

**$\eta'(958)$**

$$I^G(J^{PC}) = 0^+(0^{-+})$$

**$\eta'(958)$  MASS**

<u>VALUE (MeV)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>957.78 ± 0.06 OUR AVERAGE</b>				
957.793 ± 0.054 ± 0.036	3.9k	LIBBY	08	CLEO $J/\psi \rightarrow \gamma\eta'$
957.9 ± 0.2 ± 0.6	4800	WURZINGER	96	SPEC 1.68 $pd \rightarrow {}^3\text{He}\eta'$
957.46 ± 0.33		DUANE	74	MMS $\pi^- p \rightarrow n\text{MM}$
958.2 ± 0.5	1414	DANBURG	73	HBC 2.2 $K^- p \rightarrow \Lambda\eta'$
958 ± 1	400	JACOBS	73	HBC 2.9 $K^- p \rightarrow \Lambda\eta'$
956.1 ± 1.1	3415	<sup>1</sup> BASILE	71	CNTR 1.6 $\pi^- p \rightarrow n\eta'$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
957.5 ± 0.2		BAI	04J	BES2 $J/\psi \rightarrow \gamma\gamma\pi^+\pi^-$
959 ± 1	630	<sup>2</sup> BELADIDZE	92C	VES 36 $\pi^- \text{Be} \rightarrow \pi^- \eta' \eta \text{Be}$
958 ± 1	340	<sup>2</sup> ARMSTRONG	91B	OMEG 300 $pp \rightarrow pp\eta\pi^+\pi^-$
958.2 ± 0.4	622	<sup>2</sup> AUGUSTIN	90	DM2 $J/\psi \rightarrow \gamma\eta\pi^+\pi^-$
957.8 ± 0.2	2420	<sup>2</sup> AUGUSTIN	90	DM2 $J/\psi \rightarrow \gamma\gamma\pi^+\pi^-$
956.3 ± 1.0	143	<sup>2</sup> GIDAL	87	MRK2 $e^+e^- \rightarrow e^+e^-\eta\pi^+\pi^-$
957.4 ± 1.4	535	<sup>3</sup> BASILE	71	CNTR 1.6 $\pi^- p \rightarrow n\eta'$
957 ± 1		RITTENBERG	69	HBC 1.7-2.7 $K^- p$

<sup>1</sup> Using all  $\eta'$  decays.

<sup>2</sup> Systematic uncertainty not estimated.

<sup>3</sup> Using  $\eta'$  decays into neutrals. Not independent of the other listed BASILE 71  $\eta'$  mass measurement.

**$\eta'(958)$  WIDTH**

<u>VALUE (MeV)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>	<u>COMMENT</u>
<b>0.196 ± 0.009 OUR FIT</b>					
<b>0.230 ± 0.021 OUR AVERAGE</b>					
0.226 ± 0.017 ± 0.014	2300	CZERWINSKI	10	MMS	$pp \rightarrow pp\eta'$
0.40 ± 0.22	4800	WURZINGER	96	SPEC	1.68 $pd \rightarrow {}^3\text{He}\eta'$
0.28 ± 0.10	1000	BINNIE	79	MMS	0 $\pi^- p \rightarrow n\text{MM}$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
0.20 ± 0.04		BAI	04J	BES2	$J/\psi \rightarrow \gamma\gamma\pi^+\pi^-$

## $\eta'(958)$ DECAY MODES

Mode	Fraction ( $\Gamma_i/\Gamma$ )	Confidence level
$\Gamma_1$ $\pi^+\pi^-\eta$	(42.6 $\pm$ 0.7) %	
$\Gamma_2$ $\rho^0\gamma$ (including non-resonant $\pi^+\pi^-\gamma$ )	(28.9 $\pm$ 0.5) %	
$\Gamma_3$ $\pi^0\pi^0\eta$	(22.8 $\pm$ 0.8) %	
$\Gamma_4$ $\omega\gamma$	( 2.62 $\pm$ 0.13) %	
$\Gamma_5$ $\omega e^+ e^-$	( 2.0 $\pm$ 0.4 ) $\times 10^{-4}$	
$\Gamma_6$ $\gamma\gamma$	( 2.22 $\pm$ 0.08) %	
$\Gamma_7$ $3\pi^0$	( 2.54 $\pm$ 0.18) $\times 10^{-3}$	
$\Gamma_8$ $\mu^+\mu^-\gamma$	( 1.09 $\pm$ 0.27) $\times 10^{-4}$	
$\Gamma_9$ $\pi^+\pi^-\mu^+\mu^-$	< 2.9 $\times 10^{-5}$	90%
$\Gamma_{10}$ $\pi^+\pi^-\pi^0$	( 3.61 $\pm$ 0.17) $\times 10^{-3}$	
$\Gamma_{11}$ $(\pi^+\pi^-\pi^0)$ S-wave	( 3.8 $\pm$ 0.5 ) $\times 10^{-3}$	
$\Gamma_{12}$ $\pi^\mp\rho^\pm$	( 7.4 $\pm$ 2.3 ) $\times 10^{-4}$	
$\Gamma_{13}$ $\pi^0\rho^0$	< 4 %	90%
$\Gamma_{14}$ $2(\pi^+\pi^-)$	( 8.6 $\pm$ 0.9 ) $\times 10^{-5}$	
$\Gamma_{15}$ $\pi^+\pi^-2\pi^0$	( 1.8 $\pm$ 0.4 ) $\times 10^{-4}$	
$\Gamma_{16}$ $2(\pi^+\pi^-)$ neutrals	< 1 %	95%
$\Gamma_{17}$ $2(\pi^+\pi^-)\pi^0$	< 1.8 $\times 10^{-3}$	90%
$\Gamma_{18}$ $2(\pi^+\pi^-)2\pi^0$	< 1 %	95%
$\Gamma_{19}$ $3(\pi^+\pi^-)$	< 3.1 $\times 10^{-5}$	90%
$\Gamma_{20}$ $K^\pm\pi^\mp$	< 4 $\times 10^{-5}$	90%
$\Gamma_{21}$ $\pi^+\pi^-e^+e^-$	( 2.4 $^{+1.3}_{-1.0}$ ) $\times 10^{-3}$	
$\Gamma_{22}$ $\pi^+e^-\nu_e + \text{c.c.}$	< 2.1 $\times 10^{-4}$	90%
$\Gamma_{23}$ $\gamma e^+e^-$	( 4.73 $\pm$ 0.30) $\times 10^{-4}$	
$\Gamma_{24}$ $\pi^0\gamma\gamma$	< 8 $\times 10^{-4}$	90%
$\Gamma_{25}$ $4\pi^0$	< 3.2 $\times 10^{-4}$	90%
$\Gamma_{26}$ $e^+e^-$	< 5.6 $\times 10^{-9}$	90%
$\Gamma_{27}$ invisible	< 5 $\times 10^{-4}$	90%

### Charge conjugation (C), Parity (P), Lepton family number (LF) violating modes

$\Gamma_{28}$ $\pi^+\pi^-$	$P, CP$	< 1.8 $\times 10^{-5}$	90%
$\Gamma_{29}$ $\pi^0\pi^0$	$P, CP$	< 5 $\times 10^{-4}$	90%
$\Gamma_{30}$ $\pi^0e^+e^-$	$C$ [a]	< 1.4 $\times 10^{-3}$	90%
$\Gamma_{31}$ $\eta e^+e^-$	$C$ [a]	< 2.4 $\times 10^{-3}$	90%
$\Gamma_{32}$ $3\gamma$	$C$	< 1.1 $\times 10^{-4}$	90%
$\Gamma_{33}$ $\mu^+\mu^-\pi^0$	$C$ [a]	< 6.0 $\times 10^{-5}$	90%
$\Gamma_{34}$ $\mu^+\mu^-\eta$	$C$ [a]	< 1.5 $\times 10^{-5}$	90%
$\Gamma_{35}$ $e\mu$	$LF$	< 4.7 $\times 10^{-4}$	90%

[a] C parity forbids this to occur as a single-photon process.

### CONSTRAINED FIT INFORMATION

An overall fit to the total width, a partial width, 2 combinations of partial widths obtained from integrated cross section, and 16 branching ratios uses 46 measurements and one constraint to determine 9 parameters. The overall fit has a  $\chi^2 = 62.7$  for 38 degrees of freedom.

The following *off-diagonal* array elements are the correlation coefficients  $\langle \delta p_i \delta p_j \rangle / (\delta p_i \cdot \delta p_j)$ , in percent, from the fit to parameters  $p_i$ , including the branching fractions,  $x_i \equiv \Gamma_i / \Gamma_{\text{total}}$ . The fit constrains the  $x_i$  whose labels appear in this array to sum to one.

$x_2$	-3							
$x_3$	-76	-58						
$x_4$	-10	-13	1					
$x_6$	-27	-24	29	-1				
$x_7$	-23	-18	28	0	8			
$x_{10}$	0	-1	-1	0	-1	0		
$x_{21}$	-5	-6	-5	-1	-3	-2	0	
$\Gamma$	24	4	-17	3	-71	-4	1	3
	$x_1$	$x_2$	$x_3$	$x_4$	$x_6$	$x_7$	$x_{10}$	$x_{21}$

	Mode	Rate (MeV)
$\Gamma_1$	$\pi^+ \pi^- \eta$	0.084 $\pm$ 0.004
$\Gamma_2$	$\rho^0 \gamma$ (including non-resonant $\pi^+ \pi^- \gamma$ )	0.0567 $\pm$ 0.0027
$\Gamma_3$	$\pi^0 \pi^0 \eta$	0.0448 $\pm$ 0.0023
$\Gamma_4$	$\omega \gamma$	0.00514 $\pm$ 0.00035
$\Gamma_6$	$\gamma \gamma$	0.00436 $\pm$ 0.00013
$\Gamma_7$	$3\pi^0$	(5.0 $\pm$ 0.4) $\times 10^{-4}$
$\Gamma_{10}$	$\pi^+ \pi^- \pi^0$	(7.1 $\pm$ 0.5) $\times 10^{-4}$
$\Gamma_{21}$	$\pi^+ \pi^- e^+ e^-$	(4.6 $^{+2.5}_{-1.9}$ ) $\times 10^{-4}$

