

## 2. Astrophysical Constants and Parameters

**Table 2.1.** Revised October 2017 by D.E. Groom (LBNL) and D. Scott (University of British Columbia). The figures in parentheses after some values give the  $1\text{-}\sigma$  uncertainties in the last digit(s). Physical constants are from Ref. 1. While every effort has been made to obtain the most accurate current values of the listed quantities, the table does not represent a critical review or adjustment of the constants, and is not intended as a primary reference. The values and uncertainties for the cosmological parameters depend on the exact data sets, priors, and basis parameters used in the fit. Many of the derived parameters reported in this table have non-Gaussian likelihoods. Parameters may be highly correlated, so care must be taken in propagating errors. Unless otherwise specified, cosmological parameters are derived from a 6-parameter  $\Lambda$ CDM cosmology fit to *Planck* 2015 temperature (TT) + low  $\ell$  polarization (lowP) + lensing data [2]. For more information see Ref. 3 and the original papers.

Quantity	Symbol, equation	Value	Reference, footnote
Newtonian constant of gravitation	$G_N$	$6.674\,08(31) \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$	[1]
Planck mass	$\sqrt{\hbar c/G_N}$	$1.220\,910(29) \times 10^{19} \text{ GeV}/c^2 = 2.176\,47(5) \times 10^{-8} \text{ kg}$	[1]
Planck length	$\sqrt{\hbar G_N/c^3}$	$1.616\,229(38) \times 10^{-35} \text{ m}$	[1]
tropical year (equinox to equinox) (2011)	yr	$31\,556\,925.2 \text{ s} \approx \pi \times 10^7 \text{ s}$	[4]
sidereal year (fixed star to fixed star) (2011)		$31\,558\,149.8 \text{ s} \approx \pi \times 10^7 \text{ s}$	[4]
mean sidereal day (2011) (time between vernal equinox transits)		$23^{\text{h}}\,56^{\text{m}}\,04^{\text{s}}.090\,53$	[4]
astronomical unit	au	$149\,597\,870\,700 \text{ m}$	exact[5]
parsec (1 au/1 arc sec)	pc	$3.085\,677\,581\,49 \times 10^{16} \text{ m} = 3.262 \dots \text{ ly}$	exact[6]
light year (deprecated unit)	ly	$0.306\,6 \dots \text{ pc} = 0.946\,053 \dots \times 10^{16} \text{ m}$	
Solar mass	$M_\odot$	$1.988\,48(9) \times 10^{30} \text{ kg}$	[7]
Schwarzschild radius of the Sun	$2G_N M_\odot/c^2$	$2.953\,250\,24 \text{ km}$	[8]
nominal Solar equatorial radius	$\mathcal{R}_\odot$	$6.957 \times 10^8 \text{ m}$	exact[9]
nominal Solar constant	$\mathcal{S}_\odot$	$1361 \text{ W m}^{-2}$	exact[9,10]
nominal Solar photosphere temperature	$T_\odot$	$5772 \text{ K}$	exact[9]
nominal Solar luminosity	$\mathcal{L}_\odot$	$3.828 \times 10^{26} \text{ W}$	exact[9,11]
Earth mass	$M_\oplus$	$5.972\,4(3) \times 10^{24} \text{ kg}$	[7]
Schwarzschild radius of the Earth	$2G_N M_\oplus/c^2$	$8.870\,056\,580(18) \text{ mm}$	[12]
nominal Earth equatorial radius	$\mathcal{R}_\oplus$	$6.3781 \times 10^6 \text{ m}$	exact[9]
