^+ e^-)/\Gamma_{\text{total}}] / [B(K_S^0 \rightarrow \pi^+ \pi^-)]$ assuming $B(K_S^0 \rightarrow \pi^+ \pi^-) = (69.20 \pm 0.05) \times 10^{-2}$.

$\Gamma(\pi^0 e^+ e^-)/\Gamma_{\text{total}}$

Γ_{13}/Γ

Test for $\Delta S = 1$ weak neutral current. Allowed by first-order weak interaction combined with electromagnetic interaction.

| VALUE (units 10^{-9}) | CL% | EVTS | DOCUMENT ID | TECN | COMMENT |
|---|-----|------|---------------------|---------|------------------------------|
| $3.0^{+1.5}_{-1.2} \pm 0.2$ | | 7 | ¹ BATLEY | 03 NA48 | $m_{ee} > 0.165 \text{ GeV}$ |

• • • We do not use the following data for averages, fits, limits, etc. • • •

| | | | | | |
|--------|----|---|---------|-----|------|
| < 140 | 90 | | LAI | 01 | NA48 |
| < 1100 | 90 | 0 | BARR | 93B | NA31 |
| <45000 | 90 | | GIBBONS | 88 | E731 |

¹ BATLEY 03 extrapolate also to the full kinematical region using a constant form factor and a vector matrix element. The resulting branching ratio is $(5.8^{+2.9}_{-2.4}) \times 10^{-9}$.

$\Gamma(\pi^0 \mu^+ \mu^-) / \Gamma_{\text{total}}$ Γ_{14} / Γ
 Test for $\Delta S = 1$ weak neutral current. Allowed by first-order weak interaction combined with electromagnetic interaction.

| VALUE (units 10^{-9}) | EVTS | DOCUMENT ID | TECN | COMMENT |
|-----------------------------|------|---------------------|----------|---------------------|
| $2.9^{+1.5}_{-1.2} \pm 0.2$ | 6 | ¹ BATLEY | 04A NA48 | NA48/1 K_S^0 beam |

¹ Background estimate is $0.22^{+0.18}_{-0.11}$ events. Branching ratio assumes a vector matrix element and unit form factor.

K_S^0 FORM FACTORS

For discussion, see note on $K_{\ell 3}$ form factors in the K^\pm section of the Particle Listings above. Because the semileptonic branching fraction is smaller in K_S^0 than K_L^0 by the ratio of the mean lives, the K_S^0 semileptonic form factor has so far been measured only in the K_{e3} mode using the linear expansion $f_+(t) = f_+(0) (1 + \lambda_+ t / m_{\pi^+}^2)$, which gives the vector form factor $f_+(t)$ relative to its value at $t = 0$.

λ_+ (LINEAR ENERGY DEPENDENCE OF f_+ IN K_{e3}^0 DECAY)

| VALUE (units 10^{-2}) | EVTS | DOCUMENT ID | TECN |
|--------------------------|------|---------------|------|
| 3.39 ± 0.41 | 15k | AMBROSINO 06E | KLOE |

CP VIOLATION IN $K_S \rightarrow 3\pi$

Written 1996 by T. Nakada (Paul Scherrer Institute) and L. Wolfenstein (Carnegie-Mellon University).

The possible final states for the decay $K^0 \rightarrow \pi^+ \pi^- \pi^0$ have isospin $I = 0, 1, 2,$ and 3 . The $I = 0$ and $I = 2$ states have $CP = +1$ and K_S can decay into them without violating CP symmetry, but they are expected to be strongly suppressed by centrifugal barrier effects. The $I = 1$ and $I = 3$ states, which have no centrifugal barrier, have $CP = -1$ so that the K_S decay to these requires CP violation.

