## LIGHT QUARKS (u, d, s)

#### OMITTED FROM SUMMARY TABLE

#### u-QUARK MASS

The u-, d-, and s-quark masses are estimates of so-called "current-quark masses," in a mass- independent subtraction scheme such as  $\overline{\rm MS}$ . The ratios  $m_u/m_d$  and  $m_s/m_d$  are extracted from pion and kaon masses using chiral symmetry. The estimates of d and u masses are not without controversy and remain under active investigation. Within the literature there are even suggestions that the u quark could be essentially massless. The s-quark mass is estimated from SU(3) splittings in hadron masses.

We have normalized the  $\overline{\rm MS}$  masses at a renormalization scale of  $\mu=2$  GeV. Results quoted in the literature at  $\mu=1$  GeV have been rescaled by dividing by 1.35. The values of "Our Evaluation" were determined in part via Figures 1 and 2.

VALUE (MeV)	DOCUMENT ID		TECN	COMMENT
$2.3 \begin{array}{l} +0.7 \\ -0.5 \end{array}$ OUR EVALUATION	See the ideogram	belov	٧.	
$2.15 \pm 0.03 \pm 0.10$	<sup>1</sup> DURR	11	LATT	MS scheme
$2.24 \pm 0.10 \pm 0.34$	<sup>2</sup> BLUM	10	LATT	MS scheme
$2.01 \pm 0.14$	<sup>3</sup> MCNEILE	10	LATT	MS scheme
$2.9 \pm 0.2$	<sup>4</sup> DOMINGUEZ	09	THEO	MS scheme
$2.7 \pm 0.4$	<sup>5</sup> JAMIN	06	THEO	MS scheme
$1.9 \pm 0.2$	<sup>6</sup> MASON	06	LATT	MS scheme
$2.8 \pm 0.2$	<sup>7</sup> NARISON	06	THEO	MS scheme
• • • We do not use the followin	g data for averages	s, fits,	limits, e	etc. • • •
$2.01 \pm 0.14$	<sup>3</sup> DAVIES	10	LATT	MS scheme
$2.9 \pm 0.8$	<sup>8</sup> DEANDREA	80	THEO	MS scheme
$3.02 \pm 0.33$	<sup>9</sup> BLUM	07	LATT	MS scheme
$1.7 \pm 0.3$	<sup>10</sup> AUBIN	04A	LATT	MS scheme

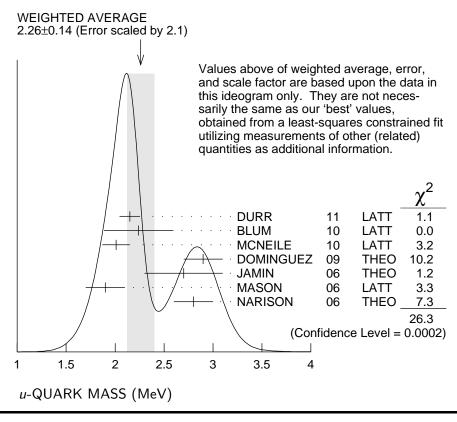
 $<sup>^1</sup>$  DURR 11 determine quark mass from a lattice computation of the meson spectrum using  $N_f=2+1$  dynamical flavors. The lattice simulations were done at the physical quark mass, so that extrapolation in the quark mass was not needed. The individual  $m_u$ ,  $m_d$  values are obtained using the lattice determination of the average mass  $m_{\rm ud}$  and of the ratio  $m_s/m_{\rm ud}$  and the value of  $Q=\left(m_s^2-m_{\rm ud}^2\right)/\left(m_d^2-m_u^2\right)$  as determined from  $\eta\to 3\pi$  decays.

 $<sup>^2</sup>$  BLUM 10 determines light quark masses using a QCD plus QED lattice computation of the electromagnetic mass splittings of the low-lying hadrons. The lattice simulations use 2+1 dynamical quark flavors.