jansky (flux density)	Jy	$10^{-26} \text{ W m}^{-2} \text{ Hz}^{-1}$	definition
luminosity conversion	$L$	$3.0128 \times 10^{28} \times 10^{-0.4 M_{\text{bol}}} \text{ W}$	[13]
flux conversion	$\mathcal{F}$	$(M_{\text{bol}} = \text{absolute bolometric magnitude} = \text{bolometric magnitude at } 10 \text{ pc})$ $2.5180 \times 10^{-8} \times 10^{-0.4 m_{\text{bol}}} \text{ W m}^{-2}$	[13]
ABsolute monochromatic magnitude	AB	$(m_{\text{bol}} = \text{apparent bolometric magnitude})$ $-2.5 \log_{10} f_\nu - 56.10$ (for $f_\nu$ in $\text{W m}^{-2} \text{ Hz}^{-1}$ ) $= -2.5 \log_{10} f_\nu + 8.90$ (for $f_\nu$ in Jy)	[14]
Solar angular velocity around the Galactic center	$\Theta_0/R_0$	$30.3 \pm 0.9 \text{ km s}^{-1} \text{ kpc}^{-1}$	[15]
Solar distance from Galactic center	$R_0$	$8.00 \pm 0.25 \text{ kpc}$	[15,16]
circular velocity at $R_0$	$v_0$ or $\Theta_0$	$254(16) \text{ km s}^{-1}$	[15]
escape velocity from Galaxy	$v_{\text{esc}}$	$498 \text{ km/s} < v_{\text{esc}} < 608 \text{ km/s}$	[17]
local disk density	$\rho_{\text{disk}}$	$3\text{--}12 \times 10^{-24} \text{ g cm}^{-3} \approx 2\text{--}7 \text{ GeV}/c^2 \text{ cm}^{-3}$	[18]
local dark matter density	$\rho_\chi$	canonical value $0.3 \text{ GeV}/c^2 \text{ cm}^{-3}$ within factor 2–3	[19]
present day CMB temperature	$T_0$	$2.7255(6) \text{ K}$	[20,21]
present day CMB dipole amplitude	$d$	$3.3645(20) \text{ mK}$	[20,22]
Solar velocity with respect to CMB	$v_\odot$	$370.09(22) \text{ km s}^{-1}$ towards $(\ell, b) = (263.00(3)^\circ, 48.24(2)^\circ)$	[22]
Local Group velocity with respect to CMB	$v_{\text{LG}}$	$627(22) \text{ km s}^{-1}$ towards $(\ell, b) = (276(3)^\circ, 30(3)^\circ)$	[20,23]
number density of CMB photons	$n_\gamma$	$410.7(3) (T/2.7255)^3 \text{ cm}^{-3}$	[24]
density of CMB photons	$\rho_\gamma$	$4.645(4) (T/2.7255)^4 \times 10^{-34} \text{ g cm}^{-3} \approx 0.260 \text{ eV cm}^{-3}$	[24]
entropy density/Boltzmann constant	$s/k$	$2891.2 (T/2.7255)^3 \text{ cm}^{-3}$	[24]
present day Hubble expansion rate	$H_0$	$100 h \text{ km s}^{-1} \text{ Mpc}^{-1} = h \times (9.777\,752 \text{ Gyr})^{-1}$	[25]
scale factor for Hubble expansion rate	$h$	$0.678(9)$	[2,26]
Hubble length	$c/H_0$	$0.925\,0629 \times 10^{26} h^{-1} \text{ m} = 1.374(18) \times 10^{26} \text{ m}$	
scale factor for cosmological constant	$c^2/3H_0^2$	$2.85247 \times 10^{51} h^{-2} \text{ m}^2 = 6.20(17) \times 10^{51} \text{ m}^2$	
critical density of the Universe	$\rho_{\text{crit}} = 3H_0^2/8\pi G_N$	$1.878\,40(9) \times 10^{-29} h^2 \text{ g cm}^{-3}$ $= 1.053\,71(5) \times 10^{-5} h^2 (\text{GeV}/c^2) \text{ cm}^{-3}$ $= 2.775\,37(13) \times 10^{11} h^2 M_\odot \text{ Mpc}^{-3}$	
baryon-to-photon ratio (from BBN)	$\eta = n_{\text{b}}/n_\gamma$	$5.8 \times 10^{-10} \leq \eta \leq 6.6 \times 10^{-10}$ (95% CL)	[27]