### $\eta'(958)$ PARTIAL WIDTHS

$\Gamma(\gamma\gamma)$						$\Gamma_6$
VALUE (keV)	EVTS	DOCUMENT ID	TECN	COMMENT		
<b>4.36 <math>\pm</math> 0.14 OUR FIT</b>						
<b>4.28 <math>\pm</math> 0.19 OUR AVERAGE</b>						
4.17 $\pm$ 0.10 $\pm$ 0.27	2000	<sup>1</sup> ACCIARRI	98Q L3	$e^+ e^- \rightarrow e^+ e^- \pi^+ \pi^- \gamma$		
4.53 $\pm$ 0.29 $\pm$ 0.51	266	KARCH	92 CBAL	$e^+ e^- \rightarrow e^+ e^- \eta \pi^0 \pi^0$		
3.61 $\pm$ 0.13 $\pm$ 0.48		<sup>2</sup> BEHREND	91 CELL	$e^+ e^- \rightarrow e^+ e^- \eta'(958)$		

4.6 ±1.1 ±0.6	23	BARU	90	MD1	$e^+e^- \rightarrow e^+e^-\pi^+\pi^-\gamma$
4.57±0.25±0.44		BUTLER	90	MRK2	$e^+e^- \rightarrow e^+e^-\eta'(958)$
5.08±0.24±0.71	547	<sup>3</sup> ROE	90	ASP	$e^+e^- \rightarrow e^+e^-2\gamma$
3.8 ±0.7 ±0.6	34	AIHARA	88C	TPC	$e^+e^- \rightarrow e^+e^-\eta\pi^+\pi^-$
4.9 ±0.5 ±0.5	136	<sup>4</sup> WILLIAMS	88	CBAL	$e^+e^- \rightarrow e^+e^-2\gamma$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
4.7 ±0.6 ±0.9	143	<sup>5</sup> GIDAL	87	MRK2	$e^+e^- \rightarrow e^+e^-\eta\pi^+\pi^-$
4.0 ±0.9		<sup>6</sup> BARTEL	85E	JADE	$e^+e^- \rightarrow e^+e^-2\gamma$

<sup>1</sup> No non-resonant  $\pi^+\pi^-$  contribution found.

<sup>2</sup> Reevaluated by us using  $B(\eta' \rightarrow \rho(770)\gamma) = (30.2 \pm 1.3)\%$ .

<sup>3</sup> Reevaluated by us using  $B(\eta' \rightarrow \gamma\gamma) = (2.11 \pm 0.13)\%$ .

<sup>4</sup> Reevaluated by us using  $B(\eta' \rightarrow \gamma\gamma) = (2.11 \pm 0.13)\%$ .

<sup>5</sup> Superseded by BUTLER 90.

<sup>6</sup> Systematic error not evaluated.

## $\Gamma(e^+e^-)$

$\Gamma_{26}$

<u>VALUE (eV)</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>&lt;1.1 × 10<sup>-3</sup></b>	90	1,2 ACHASOV	15	SND 0.958 $e^+e^- \rightarrow \pi\pi\eta$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
<2.0 × 10 <sup>-3</sup>	90	<sup>2</sup> ACHASOV	15	SND 0.958 $e^+e^- \rightarrow \pi\pi\eta$
<2.4 × 10 <sup>-3</sup>	90	<sup>2</sup> AKHMETSHIN	15	CMD3 0.958 $e^+e^- \rightarrow \pi^+\pi^-\eta$

<sup>1</sup> Combining data of ACHASOV 15 and AKHMETSHIN 15.

<sup>2</sup> Using  $\eta$  and  $\eta'$  branching fractions from PDG 14.

## $\eta'(958) \Gamma(i)\Gamma(\gamma\gamma)/\Gamma(\text{total})$

This combination of a partial width with the partial width into  $\gamma\gamma$  and with the total width is obtained from the integrated cross section into channel(i) in the  $\gamma\gamma$  annihilation.

## $\Gamma(\gamma\gamma) \times \Gamma(\rho^0\gamma(\text{including non-resonant } \pi^+\pi^-\gamma))/\Gamma_{\text{total}}$

$\Gamma_6\Gamma_2/\Gamma$

<u>VALUE (keV)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>1.26±0.04 OUR FIT</b>				
<b>1.26±0.07 OUR AVERAGE</b>		Error includes scale factor of 1.2.		
1.09±0.04±0.13		BEHREND	91	CELL $e^+e^- \rightarrow e^+e^-\rho(770)^0\gamma$
1.35±0.09±0.21		AIHARA	87	TPC $e^+e^- \rightarrow e^+e^-\rho\gamma$
1.13±0.04±0.13	867	ALBRECHT	87B	ARG $e^+e^- \rightarrow e^+e^-\rho\gamma$
1.53±0.09±0.21		ALTHOFF	84E	TASS $e^+e^- \rightarrow e^+e^-\rho\gamma$
1.14±0.08±0.11	243	BERGER	84B	PLUT $e^+e^- \rightarrow e^+e^-\rho\gamma$
1.73±0.34±0.35	95	JENNI	83	MRK2 $e^+e^- \rightarrow e^+e^-\rho\gamma$
1.49±0.13±0.027	213	BARTEL	82B	JADE $e^+e^- \rightarrow e^+e^-\rho\gamma$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
1.85±0.31±0.24	43	BEHREND	82C	CELL $e^+e^- \rightarrow e^+e^-\rho\gamma$

$\Gamma(\gamma\gamma) \times \Gamma(\pi^0\pi^0\eta)/\Gamma_{\text{total}}$   $\Gamma_6\Gamma_3/\Gamma$

VALUE (keV)                      DOCUMENT ID      TECN      COMMENT

**1.00±0.05 OUR FIT**

**0.92±0.06±0.11**                      <sup>1</sup> KARCH              92      CBAL       $e^+e^- \rightarrow e^+e^-\eta\pi^0\pi^0$

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.95±0.05±0.08                      <sup>2</sup> KARCH              90      CBAL       $e^+e^- \rightarrow e^+e^-\eta\pi^0\pi^0$

1.00±0.08±0.10                      <sup>2,3</sup> ANTREASYAN 87      CBAL       $e^+e^- \rightarrow e^+e^-\eta\pi^0\pi^0$

<sup>1</sup> Reevaluated by us using  $B(\eta \rightarrow \gamma\gamma) = (39.21 \pm 0.34)\%$ . Supersedes ANTREASYAN 87 and KARCH 90.

<sup>2</sup> Superseded by KARCH 92.

<sup>3</sup> Using  $BR(\eta \rightarrow 2\gamma) = (38.9 \pm 0.5)\%$ .

$\eta'(958) \Gamma(i)\Gamma(e^+e^-)/\Gamma(\text{total})$

$\Gamma(\pi^+\pi^-\eta) \times \Gamma(e^+e^-)/\Gamma_{\text{total}}$   $\Gamma_1\Gamma_{26}/\Gamma$

VALUE ( $10^{-3}$  eV)      CL%      DOCUMENT ID      TECN      COMMENT

**<1.0**                      90              <sup>1</sup> AKHMETSHIN 15      CMD3       $0.958 e^+e^- \rightarrow \pi^+\pi^-\eta$

<sup>1</sup> AKHMETSHIN 15 reports  $[\Gamma(\eta'(958) \rightarrow \pi^+\pi^-\eta) \times \Gamma(\eta'(958) \rightarrow e^+e^-)/\Gamma_{\text{total}}] \times [B(\eta \rightarrow 2\gamma)] < 4.1 \times 10^{-4}$  eV which we divide by our best value  $B(\eta \rightarrow 2\gamma) = 39.41 \times 10^{-2}$ .

$\eta'(958)$  BRANCHING RATIOS

$\Gamma(\pi^+\pi^-\eta)/\Gamma_{\text{total}}$   $\Gamma_1/\Gamma$

VALUE                      EVTS                      DOCUMENT ID      TECN      COMMENT

**0.426±0.007 OUR FIT**

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.424±0.011±0.004      1.2k              <sup>1</sup> PEDLAR              09      CLEO       $J/\psi \rightarrow \gamma\eta'$

<sup>1</sup> Not independent of other  $\eta'$  branching fractions and ratios in PEDLAR 09.

$\Gamma(\pi^+\pi^-\eta(\text{charged decay}))/\Gamma_{\text{total}}$  **0.2810 $\Gamma_1/\Gamma$**

VALUE                      EVTS                      DOCUMENT ID      TECN      COMMENT

**0.1196±0.0019 OUR FIT**

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.123 ±0.014              107              RITTENBERG 69      HBC      1.7-2.7  $K^-p$

0.10 ±0.04                      10              LONDON              66      HBC      2.24  $K^-p \rightarrow \Lambda 2\pi^+ 2\pi^-\pi^0$

0.07 ±0.04                      7                      BADIER              65B      HBC      3  $K^-p$

$\Gamma(\pi^+\pi^-\eta(\text{neutral decay}))/\Gamma_{\text{total}}$  **0.7212 $\Gamma_1/\Gamma$**

VALUE                      EVTS                      DOCUMENT ID      TECN      COMMENT

**0.307±0.005 OUR FIT**

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.314±0.026                      281              RITTENBERG 69      HBC      1.7-2.7  $K^-p$

$\Gamma(\rho^0 \gamma (\text{including non-resonant } \pi^+ \pi^- \gamma))/\Gamma_{\text{total}}$   $\Gamma_2/\Gamma$

VALUE      EVTS      DOCUMENT ID      TECN      COMMENT

**0.289 ± 0.005 OUR FIT**

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.287 ± 0.007 ± 0.004	0.2k	<sup>1</sup> PEDLAR	09	CLEO	$J/\psi \rightarrow \gamma \eta'$
0.329 ± 0.033	298	RITTENBERG	69	HBC	1.7–2.7 $K^- p$
0.2 ± 0.1	20	LONDON	66	HBC	2.24 $K^- p \rightarrow \Lambda \pi^+ \pi^- \gamma$
0.34 ± 0.09	35	BADIER	65B	HBC	3 $K^- p$

<sup>1</sup> Not independent of other  $\eta'$  branching fractions and ratios in PEDLAR 09.