In order to see CP violation in $K_S \rightarrow \pi^+\pi^-\pi^0$, it is necessary to observe the interference between K_S and K_L decay, which determines the amplitude ratio

$$\eta_{+-0} = \frac{A(K_S \rightarrow \pi^+\pi^-\pi^0)}{A(K_L \rightarrow \pi^+\pi^-\pi^0)}. \quad (1)$$

If η_{+-0} is obtained from an integration over the whole Dalitz plot, there is no contribution from the $I = 0$ and $I = 2$ final states and a nonzero value of η_{+-0} is entirely due to CP violation.

Only $I = 1$ and $I = 3$ states, which are $CP = -1$, are allowed for $K^0 \rightarrow \pi^0\pi^0\pi^0$ decays and the decay of K_S into $3\pi^0$ is an unambiguous sign of CP violation. Similarly to η_{+-0} , η_{000} is defined as

$$\eta_{000} = \frac{A(K_S \rightarrow \pi^0\pi^0\pi^0)}{A(K_L \rightarrow \pi^0\pi^0\pi^0)}. \quad (2)$$

If one assumes that CPT invariance holds and that there are no transitions to $I = 3$ (or to nonsymmetric $I = 1$ states), it can be shown that

$$\begin{aligned} \eta_{+-0} &= \eta_{000} \\ &= \epsilon + i \frac{\text{Im } a_1}{\text{Re } a_1}. \end{aligned} \quad (3)$$

With the Wu-Yang phase convention, a_1 is the weak decay amplitude for K^0 into $I = 1$ final states; ϵ is determined from CP violation in $K_L \rightarrow 2\pi$ decays. The real parts of η_{+-0} and η_{000} are equal to $\text{Re}(\epsilon)$. Since currently-known upper limits on $|\eta_{+-0}|$ and $|\eta_{000}|$ are much larger than $|\epsilon|$, they can be interpreted as upper limits on $\text{Im}(\eta_{+-0})$ and $\text{Im}(\eta_{000})$ and so as limits on the CP -violating phase of the decay amplitude a_1 .

CP-VIOLATION PARAMETERS IN K_S^0 DECAY

$$A_S = [\Gamma(K_S^0 \rightarrow \pi^- e^+ \nu_e) - \Gamma(K_S^0 \rightarrow \pi^+ e^- \bar{\nu}_e)] / \text{SUM}$$

Such asymmetry violates *CP*. If *CPT* is assumed then $A_S = 2 \text{Re}(\epsilon)$.

| VALUE (units 10^{-3}) | EVTS | DOCUMENT ID | TECN |
|--------------------------|------|---------------------------|------|
| $-3.8 \pm 5.0 \pm 2.6$ | 83k | ¹ ANASTASI 18A | KLOE |

• • • We do not use the following data for averages, fits, limits, etc. • • •

| | | | |
|-----------------------|-----|---------------|------|
| $1.5 \pm 9.6 \pm 2.9$ | 13k | AMBROSINO 06E | KLOE |
|-----------------------|-----|---------------|------|

¹ ANASTASI 18A result is a combination of the new measurement and AMBROSINO 06E. The new ANASTASI 18A measurement using data collected from 2004–2005, which corresponds to an integrated luminosity of 1.63 fb^{-1} is $A_S = (-4.9 \pm 5.7 \pm 2.6) \times 10^{-3}$.

PARAMETERS FOR $K_S^0 \rightarrow 3\pi$ DECAY

$$\text{Im}(\eta_{+-0})^2 = \Gamma(K_S^0 \rightarrow \pi^+ \pi^- \pi^0, \text{CP-violating}) / \Gamma(K_L^0 \rightarrow \pi^+ \pi^- \pi^0)$$

CPT assumed valid (i.e. $\text{Re}(\eta_{+-0}) \simeq 0$).

| VALUE | CL% | EVTS | DOCUMENT ID | TECN |
|-------|-----|------|-------------|------|
|-------|-----|------|-------------|------|