number density of baryons	$n_{\text{b}}$	$2.503(26) \times 10^{-7} \text{ cm}^{-3}$ $(2.4 \times 10^{-7} < n_{\text{b}} < 2.7 \times 10^{-7}) \text{ cm}^{-3}$ (95% CL)	[2,3,28,29] $\eta \times n_\gamma$
CMB radiation density of the Universe	$\Omega_\gamma = \rho_\gamma/\rho_{\text{crit}}$	$2.473 \times 10^{-5} (T/2.7255)^4 h^{-2} = 5.38(15) \times 10^{-5}$	[24]
--- <i>Planck</i> 2015 6-parameter fit to flat $\Lambda$ CDM cosmology			
baryon density of the Universe	$\Omega_{\text{b}} = \rho_{\text{b}}/\rho_{\text{crit}}$	$\ddagger 0.02226(23) h^{-2} = \dagger 0.0484(10)$	[2,3,22]
cold dark matter density of the Universe	$\Omega_{\text{c}} = \rho_{\text{c}}/\rho_{\text{crit}}$	$\ddagger 0.1186(20) h^{-2} = \dagger 0.258(11)$	[2,3,22]
100 $\times$ approx to $r_*/D_{\text{A}}$	$100 \times \theta_{\text{MC}}$	$\ddagger 1.0410(5)$	[2,3]
reionization optical depth	$\tau$	$\ddagger 0.066(16)$	[2,3,30]
scalar spectral index	$n_{\text{s}}$	$\ddagger 0.968(6)$	[2,3]
ln power prim. curv. pert. ( $k_0=0.05 \text{ Mpc}^{-1}$ )	$\ln(10^{10} \Delta_{\text{R}}^2)$	$\ddagger 3.062(29)$	[2,3]

Quantity	Symbol, equation	Value	Reference, footnote
dark energy density of the Universe	$\Omega_\Lambda$	$\dagger 0.692 \pm 0.012$	[2,3]
pressureless matter density of the Universe	$\Omega_m = \Omega_c + \Omega_b$	$\dagger 0.308 \pm 0.012$	[2,3]
fluctuation amplitude at $8 h^{-1}$ Mpc scale	$\sigma_8$	$\dagger 0.815 \pm 0.009$	[2,3]
redshift of matter-radiation equality	$z_{\text{eq}}$	$\dagger 3365 \pm 44$	[2]
redshift at which optical depth equals unity	$z_*$	$\dagger 1089.9 \pm 0.4$	[2]
comoving size of sound horizon at $z_*$	$r_*$	$\dagger 144.9 \pm 0.4$ Mpc	( <i>Planck</i> CMB) [31]
age when optical depth equals unity	$t_*$	373 kyr	[32]
redshift at half reionization	$z_{\text{reion}}$	$\dagger 8.8_{-1.4}^{+1.7}$	[2,33]
redshift when acceleration was zero	$z_q$	$\approx 0.65$	[32]
age of the Universe	$t_0$	$\dagger 13.80 \pm 0.04$ Gyr	[2]
effective number of neutrinos	$N_{\text{eff}}$	$\# 3.13 \pm 0.32$	[2,34,35]
sum of neutrino masses	$\sum m_\nu$	$\# < 0.68$ eV ( <i>Planck</i> CMB); $\geq 0.06$ eV (mixing)	[2,35,36,37]
neutrino density of the Universe	$\Omega_\nu = h^{-2} \sum m_{\nu_j} / 93.14$ eV	$\# < 0.016$ ( <i>Planck</i> CMB); $\geq 0.0012$ (mixing)	[2,36,37]
curvature	$\Omega_K$	$\# -0.005_{-0.017}^{+0.016}$ (95%CL)	[2]
running spectral index slope, $k_0 = 0.002$ Mpc $^{-1}$	$dn_s/d \ln k$	$\# -0.003(15)$	[2]
tensor-to-scalar field perturbations ratio, $k_0=0.002$ Mpc $^{-1}$	$r_{0.002} = T/S$	$\# < 0.114$ at 95% CL; no running	[2,3,20,38]
dark energy equation of state parameter	$w$	$-1.01 \pm 0.04$	[31,39]
primordial helium fraction	$Y_p$	$0.245 \pm 0.004$	[20,40]

$\ddagger$  Parameter in 6-parameter  $\Lambda$ CDM fit;  $\dagger$  Derived parameter in 6-parameter  $\Lambda$ CDM fit;  $\#$  Extended model parameter, *Planck* data only [2].