$\Gamma(\rho^0 \gamma (\text{including non-resonant } \pi^+ \pi^- \gamma))/\Gamma(\pi^+ \pi^- \eta)$   $\Gamma_2/\Gamma_1$

VALUE      DOCUMENT ID      TECN      COMMENT

**0.679 ± 0.017 OUR FIT**

**0.683 ± 0.020 OUR AVERAGE**

0.677 ± 0.024 ± 0.011	PEDLAR	09	CLE3	$J/\psi \rightarrow \eta' \gamma$
0.69 ± 0.03	ABLIKIM	06E	BES2	$J/\psi \rightarrow \eta' \gamma$

$\Gamma(\rho^0 \gamma (\text{including non-resonant } \pi^+ \pi^- \gamma))/\Gamma(\pi^+ \pi^- \eta (\text{neutral decay}))$   $\Gamma_2/0.714\Gamma_1$

VALUE      EVTS      DOCUMENT ID      TECN      COMMENT

**0.951 ± 0.024 OUR FIT**

**0.97 ± 0.09 OUR AVERAGE**

0.70 ± 0.22	AMSLER	04B	CBAR	0 $\bar{p} p \rightarrow \pi^+ \pi^- \eta$
1.07 ± 0.17	BELADIDZE	92C	VES	36 $\pi^- \text{Be} \rightarrow \pi^- \eta' \eta \text{Be}$
0.92 ± 0.14	DANBURG	73	HBC	2.2 $K^- p \rightarrow \Lambda X^0$
1.11 ± 0.18	JACOBS	73	HBC	2.9 $K^- p \rightarrow \Lambda X^0$

$\Gamma(\pi^0 \pi^0 \eta)/\Gamma_{\text{total}}$   $\Gamma_3/\Gamma$

VALUE      EVTS      DOCUMENT ID      TECN      COMMENT

**0.228 ± 0.008 OUR FIT**

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.235 ± 0.013 ± 0.004	3.2k	<sup>1</sup> PEDLAR	09	CLEO	$J/\psi \rightarrow \gamma \eta'$
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<sup>1</sup> Not independent of other  $\eta'$  branching fractions and ratios in PEDLAR 09.

$\Gamma(\pi^0 \pi^0 \eta (3\pi^0 \text{ decay}))/\Gamma_{\text{total}}$  **0.321\Gamma\_3/\Gamma**

VALUE      EVTS      DOCUMENT ID      TECN      COMMENT

**0.0733 ± 0.0026 OUR FIT**

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.11 ± 0.06	4	BENSINGER	70	DBC	2.2 $\pi^+ d$
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$\Gamma(\pi^0 \pi^0 \eta)/\Gamma(\pi^+ \pi^- \eta)$   $\Gamma_3/\Gamma_1$

VALUE      DOCUMENT ID      TECN      COMMENT

**0.536 ± 0.026 OUR FIT**

<b>0.555 ± 0.043 ± 0.013</b>	PEDLAR	09	CLE3	$J/\psi \rightarrow \eta' \gamma$
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$\Gamma(\rho^0\gamma(\text{including non-resonant } \pi^+\pi^-\gamma))/\Gamma(\pi\pi\eta)$   $\Gamma_2/(\Gamma_1+\Gamma_3)$

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>0.442±0.012 OUR FIT</b>			
<b>0.43 ±0.02 ±0.02</b>	BARBERIS	98C	OMEG 450 $p p \rightarrow p_f \eta' p_s$
• • • We do not use the following data for averages, fits, limits, etc. • • •			
0.31 ±0.15	DAVIS	68	HBC 5.5 $K^- p$

$\Gamma(\omega\gamma)/\Gamma_{\text{total}}$   $\Gamma_4/\Gamma$

<u>VALUE (units 10<sup>-2</sup>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>2.62±0.13 OUR FIT</b>				
<b>2.55±0.03±0.16</b>	33.2k	<sup>1</sup> ABLIKIM	15AD BES3	$J/\psi \rightarrow \eta'\gamma$
• • • We do not use the following data for averages, fits, limits, etc. • • •				
2.34±0.30±0.04	70	<sup>2</sup> PEDLAR	09 CLEO	$J/\psi \rightarrow \gamma\eta'$
<sup>1</sup> Using $B(J/\psi \rightarrow \eta'\gamma) = (5.15 \pm 0.16) \times 10^{-3}$ and $B(\omega \rightarrow \pi^+\pi^-\pi^0) = (89.2 \pm 0.7)\%$ .				
<sup>2</sup> Not independent of other $\eta'$ branching fractions and ratios in PEDLAR 09.				

$\Gamma(\omega\gamma)/\Gamma(\pi^+\pi^-\eta)$   $\Gamma_4/\Gamma_1$

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>0.0615±0.0033 OUR FIT</b>				
<b>0.055 ±0.007 ±0.001</b>		PEDLAR	09 CLE3	$J/\psi \rightarrow \eta'\gamma$
• • • We do not use the following data for averages, fits, limits, etc. • • •				
0.068 ±0.013	68	ZANFINO	77 ASPK	8.4 $\pi^- p$

$\Gamma(\omega\gamma)/\Gamma(\pi^0\pi^0\eta)$   $\Gamma_4/\Gamma_3$

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>0.115±0.007 OUR FIT</b>			
<b>0.147±0.016</b>	ALDE	87B GAM2	38 $\pi^- p \rightarrow n4\gamma$

$\Gamma(\omega e^+ e^-)/\Gamma(\omega\gamma)$   $\Gamma_5/\Gamma_4$

<u>VALUE (units 10<sup>-3</sup>)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
• • • We do not use the following data for averages, fits, limits, etc. • • •			
7.71±1.34±0.54	<sup>1</sup> ABLIKIM	15AD BES3	$J/\psi \rightarrow \eta'\gamma$
<sup>1</sup> Obtained from other ABLIKIM 15AD measurements with common systematics taken into account.			

$\Gamma(\omega e^+ e^-)/\Gamma_{\text{total}}$   $\Gamma_5/\Gamma$

<u>VALUE (units 10<sup>-4</sup>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>1.97±0.34±0.17</b>	66	<sup>1</sup> ABLIKIM	15AD BES3	$J/\psi \rightarrow \eta'\gamma$
<sup>1</sup> Using $B(J/\psi \rightarrow \eta'\gamma) = (5.15 \pm 0.16) \times 10^{-3}$ and $B(\omega \rightarrow \pi^+\pi^-\pi^0) = (89.2 \pm 0.7)\%$ .				

$\Gamma(\rho^0\gamma(\text{including non-resonant } \pi^+\pi^-\gamma))/[\Gamma(\pi^+\pi^-\eta) + \Gamma(\pi^0\pi^0\eta) + \Gamma(\omega\gamma)]$   $\Gamma_2/(\Gamma_1+\Gamma_3+\Gamma_4)$

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>0.425±0.011 OUR FIT</b>			
• • • We do not use the following data for averages, fits, limits, etc. • • •			
0.25 ±0.14	DAUBER	64	HBC 1.95 $K^- p$

$$\frac{[\Gamma(\pi^0\pi^0\eta(\text{charged decay})) + \Gamma(\omega(\text{charged decay})\gamma)]}{\Gamma_{\text{total}}} \quad (0.286\Gamma_3 + 0.89\Gamma_4)/\Gamma$$

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
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**0.0886 ± 0.0026 OUR FIT**

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.045 ± 0.029	42	RITTENBERG 69	HBC	1.7–2.7 $K^- p$
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$$\frac{\Gamma(\pi^+\pi^-\text{ neutrals})}{\Gamma_{\text{total}}} \quad (0.714\Gamma_1 + \Gamma_2 + 0.286\Gamma_3 + 0.89\Gamma_4)/\Gamma$$

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
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**0.3926 ± 0.0035 OUR FIT**

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.4 ± 0.1	39	LONDON 66	HBC	2.24 $K^- p \rightarrow \Lambda \pi^+ \pi^-$ neutrals
0.35 ± 0.06	33	BADIER 65B	HBC	3 $K^- p$

$$\frac{\Gamma(\gamma\gamma)}{\Gamma_{\text{total}}} \quad \Gamma_6/\Gamma$$

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
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**2.22 ± 0.08 OUR FIT**

**2.00 ± 0.15 OUR AVERAGE**

$1.98^{+0.31}_{-0.27} \pm 0.07$	114	<sup>1</sup> WICHT 08	BELL 08	$B^\pm \rightarrow K^\pm \gamma\gamma$
$2.00 \pm 0.18$		<sup>2</sup> STANTON 80	SPEC 80	$8.45 \pi^- p \rightarrow n \pi^+ \pi^- 2\gamma$

• • • We do not use the following data for averages, fits, limits, etc. • • •

$2.25 \pm 0.16 \pm 0.03$	0.3k	<sup>3</sup> PEDLAR 09	CLEO 09	$J/\psi \rightarrow \gamma \eta'$
$1.8 \pm 0.2$	6000	<sup>4</sup> APEL 79	NICE 79	$15\text{--}40 \pi^- p \rightarrow n 2\gamma$
$2.5 \pm 0.7$		DUANE 74	MMS 74	$\pi^- p \rightarrow n \text{MM}$
$1.71 \pm 0.33$	68	DALPIAZ 72	CNTR 72	$1.6 \pi^- p \rightarrow n X^0$
$2.0^{+0.8}_{-0.6}$	31	HARVEY 71	OSPK 71	$3.65 \pi^- p \rightarrow n X^0$

<sup>1</sup> WICHT 08 reports  $[\Gamma(\eta'(958) \rightarrow \gamma\gamma)/\Gamma_{\text{total}}] \times [B(B^+ \rightarrow \eta' K^+)] = (1.40^{+0.16+0.15}_{-0.15-0.12}) \times 10^{-6}$  which we divide by our best value  $B(B^+ \rightarrow \eta' K^+) = (7.06 \pm 0.25) \times 10^{-5}$ . Our first error is their experiment's error and our second error is the systematic error from using our best value.

<sup>2</sup> Includes APEL 79 result.

<sup>3</sup> Not independent of other  $\eta'$  branching fractions and ratios in PEDLAR 09.