• • • We do not use the following data for averages, fits, limits, etc. • • •

| | | | | |
|-------|----|-----|------------------------|------|
| <0.23 | 90 | 601 | ¹ BARMIN 85 | HLBC |
| <0.12 | 90 | 384 | METCALF 72 | ASPK |

¹ BARMIN 85 find $\text{Re}(\eta_{+-0}) = (0.05 \pm 0.17)$ and $\text{Im}(\eta_{+-0}) = (0.15 \pm 0.33)$. Includes events of BALDO-CEOLIN 75.

$$\text{Im}(\eta_{+-0}) = \text{Im}(A(K_S^0 \rightarrow \pi^+ \pi^- \pi^0, \text{CP-violating}) / A(K_L^0 \rightarrow \pi^+ \pi^- \pi^0))$$

| VALUE | EVTS | DOCUMENT ID | TECN | COMMENT |
|-------|------|-------------|------|---------|
|-------|------|-------------|------|---------|

| | | | | |
|--------------------------------|------|------------------------|------|--|
| -0.002 ± 0.009 -0.001 | 500k | ¹ ADLER 97B | CPLR | |
|--------------------------------|------|------------------------|------|--|

• • • We do not use the following data for averages, fits, limits, etc. • • •

| | | | | |
|------------------------------|------|------------------------|------|-------------------|
| $-0.002 \pm 0.018 \pm 0.003$ | 137k | ² ADLER 96D | CPLR | Sup. by ADLER 97B |
| $-0.015 \pm 0.017 \pm 0.025$ | 272k | ³ ZOU 94 | SPEC | |

¹ ADLER 97B also find $\text{Re}(\eta_{+-0}) = -0.002 \pm 0.007$
 -0.001 . See also ANGELOPOULOS 98c.

² The ADLER 96D fit also yields $\text{Re}(\eta_{+-0}) = 0.006 \pm 0.013 \pm 0.001$ with a correlation +0.66 between real and imaginary parts. Their results correspond to $|\eta_{+-0}| < 0.037$ with 90% CL.

³ ZOU 94 use theoretical constraint $\text{Re}(\eta_{+-0}) = \text{Re}(\epsilon) = 0.0016$. Without this constraint they find $\text{Im}(\eta_{+-0}) = 0.019 \pm 0.061$ and $\text{Re}(\eta_{+-0}) = 0.019 \pm 0.027$.

$$\text{Im}(\eta_{000})^2 = \Gamma(K_S^0 \rightarrow 3\pi^0) / \Gamma(K_L^0 \rightarrow 3\pi^0)$$

CPT assumed valid (i.e. $\text{Re}(\eta_{000}) \simeq 0$). This limit determines branching ratio $\Gamma(3\pi^0) / \Gamma_{\text{total}}$ above.

| VALUE | CL% | EVTS | DOCUMENT ID | TECN | COMMENT |
|-------|-----|------|-------------|------|---------|
|-------|-----|------|-------------|------|---------|

• • • We do not use the following data for averages, fits, limits, etc. • • •

| | | | | | |
|-------|----|-----|--------------------------|------|----------------|
| <0.1 | 90 | 632 | ¹ BARMIN 83 | HLBC | |
| <0.28 | 90 | | ² GJESDAL 74B | SPEC | Indirect meas. |

¹ BARMIN 83 find $\text{Re}(\eta_{000}) = (-0.08 \pm 0.18)$ and $\text{Im}(\eta_{000}) = (-0.05 \pm 0.27)$. Assuming *CPT* invariance they obtain the limit quoted above.