### References:

- CODATA recommended 2014 values of the fundamental physical constants: [physics.nist.gov/constants](http://physics.nist.gov/constants).
- Planck Collab. 2015 Results XIII, *Astron. & Astrophys.* **594**, A13 (2016), [arXiv:1502.01589v2](https://arxiv.org/abs/1502.01589v2).
- O. Lahav & A.R. Liddle, “The Cosmological Parameters,” Sec. 25 in this *Review*.
- The Astronomical Almanac Online for the year 2016*, [asa.usno.navy.mil/SecK/Constants.html](http://asa.usno.navy.mil/SecK/Constants.html).
- The astronomical unit of length (au) in meters is re-defined (resolution B2, IAU XXVIII General Assembly 2012) to be a conventional unit of length in agreement with the value adopted in IAU 2009 Resolution B2; it is to be used with all time scales.
- The distance at which 1 au subtends 1 arc sec: 1 au divided by  $\pi/648000$ .
- $G_N M$  [4]  $\div G_N$  [1] for either the Sun or the Earth.
- Product of  $2/c^2$  and the observationally determined Solar mass parameter  $G_N M_\odot$  [4]. Truncated to 8 places so that TCB and TDB time scale values agree.
- IAU XXIX GA, Resolution B3, “on recommended nominal conversion constants ...” Calligraphic symbol indicates recommended nominal value.
- See also G. Kopp & J.L. Lean, *Geophys. Res. Lett.* **38**, L01706 (2011), who give  $1360.8 \pm 0.6$  W m $^{-2}$ . See paper for caveats and other measurements.
- $4\pi (1 \text{ au})^2 \times \mathcal{S}_\odot$ , assuming isotropic irradiance.
- Product of  $2/c^2$  and the geocentric gravitational constant  $G_N M_\oplus$  [4]. Truncated to 8 places so that TCB, TT, and TDB time scale values agree.
- IAU XXIX GA, Resolution B2, “on recommended zero points for the absolute and apparent bolometric magnitude scales”.
- J. B. Oke and J. E. Gunn, *Astrophys. J.* **266**, 713 (1983). Note that in the original definition the sign of the constant is wrong.
- M.J. Reid, *et al.*, *Astrophys. J.* **700**, 137 (2009). Note that  $\Theta_0/R_0$  is better determined than either  $\Theta_0$  or  $R_0$ .
- Z.M. Malkin, [arXiv:1202.6128](https://arxiv.org/abs/1202.6128) and *Astron. Rep.* **57**, 128 (2013). 52 determinations of  $R_0$  over 20 years are given. The weighted mean of these *unevaluated* results is  $7.94 \pm 0.05$  kpc, with  $\chi^2/N_{\text{dof}} = 1.26$ . If the 8 values more than  $3\sigma$  from the mean are eliminated,  $\langle R_0 \rangle = 8.02 \pm 0.06$  kpc and  $\chi^2/N_{\text{dof}} = 0.67$ . The author suggests using  $R_0 = 8.00 \pm 0.25$  kpc.
- M. C. Smith *et al.*, *MNRAS* **379**, 755 (2007).
- G. Gilmore, R.F.G. Wyse, & K. Kuijken, *Ann. Rev. Astron. & Astrophys.* **27**, 555 (1989).
- Sampling of many references: M. Mori *et al.*, *Phys. Lett.* **B289**, 463 (1992); E.I. Gates *et al.*, *Astrophys. J.* **449**, L133 (1995); M. Kamionkowski & A. Kinkhabwala, *Phys. Rev.* **D57**, 325 (1998); M. Weber & W. de Boer, *Astron. & Astrophys.* **509**, A25 (2010); P. Salucci *et al.*, *Astron. & Astrophys.* **523**, A83 (2010); R. Catena & P. Ullio, *JCAP* **1008**, 004 (2010). The conclusion is  $\rho_{\text{DM}}^{\text{local}} = 0.39 \pm 0.03$  GeV cm $^{-3}$ .