<sup>4</sup> Data is included in STANTON 80 evaluation.

$$\frac{\Gamma(\gamma\gamma)}{\Gamma(\pi^+\pi^-\eta)} \quad \Gamma_6/\Gamma_1$$

VALUE	DOCUMENT ID	TECN	COMMENT
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**0.0522 ± 0.0022 OUR FIT**

<b>0.053 ± 0.004 ± 0.001</b>	PEDLAR 09	CLE3 09	$J/\psi \rightarrow \eta' \gamma$
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$$\frac{\Gamma(\gamma\gamma)}{\Gamma(\rho^0\gamma(\text{including non-resonant } \pi^+\pi^-\gamma))} \quad \Gamma_6/\Gamma_2$$

VALUE	DOCUMENT ID	TECN	COMMENT
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**0.0768 ± 0.0033 OUR FIT**

<b>0.080 ± 0.008</b>	ABLIKIM 06E	BES2 06E	$J/\psi \rightarrow \eta' \gamma$
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$\Gamma(\gamma\gamma)/\Gamma(\pi^0\pi^0\eta)$   $\Gamma_6/\Gamma_3$

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>0.097±0.004 OUR FIT</b>			
<b>0.105±0.010 OUR AVERAGE</b>	Error includes scale factor of 1.9.		
0.091±0.009	AMSLER	93	CBAR 0.0 $\bar{p}p$
0.112±0.002±0.006	ALDE	87B	GAM2 38 $\pi^- p \rightarrow n2\gamma$

$\Gamma(\gamma\gamma)/\Gamma(\pi^0\pi^0\eta(\text{neutral decay}))$   $\Gamma_6/0.714\Gamma_3$

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>0.136±0.006 OUR FIT</b>				
• • • We do not use the following data for averages, fits, limits, etc. • • •				
0.188±0.058	16	APEL	72	OSPK 3.8 $\pi^- p \rightarrow nX^0$

$\Gamma(\text{neutrals})/\Gamma_{\text{total}}$   $(0.714\Gamma_3+0.09\Gamma_4+\Gamma_6)/\Gamma$

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>0.188±0.006 OUR FIT</b>				
• • • We do not use the following data for averages, fits, limits, etc. • • •				
0.185±0.022	535	BASILE	71	CNTR 1.6 $\pi^- p \rightarrow nX^0$
0.189±0.026	123	RITTENBERG	69	HBC 1.7–2.7 $K^- p$

$\Gamma(3\pi^0)/\Gamma_{\text{total}}$   $\Gamma_7/\Gamma$

<u>VALUE (units 10<sup>-3</sup>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>2.54 ±0.18 OUR FIT</b>				
<b>3.57 ±0.26 OUR AVERAGE</b>				
3.522±0.082±0.254	2015	ABLIKIM	17	BES3 $J/\psi \rightarrow \gamma(3\pi^0)$
4.79 ±0.59 ±1.14	183	<sup>1</sup> ABLIKIM	15P	BES3 $J/\psi \rightarrow K^+ K^- 3\pi$
• • • We do not use the following data for averages, fits, limits, etc. • • •				
3.56 ±0.22 ±0.34	309	<sup>2</sup> ABLIKIM	12E	BES3 $J/\psi \rightarrow \gamma(3\pi^0)$
<sup>1</sup> We have added all systematic uncertainties in quadrature to a single value.				
<sup>2</sup> Superseded by ABLIKIM 17.				

$\Gamma(3\pi^0)/\Gamma(\pi^0\pi^0\eta)$   $\Gamma_7/\Gamma_3$

<u>VALUE (units 10<sup>-4</sup>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>111± 8 OUR FIT</b>				
<b>78±10 OUR AVERAGE</b>				
86±19	235	BLIK	08	GAMS 32 $\pi^- p \rightarrow \eta' n$
74±15		ALDE	87B	GAM2 38 $\pi^- p \rightarrow n6\gamma$
75±18		BINON	84	GAM2 30–40 $\pi^- p \rightarrow n6\gamma$

$\Gamma(\mu^+\mu^-\gamma)/\Gamma(\gamma\gamma)$   $\Gamma_8/\Gamma_6$

<u>VALUE (units 10<sup>-3</sup>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>4.9±1.2</b>	33	VIKTOROV	80	CNTR 25,33 $\pi^- p \rightarrow 2\mu\gamma$

$\Gamma(\pi^+\pi^-\mu^+\mu^-)/\Gamma_{\text{total}}$   $\Gamma_9/\Gamma$

<u>VALUE (units 10<sup>-4</sup>)</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
• • • We do not use the following data for averages, fits, limits, etc. • • •				
<0.29	90	<sup>1</sup> ABLIKIM	130	BES3 $J/\psi \rightarrow \gamma\eta'$
<2.4	90	<sup>2</sup> NAIK	09	CLEO $J/\psi \rightarrow \gamma\eta'$
<sup>1</sup> Using $\Gamma_2/\Gamma = (29.3 \pm 0.6)\%$ from PDG 12.				
<sup>2</sup> Not independent of measured value of $\Gamma_9/\Gamma_1$ from NAIK 09.				

$\Gamma(\pi^+\pi^-\mu^+\mu^-)/\Gamma(\pi^+\pi^-\eta)$   $\Gamma_9/\Gamma_1$

VALUE (units $10^{-3}$ )	CL%	DOCUMENT ID	TECN	COMMENT
<b>&lt;0.5</b>	90	<sup>1</sup> NAIK	09	CLEO $J/\psi \rightarrow \gamma\eta'$

<sup>1</sup> NAIK 09 reports  $[\Gamma(\eta'(958) \rightarrow \pi^+\pi^-\mu^+\mu^-)/\Gamma(\eta'(958) \rightarrow \pi^+\pi^-\eta)] / [B(\eta \rightarrow 2\gamma)] < 1.3 \times 10^{-3}$  which we multiply by our best value  $B(\eta \rightarrow 2\gamma) = 39.41 \times 10^{-2}$ .

$\Gamma(\pi^+\pi^-\mu^+\mu^-)/\Gamma(\rho^0\gamma(\text{including non-resonant } \pi^+\pi^-\gamma))$   $\Gamma_9/\Gamma_2$

VALUE (units $10^{-4}$ )	CL%	DOCUMENT ID	TECN	COMMENT
<b>&lt;1.0</b>	90	ABLIKIM	130	BES3 $J/\psi \rightarrow \gamma\eta'$

$\Gamma(\pi^+\pi^-\pi^0)/\Gamma_{\text{total}}$   $\Gamma_{10}/\Gamma$

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>3.61 ± 0.18 OUR FIT</b>				
<b>3.61 ± 0.18 OUR AVERAGE</b>				
3.591 ± 0.054 ± 0.174	6067	ABLIKIM	17	BES3 $J/\psi \rightarrow \gamma(\pi^+\pi^-\pi^0)$
4.28 ± 0.49 ± 1.11	78	<sup>1</sup> ABLIKIM	15P	BES3 $J/\psi \rightarrow K^+K^-3\pi$
3.7 $^{+1.1}_{-0.9}$ ± 0.4		<sup>2</sup> NAIK	09	CLEO $J/\psi \rightarrow \gamma\eta'$

• • • We do not use the following data for averages, fits, limits, etc. • • •

3.83 ± 0.15 ± 0.39	1014	<sup>3</sup> ABLIKIM	12E	BES3 $J/\psi \rightarrow \gamma(\pi^+\pi^-\pi^0)$
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<sup>1</sup> We have added all systematic uncertainties in quadrature to a single value.

<sup>2</sup> Not independent of measured value of  $\Gamma_{10}/\Gamma_1$  from NAIK 09.

<sup>3</sup> Superseded by ABLIKIM 17.

$\Gamma((\pi^+\pi^-\pi^0) \text{ S-wave})/\Gamma_{\text{total}}$   $\Gamma_{11}/\Gamma$

VALUE (units $10^{-4}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>37.63 ± 0.77 ± 5.00</b>	6580	<sup>1</sup> ABLIKIM	17	BES3 $J/\psi \rightarrow \gamma(\pi^+\pi^-\pi^0)$

<sup>1</sup> We have added all systematic uncertainties in quadrature .

$\Gamma(\pi^\mp\rho^\pm)/\Gamma_{\text{total}}$   $\Gamma_{12}/\Gamma$

VALUE (units $10^{-4}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>7.44 ± 0.60 ± 2.23</b>	1231	<sup>1</sup> ABLIKIM	17	BES3 $J/\psi \rightarrow \gamma(\pi^\mp\rho^\pm)$

<sup>1</sup> We have added all systematic uncertainties in quadrature .

$\Gamma(\pi^+\pi^-\pi^0)/\Gamma(\pi^+\pi^-\eta)$   $\Gamma_{10}/\Gamma_1$

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>8.5 ± 0.4 OUR FIT</b>				
<b>8.28 <math>^{+2.49}_{-2.12}</math> ± 0.04</b>	20	<sup>1</sup> NAIK	09	CLEO $J/\psi \rightarrow \gamma\eta'$

<sup>1</sup> NAIK 09 reports  $[\Gamma(\eta'(958) \rightarrow \pi^+\pi^-\pi^0)/\Gamma(\eta'(958) \rightarrow \pi^+\pi^-\eta)] / [B(\eta \rightarrow 2\gamma)] = (21^{+6}_{-5} \pm 2) \times 10^{-3}$  which we multiply by our best value  $B(\eta \rightarrow 2\gamma) = (39.41 \pm 0.20) \times 10^{-2}$ . Our first error is their experiment's error and our second error is the systematic error from using our best value.

$\Gamma(\pi^0\rho^0)/\Gamma_{\text{total}}$   $\Gamma_{13}/\Gamma$

VALUE	CL%	DOCUMENT ID	TECN	COMMENT
<b>&lt;0.04</b>	90	RITTENBERG	65	HBC $2.7 K^-p$

$\Gamma(2(\pi^+\pi^-))/\Gamma_{\text{total}}$   $\Gamma_{14}/\Gamma$

VALUE (units $10^{-5}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
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**$8.6 \pm 0.9 \pm 0.3$**       199      <sup>1</sup> ABLIKIM      14M      BES3       $J/\psi \rightarrow \gamma\eta'$

• • • We do not use the following data for averages, fits, limits, etc. • • •

< 24      90      <sup>2</sup> NAIK      09      CLEO       $J/\psi \rightarrow \gamma\eta'$   
 <1000      90      RITTENBERG      69      HBC      1.7–2.7  $K^-p$

<sup>1</sup> ABLIKIM 14M reports  $[\Gamma(\eta'(958) \rightarrow 2(\pi^+\pi^-))/\Gamma_{\text{total}}] \times [B(J/\psi(1S) \rightarrow \gamma\eta'(958))]$   
 =  $(4.40 \pm 0.35 \pm 0.30) \times 10^{-7}$  which we divide by our best value  $B(J/\psi(1S) \rightarrow \gamma\eta'(958)) = (5.13 \pm 0.17) \times 10^{-3}$ . Our first error is their experiment's error and our second error is the systematic error from using our best value.

<sup>2</sup> Not independent of measured value of  $\Gamma_{14}/\Gamma_1$  from NAIK 09.