² GJESDAL 74B uses $K_{2\pi}$, $K_{\mu 3}$, and $K_{e 3}$ decay results, unitarity, and *CPT*. Calculates $|\eta_{000}| = 0.26 \pm 0.20$. We convert to upper limit.

$$\text{Im}(\eta_{000}) = \text{Im}(A(K_S^0 \rightarrow \pi^0 \pi^0 \pi^0)/A(K_L^0 \rightarrow \pi^0 \pi^0 \pi^0))$$

$K_S^0 \rightarrow \pi^0 \pi^0 \pi^0$ violates CP conservation, in contrast to $K_S^0 \rightarrow \pi^+ \pi^- \pi^0$ which has a CP -conserving part.

| VALUE | EVTS | DOCUMENT ID | TECN | COMMENT |
|---------------------------------|-------|--------------------------|----------|---------------|
| -0.001±0.016 OUR AVERAGE | | | | |
| 0.000±0.009±0.013 | 4.9M | ¹ LAI | 05A NA48 | Assumes CPT |
| -0.05 ±0.12 ±0.05 | 17300 | ² ANGELOPO... | 98B CPLR | Assumes CPT |

¹ LAI 05A assumes $\text{Re}(\eta_{000})=\text{Re}(\epsilon)=1.66 \times 10^{-3}$. The equivalent limit is $|\eta_{000}|_{CPT} < 0.025$ at 90% CL Without assuming CPT invariance, they obtain $\text{Re}(\eta_{000})=-0.002 \pm 0.011 \pm 0.015$ and $\text{Im}(\eta_{000})=-0.003 \pm 0.013 \pm 0.017$ with a statistical correlation coefficient of 0.77 and an overall correlation coefficient of 0.57 between imaginary and real part. The equivalent limit is $|\eta_{000}| < 0.045$ at 90% CL

² ANGELOPOULOS 98B assumes $\text{Re}(\eta_{000}) = \text{Re}(\epsilon) = 1.635 \times 10^{-3}$. Without assuming CPT invariance, they obtain $\text{Re}(\eta_{000}) = 0.18 \pm 0.14 \pm 0.06$ and $\text{Im}(\eta_{000}) = 0.15 \pm 0.20 \pm 0.03$.

$$|\eta_{000}| = |A(K_S^0 \rightarrow 3\pi^0)/A(K_L^0 \rightarrow 3\pi^0)|$$

A non-zero value violates CP invariance.

| VALUE | CL% | EVTS | DOCUMENT ID | TECN |
|---|-----|-------|-------------|----------|
| <0.0088 | 90 | 590M | BABUSCI | 13C KLOE |
| • • • We do not use the following data for averages, fits, limits, etc. • • • | | | | |
| <0.018 | 90 | 37.8M | AMBROSINO | 05B KLOE |
| <0.045 | 90 | 4.9M | LAI | 05A NA48 |

DECAY-PLANE ASYMMETRY IN $\pi^+ \pi^- e^+ e^-$ DECAYS

This is the CP -violating asymmetry

$$A = \frac{N_{\sin\phi\cos\phi>0.0} - N_{\sin\phi\cos\phi<0.0}}{N_{\sin\phi\cos\phi>0.0} + N_{\sin\phi\cos\phi<0.0}}$$

where ϕ is the angle between the $e^+ e^-$ and $\pi^+ \pi^-$ planes in the K_S^0 rest frame.

CP asymmetry A in $K_S^0 \rightarrow \pi^+ \pi^- e^+ e^-$

| VALUE (%) | DOCUMENT ID | TECN | COMMENT |
|---|---------------------|------|---------------------|
| -0.4±0.8 OUR AVERAGE | | | |
| -0.4±0.8 | ¹ BATLEY | 11 | NA48 2002 data |
| -1.1±4.1 | LAI | 03C | NA48 1998+1999 data |
| • • • We do not use the following data for averages, fits, limits, etc. • • • | | | |
| 0.5±4.0±1.6 | LAI | 03C | NA48 1999 data |

¹ The result is used to set the limit $A < 1.5\%$ at 90% C.L.

K_S^0 REFERENCES

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| ZOU | 96 | PL B369 362 | Y. Zou <i>et al.</i> | (RUTG, MINN, MICH) |
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| BLICK | 94 | PL B334 234 | A.M. Blick <i>et al.</i> | (SERP, JINR) |
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