- D. Scott & G.F. Smoot, “Cosmic Microwave Background,” Sec. 29 in this *Review*.
- D. Fixsen, *Astrophys. J.* **707**, 916 (2009).
- Planck Collab. 2015 Results I, *Astron. & Astrophys.* **594**, A1 (2016), [arXiv:1502.01581v3](https://arxiv.org/abs/1502.01581v3).
- D.J. Fixsen *et al.*, *Astrophys. J.* **473**, 576 (1996); A. Kogut *et al.*, *Astrophys. J.* **419**, 1 (1993).
- $n_\gamma = \frac{2\zeta(3)}{\pi^2} \left(\frac{kT}{hc}\right)^3$ ;  $\rho_\gamma = \frac{\pi^2 kT}{15 c^2} \left(\frac{kT}{hc}\right)^3$ ;  $s/k = \frac{2 \cdot 43 \cdot \pi^2}{11 \cdot 45} \left(\frac{kT}{hc}\right)^3$ ;  $kT/hc = 11.902(3)(T/2.7255)/\text{cm}$ .
- Conversion using length of sidereal year.
- Measurements from traditional cosmic distance-ladder methods tend to be higher, *e.g.*,  $0.732 \pm 0.017$  from A.G. Riess *et al.*, *Astrophys. J.* **826**, 56 (2016); for discussion see O. Lahav & A.R. Liddle, “The Cosmological Parameters,” Sec. 25 in this *Review*.
- B.D. Fields, P. Molarto, & S. Sarkar, “Big-Bang Nucleosynthesis,” in this *Review*.
- $n_b$  depends only upon the measured  $\Omega_b h^2$ , the average baryon mass at the present epoch [29], and  $G_N$ :  $n_b = (\Omega_b h^2)(h^{-2} \rho_{\text{crit}})/(0.93711 \text{ GeV}/c^2 \text{ per baryon})$ .
- G. Steigman, *JCAP* **10**, 016, (2006).
- Planck Collab. Interm. Results XLVI, *Astron. & Astrophys.* **596**, A107 (2016) describes an improved study yielding the lower value  $0.055 \pm 0.009$ , although a full *Planck* polarization analysis has yet to appear.
- D.H. Weinberg, M. White, “Dark Energy,” Sec. 28 in this *Review*.
- D. Scott, A. Narimani, & D.N. Page, *Phys. Canada* **70**, 258 (2015), [arXiv:1309.2381v2](https://arxiv.org/abs/1309.2381v2).
- Planck Collab. Interm. Results XLVI, *Astron. & Astrophys.* **596**, A108 (2016) revise this to  $7.8\text{--}8.8 (\pm 0.9)$ , depending on the reionization model.
- Summary Tables in this *Review* list  $N_\nu = 2.984(8)$  (Standard Model fits to LEP-SLC data). Because neutrinos are not completely decoupled at  $e^\pm$  annihilation, the effective number of massless neutrino species is 3.046, rather than 3.
- J. Lesgourgues & L. Verde, “Neutrinos in Cosmology,” Sec. 26 in this *Review*.
- The sum is over all neutrino mass eigenstates, the lower limit following from neutrino mixing results reported in this *Review* combined with the assumptions that there are three light neutrinos and that the lightest neutrino is substantially less massive than the others.
- Astrophysical determinations of  $\sum m_{\nu_j}$ , reported in the Full Listings of this *Review* under “Sum of the neutrino masses,” range from  $< 0.17$  eV to  $< 2.3$  eV in papers published since 2003.
- Combining this with a direct upper limit on CMB  $B$  modes, cleaned using *Planck* polarization data, gives  $r < 0.07$ , Keck Array and BICEP2 Collabs. V, *Astrophys. J.* **811**, 126, (2015).
- S. Alam *et al.*, *MNRAS* **470**, 2617 (2017).
- E. Aver *et al.*, *JCAP* **07**, 011 (2015).