$\Gamma(2(\pi^+\pi^-))/\Gamma(\pi^+\pi^-\eta)$   $\Gamma_{14}/\Gamma_1$

VALUE (units $10^{-3}$ )	CL%	DOCUMENT ID	TECN	COMMENT
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**<0.6**      90      <sup>1</sup> NAIK      09      CLEO       $J/\psi \rightarrow \gamma\eta'$

<sup>1</sup> NAIK 09 reports  $[\Gamma(\eta'(958) \rightarrow 2(\pi^+\pi^-))/\Gamma(\eta'(958) \rightarrow \pi^+\pi^-\eta)] / [B(\eta \rightarrow 2\gamma)]$   
 <  $1.4 \times 10^{-3}$  which we multiply by our best value  $B(\eta \rightarrow 2\gamma) = 39.41 \times 10^{-2}$ .

$\Gamma(\pi^+\pi^-2\pi^0)/\Gamma_{\text{total}}$   $\Gamma_{15}/\Gamma$

VALUE (units $10^{-4}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
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**$1.8 \pm 0.4 \pm 0.1$**       84      <sup>1</sup> ABLIKIM      14M      BES3       $J/\psi \rightarrow \gamma\eta'$

• • • We do not use the following data for averages, fits, limits, etc. • • •

<27      90      <sup>2</sup> NAIK      09      CLEO       $J/\psi \rightarrow \gamma\eta'$

<sup>1</sup> ABLIKIM 14M reports  $[\Gamma(\eta'(958) \rightarrow \pi^+\pi^-2\pi^0)/\Gamma_{\text{total}}] \times [B(J/\psi(1S) \rightarrow \gamma\eta'(958))]$   
 =  $(9.38 \pm 1.79 \pm 0.89) \times 10^{-7}$  which we divide by our best value  $B(J/\psi(1S) \rightarrow \gamma\eta'(958))$   
 =  $(5.13 \pm 0.17) \times 10^{-3}$ . Our first error is their experiment's error and our second error is the systematic error from using our best value.

<sup>2</sup> Not independent of measured value of  $\Gamma_{15}/\Gamma_1$  from NAIK 09.

$\Gamma(\pi^+\pi^-2\pi^0)/\Gamma(\pi^+\pi^-\eta)$   $\Gamma_{15}/\Gamma_1$

VALUE (units $10^{-3}$ )	CL%	DOCUMENT ID	TECN	COMMENT
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**<6**      90      <sup>1</sup> NAIK      09      CLEO       $J/\psi \rightarrow \gamma\eta'$

<sup>1</sup> NAIK 09 reports  $[\Gamma(\eta'(958) \rightarrow \pi^+\pi^-2\pi^0)/\Gamma(\eta'(958) \rightarrow \pi^+\pi^-\eta)] / [B(\eta \rightarrow 2\gamma)]$   
 <  $15 \times 10^{-3}$  which we multiply by our best value  $B(\eta \rightarrow 2\gamma) = 39.41 \times 10^{-2}$ .

$\Gamma(2(\pi^+\pi^- \text{ neutrals}))/\Gamma_{\text{total}}$   $\Gamma_{16}/\Gamma$

VALUE	CL%	DOCUMENT ID	TECN	COMMENT
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**<0.01**      95      DANBURG      73      HBC       $2.2 K^-p \rightarrow \Lambda X^0$

• • • We do not use the following data for averages, fits, limits, etc. • • •

<0.01      90      RITTENBERG      69      HBC      1.7–2.7  $K^-p$

$\Gamma(2(\pi^+\pi^-\pi^0))/\Gamma_{\text{total}}$   $\Gamma_{17}/\Gamma$

VALUE	CL%	DOCUMENT ID	TECN	COMMENT
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• • • We do not use the following data for averages, fits, limits, etc. • • •

<0.002      90      <sup>1</sup> NAIK      09      CLEO       $J/\psi \rightarrow \gamma\eta'$

<0.01      90      RITTENBERG      69      HBC      1.7–2.7  $K^-p$

<sup>1</sup> Not independent of measured value of  $\Gamma_{17}/\Gamma_1$  from NAIK 09.

$\Gamma(2(\pi^+\pi^-)\pi^0)/\Gamma(\pi^+\pi^-\eta)$   $\Gamma_{17}/\Gamma_1$

VALUE (units $10^{-3}$ )	CL%	DOCUMENT ID	TECN	COMMENT
<b>&lt;4</b>	90	<sup>1</sup> NAIK	09	CLEO $J/\psi \rightarrow \gamma\eta'$
<sup>1</sup> NAIK 09 reports $[\Gamma(\eta'(958) \rightarrow 2(\pi^+\pi^-)\pi^0)/\Gamma(\eta'(958) \rightarrow \pi^+\pi^-\eta)] / [B(\eta \rightarrow 2\gamma)] < 11 \times 10^{-3}$ which we multiply by our best value $B(\eta \rightarrow 2\gamma) = 39.41 \times 10^{-2}$ .				

$\Gamma(2(\pi^+\pi^-)2\pi^0)/\Gamma_{\text{total}}$   $\Gamma_{18}/\Gamma$

VALUE	CL%	DOCUMENT ID	TECN	COMMENT
<b>&lt;0.01</b>	95	KALBFLEISCH 64B	HBC	$K^-p \rightarrow \Lambda 2(\pi^+\pi^-)+MM$
••• We do not use the following data for averages, fits, limits, etc. •••				
<0.01	90	LONDON	66	HBC Compilation

$\Gamma(3(\pi^+\pi^-))/\Gamma_{\text{total}}$   $\Gamma_{19}/\Gamma$

VALUE (units $10^{-5}$ )	CL%	DOCUMENT ID	TECN	COMMENT
<b>&lt; 3.1</b>	90	<sup>1</sup> ABLIKIM	13U	BES3 $J/\psi \rightarrow \gamma 3(\pi^+\pi^-)$
••• We do not use the following data for averages, fits, limits, etc. •••				
< 53	90	<sup>2</sup> NAIK	09	CLEO $J/\psi \rightarrow \gamma\eta'$
<500	95	KALBFLEISCH 64B	HBC	$K^-p \rightarrow \Lambda 2(\pi^+\pi^-)$
<sup>1</sup> Using $B(J/\psi \rightarrow \gamma\eta'(958)) = (5.16 \pm 0.15) \times 10^{-3}$ .				
<sup>2</sup> Not independent of measured value of $\Gamma_{19}/\Gamma_1$ from NAIK 09.				

$\Gamma(3(\pi^+\pi^-))/\Gamma(\pi^+\pi^-\eta)$   $\Gamma_{19}/\Gamma_1$

VALUE (units $10^{-3}$ )	CL%	DOCUMENT ID	TECN	COMMENT
<b>&lt;1.2</b>	90	<sup>1</sup> NAIK	09	CLEO $J/\psi \rightarrow \gamma\eta'$
<sup>1</sup> NAIK 09 reports $[\Gamma(\eta'(958) \rightarrow 3(\pi^+\pi^-))/\Gamma(\eta'(958) \rightarrow \pi^+\pi^-\eta)] / [B(\eta \rightarrow 2\gamma)] < 3.0 \times 10^{-3}$ which we multiply by our best value $B(\eta \rightarrow 2\gamma) = 39.41 \times 10^{-2}$ .				

$\Gamma(K^\pm\pi^\mp)/\Gamma(\rho^0\gamma(\text{including non-resonant } \pi^+\pi^-\gamma))$   $\Gamma_{20}/\Gamma_2$

VALUE	CL%	DOCUMENT ID	TECN	COMMENT
<b>&lt;1.3 <math>\times 10^{-4}</math></b>	90	ABLIKIM	16M	BES3 $e^+e^- \rightarrow J/\psi \rightarrow \text{hadrons}$

$\Gamma(\pi^+\pi^-e^+e^-)/\Gamma_{\text{total}}$   $\Gamma_{21}/\Gamma$

VALUE (units $10^{-3}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<b>2.4 <math>^{+1.3}_{-1.0}</math></b>					<b>OUR FIT</b>

••• We do not use the following data for averages, fits, limits, etc. •••

$2.11 \pm 0.12 \pm 0.14$	429	<sup>1</sup> ABLIKIM	130	BES3	$J/\psi \rightarrow \gamma\eta'$
$2.5 ^{+1.2}_{-0.9} \pm 0.5$		<sup>2</sup> NAIK	09	CLEO	$J/\psi \rightarrow \gamma\eta'$
<6	90	RITTENBERG	65	HBC	2.7 $K^-p$
<sup>1</sup> Using $\Gamma_2/\Gamma = (29.3 \pm 0.6)\%$ from PDG 12.					
<sup>2</sup> Not independent of measured value of $\Gamma_{21}/\Gamma_1$ from NAIK 09.					

$\Gamma(\pi^+\pi^-\rho^0)/\Gamma(\pi^+\pi^-\eta)$   $\Gamma_{21}/\Gamma_1$

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
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**5.5  $^{+3.0}_{-2.2}$  OUR FIT**

<b>5.5 <math>^{+3.00}_{-2.30} \pm 0.03</math></b>	8	<sup>1</sup> NAIK	09	CLEO $J/\psi \rightarrow \gamma\eta'$
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<sup>1</sup> NAIK 09 reports  $[\Gamma(\eta'(958) \rightarrow \pi^+\pi^-e^+e^-)/\Gamma(\eta'(958) \rightarrow \pi^+\pi^-\eta)] / [B(\eta \rightarrow 2\gamma)] = (14^{+7}_{-5} \pm 3) \times 10^{-3}$  which we multiply by our best value  $B(\eta \rightarrow 2\gamma) = (39.41 \pm 0.20) \times 10^{-2}$ . Our first error is their experiment's error and our second error is the systematic error from using our best value.

$\Gamma(\pi^+\pi^-\rho^0)/\Gamma(\rho^0\gamma(\text{including non-resonant } \pi^+\pi^-\gamma))$   $\Gamma_{21}/\Gamma_2$

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
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<b>7.2 <math>\pm 0.4 \pm 0.5</math></b>	429	ABLIKIM	130	BES3 $J/\psi \rightarrow \gamma\eta'$
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$\Gamma(\pi^+e^-\nu_e + \text{c.c.})/\Gamma(\pi^+\pi^-\eta)$   $\Gamma_{22}/\Gamma_1$

VALUE (units $10^{-4}$ )	CL%	DOCUMENT ID	TECN	COMMENT
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<b>&lt;5.0</b>	90	ABLIKIM	13G	BES3 $J/\psi \rightarrow \phi\eta'$
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$\Gamma(\gamma e^+e^-)/\Gamma_{\text{total}}$   $\Gamma_{23}/\Gamma$

VALUE (units $10^{-3}$ )	CL%	DOCUMENT ID	TECN	COMMENT
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• • • We do not use the following data for averages, fits, limits, etc. • • •

<0.9	90	BRIERE	00	CLEO $10.6 e^+e^-$
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$\Gamma(\gamma e^+e^-)/\Gamma(\gamma\gamma)$   $\Gamma_{23}/\Gamma_6$

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
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<b>2.13 <math>\pm 0.09 \pm 0.07</math></b>	864	ABLIKIM	150	BES3 $J/\psi \rightarrow \gamma e^+e^-$
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$\Gamma(\pi^0\gamma\gamma)/\Gamma(\pi^0\pi^0\eta)$   $\Gamma_{24}/\Gamma_3$

VALUE (units $10^{-4}$ )	CL%	DOCUMENT ID	TECN	COMMENT
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<b>&lt;37</b>	90	ALDE	87B	GAM2 $38 \pi^- p \rightarrow n4\gamma$
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$\Gamma(4\pi^0)/\Gamma_{\text{total}}$   $\Gamma_{25}/\Gamma$

VALUE	CL%	DOCUMENT ID	TECN	COMMENT
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<b>&lt;3.2 <math>\times 10^{-4}</math></b>	90	DONSKOV	14	GAM4 $32.5 \pi^- p \rightarrow \eta' n$
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$\Gamma(4\pi^0)/\Gamma(\pi^0\pi^0\eta)$   $\Gamma_{25}/\Gamma_3$

VALUE (units $10^{-4}$ )	CL%	DOCUMENT ID	TECN	COMMENT
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• • • We do not use the following data for averages, fits, limits, etc. • • •

<23	90	ALDE	87B	GAM2 $38 \pi^- p \rightarrow n8\gamma$
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$\Gamma(e^+e^-)/\Gamma_{\text{total}}$   $\Gamma_{26}/\Gamma$

VALUE	CL%	DOCUMENT ID	TECN	COMMENT
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<b>&lt; 5.6 <math>\times 10^{-9}</math></b>	90	<sup>1</sup> ACHASOV	15	SND $0.958 e^+e^- \rightarrow \pi\pi\eta$
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• • • We do not use the following data for averages, fits, limits, etc. • • •

<12 $\times 10^{-9}$	90	<sup>2</sup> AKHMETSHIN	15	CMD3 $0.958 e^+e^- \rightarrow \pi^+\pi^-\eta$
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< 2.1 $\times 10^{-7}$	90	VOROBYEV	88	ND $e^+e^- \rightarrow \pi^+\pi^-\eta$
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<sup>1</sup> Combining data of ACHASOV 15 and AKHMETSHIN 15 and using  $\Gamma(\eta') = 0.198 \pm 0.009$  MeV.

<sup>2</sup> Using  $\Gamma_{\eta'(958)} = 198 \pm 9$  keV,  $B(\eta'(958) \rightarrow \pi^+ \pi^- \eta) = (42.9 \pm 0.7)\%$ , and  $B(\eta \rightarrow \gamma\gamma) = (39.41 \pm 0.20)\%$ .

### $\Gamma(\text{invisible})/\Gamma_{\text{total}}$ $\Gamma_{27}/\Gamma$

VALUE (units $10^{-4}$ )	CL%	DOCUMENT ID	TECN	COMMENT
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• • • We do not use the following data for averages, fits, limits, etc. • • •

<9.5	90	<sup>1</sup> NAIK	09	CLEO $J/\psi \rightarrow \gamma\eta'$
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<sup>1</sup> Not independent of measured value of  $\Gamma_{27}/\Gamma_1$  from NAIK 09.

### $\Gamma(\text{invisible})/\Gamma(\gamma\gamma)$ $\Gamma_{27}/\Gamma_6$

VALUE (units $10^{-2}$ )	CL%	DOCUMENT ID	TECN	COMMENT
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<b>&lt;2.4</b>	90	ABLIKIM	13	BES3 $J/\psi \rightarrow \phi\eta'$
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• • • We do not use the following data for averages, fits, limits, etc. • • •

<6.69	90	ABLIKIM	06Q	BES $J/\psi \rightarrow \phi\eta'$
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### $\Gamma(\text{invisible})/\Gamma(\pi^+ \pi^- \eta)$ $\Gamma_{27}/\Gamma_1$

VALUE (units $10^{-3}$ )	CL%	DOCUMENT ID	TECN	COMMENT
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• • • We do not use the following data for averages, fits, limits, etc. • • •

<2.1	90	<sup>1</sup> NAIK	09	CLEO $J/\psi \rightarrow \gamma\eta'$
------	----	-------------------	----	---------------------------------------

<sup>1</sup> NAIK 09 reports  $[\Gamma(\eta'(958) \rightarrow \text{invisible})/\Gamma(\eta'(958) \rightarrow \pi^+ \pi^- \eta)] / [B(\eta \rightarrow 2\gamma)] < 5.4 \times 10^{-3}$  which we multiply by our best value  $B(\eta \rightarrow 2\gamma) = 39.41 \times 10^{-2}$ .

### $\Gamma(\pi^+ \pi^-)/\Gamma_{\text{total}}$ $\Gamma_{28}/\Gamma$

VALUE (units $10^{-4}$ )	CL%	DOCUMENT ID	TECN	COMMENT
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<b>&lt; 0.18</b>	90	<sup>1</sup> AAIJ	17D	LHCB $D_{(s)}^+ \rightarrow \pi^+ \pi^- \pi^+$
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• • • We do not use the following data for averages, fits, limits, etc. • • •

< 0.6	90	<sup>2</sup> ABLIKIM	11G	BES3 $J/\psi \rightarrow \gamma\pi^+ \pi^-$
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< 29	90	<sup>3</sup> MORI	07A	BELL $\gamma\gamma \rightarrow \pi^+ \pi^-$
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< 3.3	90	<sup>4</sup> MORI	07A	BELL $\gamma\gamma \rightarrow \pi^+ \pi^-$
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<800	95	DANBURG	73	HBC $2.2 K^- p \rightarrow \Lambda X^0$
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<200	90	RITTENBERG	69	HBC $1.7\text{--}2.7 K^- p$
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<sup>1</sup> Using branching fractions of  $D_{(s)}^+$  decays from PDG 15.

<sup>2</sup> ABLIKIM 11G reports  $[\Gamma(\eta'(958) \rightarrow \pi^+ \pi^-)/\Gamma_{\text{total}}] \times [B(J/\psi(1S) \rightarrow \gamma\eta'(958))] < 2.84 \times 10^{-7}$  which we divide by our best value  $B(J/\psi(1S) \rightarrow \gamma\eta'(958)) = 5.13 \times 10^{-3}$ .

<sup>3</sup> Taking into account interference with the  $\gamma\gamma \rightarrow \pi^+ \pi^-$  continuum.

<sup>4</sup> Without interference with the  $\gamma\gamma \rightarrow \pi^+ \pi^-$  continuum.

### $\Gamma(\pi^0 \pi^0)/\Gamma_{\text{total}}$ $\Gamma_{29}/\Gamma$

VALUE	CL%	DOCUMENT ID	TECN	COMMENT
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<b>&lt; <math>5 \times 10^{-4}</math></b>	90	<sup>1</sup> ABLIKIM	11G	BES3 $J/\psi \rightarrow \gamma\pi^0 \pi^0$
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<sup>1</sup> ABLIKIM 11G reports  $[\Gamma(\eta'(958) \rightarrow \pi^+ \pi^-)/\Gamma_{\text{total}}] \times [B(J/\psi(1S) \rightarrow \gamma\eta'(958))] < 2.84 \times 10^{-7}$  which we divide by our best value  $B(J/\psi(1S) \rightarrow \gamma\eta'(958)) = 5.13 \times 10^{-3}$ .

$\Gamma(\pi^0\pi^0)/\Gamma(\pi^0\pi^0\eta)$					$\Gamma_{29}/\Gamma_3$
<u>VALUE (units <math>10^{-4}</math>)</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>	
<b>&lt;45</b>	90	ALDE	87B	GAM2	$38 \pi^- p \rightarrow n4\gamma$
$\Gamma(\pi^0 e^+ e^-)/\Gamma_{\text{total}}$					$\Gamma_{30}/\Gamma$
<u>VALUE (units <math>10^{-3}</math>)</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>	
<b>&lt; 1.4</b>	90	BRIERE	00	CLEO	$10.6 e^+ e^-$
• • • We do not use the following data for averages, fits, limits, etc. • • •					
<13	90	RITTENBERG	65	HBC	$2.7 K^- p$
$\Gamma(\eta e^+ e^-)/\Gamma_{\text{total}}$					$\Gamma_{31}/\Gamma$
<u>VALUE (units <math>10^{-3}</math>)</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>	
<b>&lt; 2.4</b>	90	BRIERE	00	CLEO	$10.6 e^+ e^-$
• • • We do not use the following data for averages, fits, limits, etc. • • •					
<11	90	RITTENBERG	65	HBC	$2.7 K^- p$
$\Gamma(3\gamma)/\Gamma(\pi^0\pi^0\eta)$					$\Gamma_{32}/\Gamma_3$
<u>VALUE (units <math>10^{-4}</math>)</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>	
<b>&lt;4.6</b>	90	ALDE	87B	GAM2	$38 \pi^- p \rightarrow n3\gamma$
$\Gamma(\mu^+ \mu^- \pi^0)/\Gamma_{\text{total}}$					$\Gamma_{33}/\Gamma$
<u>VALUE (units <math>10^{-5}</math>)</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>	
<b>&lt;6.0</b>	90	DZHELYADIN	81	CNTR	$30 \pi^- p \rightarrow \eta' n$
$\Gamma(\mu^+ \mu^- \eta)/\Gamma_{\text{total}}$					$\Gamma_{34}/\Gamma$
<u>VALUE (units <math>10^{-5}</math>)</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>	
<b>&lt;1.5</b>	90	DZHELYADIN	81	CNTR	$30 \pi^- p \rightarrow \eta' n$
$\Gamma(e\mu)/\Gamma_{\text{total}}$					$\Gamma_{35}/\Gamma$
<u>VALUE (units <math>10^{-4}</math>)</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>	
<b>&lt;4.7</b>	90	BRIERE	00	CLEO	$10.6 e^+ e^-$

### $\eta'(958) \rightarrow \eta\pi\pi$ DECAY PARAMETERS

$$|\text{MATRIX ELEMENT}|^2 = |1 + \alpha Y|^2 + CX + DX^2$$

$X$  and  $Y$  are Dalitz variables;  $\alpha$  is complex and  $C$ , and  $D$  are real-valued. Parameters  $C$  and  $D$  are not necessarily equal to  $c$  and  $d$ , respectively, in the generalized parameterization following this one. May be different for  $\eta'(958) \rightarrow \eta\pi^+\pi^-$  and  $\eta'(958) \rightarrow \eta\pi^0\pi^0$  decays. Because of different initial assumptions and strong correlations of the parameters we do not average the parameters in the section below.

**Re( $\alpha$ ) decay parameter**

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
$-0.033 \pm 0.005 \pm 0.003$	44k	<sup>1</sup> ABLIKIM 11	BES3	$J/\psi \rightarrow \gamma \eta \pi^+ \pi^-$
$-0.072 \pm 0.012 \pm 0.006$	7k	<sup>2</sup> AMELIN 05A	VES	$28 \pi^- A \rightarrow \eta \pi^+ \pi^- \pi^- A^*$
$-0.021 \pm 0.018 \pm 0.017$	6.7k	<sup>3</sup> BRIERE 00	CLEO	$10.6 e^+ e^- \rightarrow \eta \pi^+ \pi^- X$
$-0.058 \pm 0.013 \pm 0.003$	5.4k	<sup>4</sup> ALDE 86	GAM2	$38 \pi^- p \rightarrow n \eta \pi^0 \pi^0$
$-0.08 \pm 0.03$		<sup>4,5</sup> KALBFLEISCH 74	RVUE	$\eta' \rightarrow \eta \pi^+ \pi^-$

<sup>1</sup> See ABLIKIM 11 for the full correlation matrix.<sup>2</sup> Superseded by DOROFEEV 07, which found this parameterization unacceptable. See below.<sup>3</sup> Assuming  $\text{Im}(\alpha) = 0$ ,  $C = 0$ , and  $D = 0$ .<sup>4</sup> Assuming  $C = 0$ .<sup>5</sup> From the data of DAUBER 64, RITTENBERG 69, AGUILAR-BENITEZ 72B, JACOBS 73, and DANBURG 73.**Im( $\alpha$ ) decay parameter**

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
$0.000 \pm 0.049 \pm 0.001$	44k	<sup>1</sup> ABLIKIM 11	BES3	$J/\psi \rightarrow \gamma \eta \pi^+ \pi^-$
$0.0 \pm 0.1 \pm 0.0$	7k	<sup>2</sup> AMELIN 05A	VES	$28 \pi^- A \rightarrow \eta \pi^+ \pi^- \pi^- A^*$
$-0.00 \pm 0.13 \pm 0.00$	5.4k	<sup>3</sup> ALDE 86	GAM2	$38 \pi^- p \rightarrow n \eta \pi^0 \pi^0$
$0.0 \pm 0.3$		<sup>3,4</sup> KALBFLEISCH 74	RVUE	$\eta' \rightarrow \eta \pi^+ \pi^-$

<sup>1</sup> See ABLIKIM 11 for the full correlation matrix.<sup>2</sup> Superseded by DOROFEEV 07, which found this parameterization unacceptable. See below.<sup>3</sup> Assuming  $C = 0$ .<sup>4</sup> From the data of DAUBER 64, RITTENBERG 69, AGUILAR-BENITEZ 72B, JACOBS 73, and DANBURG 73.**C decay parameter**

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
$+0.018 \pm 0.009 \pm 0.003$	44k	<sup>1</sup> ABLIKIM 11	BES3	$J/\psi \rightarrow \gamma \eta \pi^+ \pi^-$
$0.020 \pm 0.018 \pm 0.004$	7k	<sup>2</sup> AMELIN 05A	VES	$28 \pi^- A \rightarrow \eta \pi^+ \pi^- \pi^- A^*$

<sup>1</sup> See ABLIKIM 11 for the full correlation matrix.<sup>2</sup> Superseded by DOROFEEV 07, which found this parameterization unacceptable. See below.**D decay parameter**

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
$-0.059 \pm 0.012 \pm 0.004$	44k	<sup>1</sup> ABLIKIM 11	BES3	$J/\psi \rightarrow \gamma \eta \pi^+ \pi^-$
$-0.066 \pm 0.030 \pm 0.015$	7k	<sup>2</sup> AMELIN 05A	VES	$28 \pi^- A \rightarrow \eta \pi^+ \pi^- \pi^- A^*$
$0.00 \pm 0.03 \pm 0.00$	5.4k	<sup>3</sup> ALDE 86	GAM2	$38 \pi^- p \rightarrow n \eta \pi^0 \pi^0$
0		<sup>3,4</sup> KALBFLEISCH 74	RVUE	$\eta' \rightarrow \eta \pi^+ \pi^-$



<sup>1</sup> See ABLIKIM 11 for the full correlation matrix.

<sup>2</sup> Superseded by DOROFEEV 07, which found this parameterization unacceptable. See below.

<sup>3</sup> Assuming  $C = 0$ .

<sup>4</sup> From the data of DAUBER 64, RITTENBERG 69, AGUILAR-BENITEZ 72B, JACOBS 73, and DANBURG 73.

## $\eta'(958) \rightarrow \eta\pi\pi$ DECAY PARAMETERS

$$|\text{MATRIX ELEMENT}|^2 \propto 1 + a Y + b Y^2 + c X + d X^2$$

$X$  and  $Y$  are Dalitz variables and  $a$ ,  $b$ ,  $c$ , and  $d$  are real-valued parameters. May be different for  $\eta'(958) \rightarrow \eta\pi^+\pi^-$  and  $\eta'(958) \rightarrow \eta\pi^0\pi^0$  decays. We do not average measurements in the section below because parameter values from each experiment are strongly correlated.

### **a** decay parameter

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
$-0.047 \pm 0.011 \pm 0.003$	44k	<sup>1</sup> ABLIKIM 11	BES3	$J/\psi \rightarrow \gamma\eta\pi^+\pi^-$
$-0.066 \pm 0.016 \pm 0.003$	15k	<sup>2</sup> BLIK 09	GAM4	$32.5 \pi^- p \rightarrow \eta' n$
$-0.127 \pm 0.016 \pm 0.008$	20k	<sup>3</sup> DOROFEEV 07	VES	$27 \pi^- p \rightarrow \eta' n,$ $\pi^- A \rightarrow \eta' \pi^- A^*$

<sup>1</sup> See ABLIKIM 11 for the full correlation matrix.

<sup>2</sup> From  $\eta' \rightarrow \eta\pi^0\pi^0$  decay.

<sup>3</sup> From  $\eta' \rightarrow \eta\pi^+\pi^-$  decay.

### **b** decay parameter

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
$-0.069 \pm 0.019 \pm 0.009$	44k	<sup>1</sup> ABLIKIM 11	BES3	$J/\psi \rightarrow \gamma\eta\pi^+\pi^-$
$-0.063 \pm 0.028 \pm 0.004$	15k	<sup>2</sup> BLIK 09	GAM4	$32.5 \pi^- p \rightarrow \eta' n$
$-0.106 \pm 0.028 \pm 0.014$	20k	<sup>3</sup> DOROFEEV 07	VES	$27 \pi^- p \rightarrow \eta' n,$ $\pi^- A \rightarrow \eta' \pi^- A^*$

<sup>1</sup> See ABLIKIM 11 for the full correlation matrix.

<sup>2</sup> From  $\eta' \rightarrow \eta\pi^0\pi^0$  decay.

<sup>3</sup> From  $\eta' \rightarrow \eta\pi^+\pi^-$  decay.

### **c** decay parameter

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
$+0.019 \pm 0.011 \pm 0.003$	44k	<sup>1</sup> ABLIKIM 11	BES3	$J/\psi \rightarrow \gamma\eta\pi^+\pi^-$
$-0.107 \pm 0.096 \pm 0.003$	15k	<sup>2</sup> BLIK 09	GAM4	$32.5 \pi^- p \rightarrow \eta' n$
$0.015 \pm 0.011 \pm 0.014$	20k	<sup>3</sup> DOROFEEV 07	VES	$27 \pi^- p \rightarrow \eta' n,$ $\pi^- A \rightarrow \eta' \pi^- A^*$

<sup>1</sup> See ABLIKIM 11 for the full correlation matrix.

<sup>2</sup> From  $\eta' \rightarrow \eta\pi^0\pi^0$  decay.

<sup>3</sup> From  $\eta' \rightarrow \eta\pi^+\pi^-$  decay.

***d* decay parameter**

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
$-0.073 \pm 0.012 \pm 0.003$	44k	<sup>1</sup> ABLIKIM 11	BES3	$J/\psi \rightarrow \gamma \eta \pi^+ \pi^-$
$0.018 \pm 0.078 \pm 0.006$	15k	<sup>2</sup> BLIK 09	GAM4	$32.5 \pi^- p \rightarrow \eta' n$
$-0.082 \pm 0.017 \pm 0.008$	20k	<sup>3</sup> DOROFEEV 07	VES	$27 \pi^- p \rightarrow \eta' n,$ $\pi^- A \rightarrow \eta' \pi^- A^*$

<sup>1</sup> See ABLIKIM 11 for the full correlation matrix.<sup>2</sup> From  $\eta' \rightarrow \eta \pi^0 \pi^0$  decay. If  $c \equiv 0$  from Bose-Einstein symmetry,  $d = -0.067 \pm 0.020 \pm 0.003$ .<sup>3</sup> From  $\eta' \rightarrow \eta \pi^+ \pi^-$  decay.

### $\eta'(958)$ $\beta$ PARAMETER |MATRIX ELEMENT|<sup>2</sup> = (1 + 2 $\beta$ Z)

See the "Note on  $\eta$  Decay Parameters" in our 1994 edition *Physical Review D* **50** 1173 (1994), p. 1454.

 **$\beta$  decay parameter**

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b><math>-0.61 \pm 0.08</math> OUR AVERAGE</b>		Error includes scale factor of 1.2.		
$-0.640 \pm 0.046 \pm 0.047$	1.8k	ABLIKIM 15G	BES3	$J/\psi \rightarrow \gamma(\pi^0 \pi^0 \pi^0)$
$-0.59 \pm 0.18$	235	BLIK 08	GAMS	$32 \pi^- p \rightarrow \eta' n$
$-0.1 \pm 0.3$		ALDE 87B	GAM2	$38 \pi^- p \rightarrow n 3\pi^0$

 **$\eta'(958)$  C-NONCONSERVING DECAY PARAMETER**

See the note on  $\eta$  decay parameters in the Stable Particle Particle Listings for definition of this parameter.

**DECAY ASYMMETRY PARAMETER FOR  $\pi^+ \pi^- \gamma$** 

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b><math>-0.03 \pm 0.04</math> OUR AVERAGE</b>				
$-0.019 \pm 0.056$		AIHARA 87	TPC	$2\gamma \rightarrow \pi^+ \pi^- \gamma$
$-0.069 \pm 0.078$	295	GRIGORIAN 75	STRC	$2.1 \pi^- p$
$0.00 \pm 0.10$	103	KALBFLEISCH 75	HBC	$2.18 K^- p \rightarrow \Lambda \pi^+ \pi^- \gamma$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
$0.07 \pm 0.08$	152	RITTENBERG 65	HBC	$2.1-2.7 K^- p$

 **$\eta'(958) \rightarrow \gamma \ell^+ \ell^-$  TRANSITION FORM FACTOR SLOPE**

Related to the effective virtual meson mass  $\Lambda$ , via slope  $\approx \Lambda^{-2}$ . See e.g. LANDSBERG 85, eq. (3.8), for a detailed definition.

<u>VALUE (GeV<sup>-2</sup>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b><math>1.62 \pm 0.17</math> OUR AVERAGE</b>				
$1.60 \pm 0.17 \pm 0.08$	864	<sup>1</sup> ABLIKIM 150	BES3	$J/\psi \rightarrow \gamma e^+ e^-$
$1.7 \pm 0.4$	33	<sup>1</sup> VIKTOROV 80		$25,33 \pi^- p \rightarrow 2\mu\gamma$

<sup>1</sup> In the single-pole Ansatz where slope =  $1/(\Lambda^2 + \gamma^2)$  with  $\Lambda$ ,  $\gamma$  being a Breit-Wigner mass, width for the effective contributing vector meson.

$\eta'(958)$  REFERENCES

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ABLIKIM	16M	PR D93 072008	M. Ablikim <i>et al.</i>	(BES III Collab.)
ABLIKIM	15AD	PR D92 051101	M. Ablikim <i>et al.</i>	(BES III Collab.)
ABLIKIM	15G	PR D92 012014	M. Ablikim <i>et al.</i>	(BES III Collab.)
ABLIKIM	15O	PR D92 012001	M. Ablikim <i>et al.</i>	(BES III Collab.)
ABLIKIM	15P	PR D92 012007	M. Ablikim <i>et al.</i>	(BES III Collab.)
ACHASOV	15	PR D91 092010	M.N. Achasov <i>et al.</i>	(SND Collab.)
AKHMETSHIN	15	PL B740 273	R.R. Akhmetshin <i>et al.</i>	(CMD-3 Collab.)
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ABLIKIM	12E	PRL 108 182001	M. Ablikim <i>et al.</i>	(BES III Collab.)
PDG	12	PR D86 010001	J. Beringer <i>et al.</i>	(PDG Collab.)
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BLIK	09	PAN 72 231	A.M. Blik <i>et al.</i>	(IHEP (Protvino))
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WICHT	08	PL B662 323	J. Wicht <i>et al.</i>	(BELLE Collab.)
DOROFEEV	07	PL B651 22	V. Dorofeev <i>et al.</i>	(VES Collab.)
MORI	07A	JPSJ 76 074102	T. Mori <i>et al.</i>	(BELLE Collab.)
ABLIKIM	06E	PR D73 052008	M. Ablikim <i>et al.</i>	(BES Collab.)
ABLIKIM	06Q	PRL 97 202002	M. Ablikim <i>et al.</i>	(BES Collab.)
AMELIN	05A	PAN 68 372	D.V. Amelin <i>et al.</i>	(VES Collab.)
AMSLER	04B	EPJ C33 23	C. Amsler <i>et al.</i>	(Crystal Barrel Collab.)
BAI	04J	PL B594 47	J.Z. Bai <i>et al.</i>	(BES Collab.)
BRIERE	00	PRL 84 26	R. Briere <i>et al.</i>	(CLEO Collab.)
ACCIARRI	98Q	PL B418 399	M. Acciarri <i>et al.</i>	(L3 Collab.)
BARBERIS	98C	PL B440 225	D. Barberis <i>et al.</i>	(WA 102 Collab.)
WURZINGER	96	PL B374 283	R. Wurzinger <i>et al.</i>	(BONN, ORSAY, SACL+)
PDG	94	PR D50 1173	L. Montanet <i>et al.</i>	(CERN, LBL, BOST+)
AMSLER	93	ZPHY C58 175	C. Amsler <i>et al.</i>	(Crystal Barrel Collab.)
BELADIDZE	92C	SJNP 55 1535	G.M. Beladidze, S.I. Bityukov, G.V. Borisov	(SERP+)
KARCH	92	ZPHY C54 33	K. Karch <i>et al.</i>	(Crystal Ball Collab.)
ARMSTRONG	91B	ZPHY C52 389	T.A. Armstrong <i>et al.</i>	(ATHU, BARI, BIRM+)
BEHREND	91	ZPHY C49 401	H.J. Behrend <i>et al.</i>	(CELLO Collab.)
AUGUSTIN	90	PR D42 10	J.E. Augustin <i>et al.</i>	(DM2 Collab.)
BARU	90	ZPHY C48 581	S.E. Baru <i>et al.</i>	(MD-1 Collab.)
BUTLER	90	PR D42 1368	F. Butler <i>et al.</i>	(Mark II Collab.)
KARCH	90	PL B249 353	K. Karch <i>et al.</i>	(Crystal Ball Collab.)
ROE	90	PR D41 17	N.A. Roe <i>et al.</i>	(ASP Collab.)
AIHARA	88C	PR D38 1	H. Aihara <i>et al.</i>	(TPC-2 $\gamma$ Collab.)
VOROBYEV	88	SJNP 48 273	P.V. Vorobiev <i>et al.</i>	(NOVO)
WILLIAMS	88	PR D38 1365	D.A. Williams <i>et al.</i>	(Crystal Ball Collab.)
AIHARA	87	PR D35 2650	H. Aihara <i>et al.</i>	(TPC-2 $\gamma$ Collab.) JP
ALBRECHT	87B	PL B199 457	H. Albrecht <i>et al.</i>	(ARGUS Collab.)
ALDE	87B	ZPHY C36 603	D.M. Alde <i>et al.</i>	(LANL, BELG, SERP, LAPP)
ANTREASYAN	87	PR D36 2633	D. Antreasyan <i>et al.</i>	(Crystal Ball Collab.)
GIDAL	87	PRL 59 2012	G. Gidal <i>et al.</i>	(LBL, SLAC, HARV)
ALDE	86	PL B177 115	D.M. Alde <i>et al.</i>	(SERP, BELG, LANL, LAPP)
BARTEL	85E	PL 160B 421	W. Bartel <i>et al.</i>	(JADE Collab.)
LANDSBERG	85	PRPL 128 301	L.G. Landsberg	(SERP)
ALTHOFF	84E	PL 147B 487	M. Althoff <i>et al.</i>	(TASSO Collab.)
BERGER	84B	PL 142B 125	C. Berger	(PLUTO Collab.)
BINON	84	PL 140B 264	F.G. Binon <i>et al.</i>	(SERP, BELG, LAPP+)

JENNI	83	PR D27 1031	P. Jenni <i>et al.</i>	(SLAC, LBL)
BARTEL	82B	PL 113B 190	W. Bartel <i>et al.</i>	(JADE Collab.)
BEHREND	82C	PL 114B 378	H.J. Behrend <i>et al.</i>	(CELLO Collab.)
Also		PL 125B 518 (erratum)	H.J. Behrend <i>et al.</i>	(CELLO Collab.)
DZHEL'YADIN	81	PL 105B 239	R.I. Dzhelyadin <i>et al.</i>	(SERP)
STANTON	80	PL B92 353	N.R. Stanton <i>et al.</i>	(OSU, CARL, MCGI+)
VIKTOROV	80	SJNP 32 520	V.A. Viktorov <i>et al.</i>	(SERP)
APEL	79	PL 83B 131	W.D. Apel, K.H. Augenstein, E. Bertolucci	(KARLK+)
BINNIE	79	PL 83B 141	D.M. Binnie <i>et al.</i>	(LOIC)
ZANFINO	77	PRL 38 930	C. Zanfino <i>et al.</i>	(CARL, MCGI, OHIO+)
GRIGORIAN	75	NP B91 232	A. Grigorian <i>et al.</i>	(+)
KALBFLEISCH	75	PR D11 987	G.R. Kalbfleisch, R.C. Strand, J.W. Chapman	(BNL+)
DUANE	74	PRL 32 425	A. Duane <i>et al.</i>	(LOIC, SHMP)
KALBFLEISCH	74	PR D10 916	G.R. Kalbfleisch	(BNL)
DANBURG	73	PR D8 3744	J.S. Danburg <i>et al.</i>	(BNL, MICH) JP
JACOBS	73	PR D8 18	S.M. Jacobs <i>et al.</i>	(BRAN, UMD, SYRA+) JP
AGUILAR-...	72B	PR D6 29	M. Aguilar-Benitez <i>et al.</i>	(BNL)
APEL	72	PL 40B 680	W.D. Apel <i>et al.</i>	(KARLK, KARLE, PISA)
DALPIAZ	72	PL 42B 377	P.F. Dalpiaz <i>et al.</i>	(CERN)
BASILE	71	NC 3A 371	M. Basile <i>et al.</i>	(CERN, BGNA, STRB)
HARVEY	71	PRL 27 885	E.H. Harvey <i>et al.</i>	(MINN, MICH)
BENSINGER	70	PL 33B 505	J.R. Bensinger <i>et al.</i>	(WISC)
RITTENBERG	69	Thesis UCRL 18863	A. Rittenberg	(LRL) I
DAVIS	68	PL 27B 532	R. Davis <i>et al.</i>	(NWES, ANL)
LONDON	66	PR 143 1034	G.W. London <i>et al.</i>	(BNL, SYRA) IJP
BADIER	65B	PL 17 337	J. Badier <i>et al.</i>	(EPOL, SACL, AMST)
RITTENBERG	65	PRL 15 556	A. Rittenberg, G.R. Kalbfleisch	(LRL, BNL)
DAUBER	64	PRL 13 449	P.M. Dauber <i>et al.</i>	(UCLA) JP
KALBFLEISCH	64B	PRL 13 349	G.R. Kalbfleisch, O.I. Dahl, A. Rittenberg	(LRL) JP