 $<sup>^3</sup>$  DAVIES 10 and MCNEILE 10 determine  $\overline{m}_{\mathcal{C}}(\mu)/\overline{m}_{\mathcal{S}}(\mu)=11.85\pm0.16$  using a lattice computation with  $N_f=2+1$  dynamical fermions of the pseudoscalar meson masses. Mass  $m_U$  is obtained from this using the value of  $m_C$  from ALLISON 08 or MCNEILE 10 and the BAZAVOV 10 values for the light quark mass ratios,  $m_S/\overline{m}$  and  $m_U/m_d$ .

<sup>&</sup>lt;sup>4</sup>DOMINGUEZ 09 use QCD finite energy sum rules for the two-point function of the divergence of the axial vector current computed to order  $\alpha_s^4$ .

- <sup>5</sup> JAMIN 06 determine  $m_u(2 \text{ GeV})$  by combining the value of  $m_s$  obtained from the spectral function for the scalar  $K\pi$  form factor with other determinations of the quark mass ratios.
- <sup>6</sup> MASON 06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate u and d quarks. Perturbative corrections were included at NNLO order. The quark masses  $m_u$  and  $m_d$  were determined from their  $(m_u + m_d)/2$  measurement and AUBIN 04A  $m_u/m_d$  value.
- <sup>7</sup> NARISON 06 uses sum rules for  $e^+e^- \rightarrow$  hadrons to order  $\alpha_s^3$  to determine  $m_s$  combined with other determinations of the quark mass ratios.
- $^8$  DEANDREA 08 determine  $m_u-m_d$  from  $\eta\to 3\pi^0$ , and combine with the PDG 06 lattice average value of  $m_u+m_d=7.6\pm1.6$  to determine  $m_u$  and  $m_d$ .
- <sup>9</sup> BLUM 07 determine quark masses from the pseudoscalar meson masses using a QED plus QCD lattice computation with two dynamical quark flavors.
- 10 AUBIN 04A employ a partially quenched lattice calculation of the pseudoscalar meson masses.



#### d-QUARK MASS

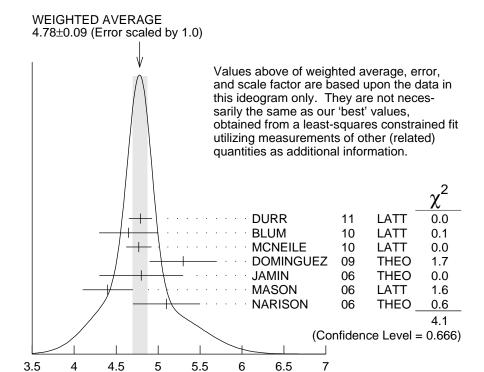
See the comment for the u quark above.

We have normalized the  $\overline{\rm MS}$  masses at a renormalization scale of  $\mu=2$  GeV. Results quoted in the literature at  $\mu=1$  GeV have been rescaled by

dividing by 1.35. The values of "Our Evaluation" were determined in part via Figures 1 and 2.

VALUE (MeV)	DOCUMENT ID		TECN	COMMENT
4.8 $^{+0.5}_{-0.3}$ OUR EVALUATION	See the ideogram	below	·.	
$4.79\pm0.07\pm0.12$	<sup>11</sup> DURR	11	LATT	MS scheme
$4.65 \pm 0.15 \pm 0.32$	<sup>12</sup> BLUM	10	LATT	MS scheme
$4.77 \pm 0.15$	<sup>13</sup> MCNEILE	10	LATT	MS scheme
5.3 ±0.4	<sup>14</sup> DOMINGUEZ	09	THEO	MS scheme
$4.8 \pm 0.5$	<sup>15</sup> JAMIN	06	THEO	MS scheme
$4.4 \pm 0.3$	<sup>16</sup> MASON	06	LATT	MS scheme
$5.1 \pm 0.4$	<sup>17</sup> NARISON	06	THEO	MS scheme
• • • We do not use the following	g data for averages	, fits,	limits, e	etc. • • •
$4.79 \pm 0.16$	<sup>13</sup> DAVIES	10	LATT	MS scheme
$4.7 \pm 0.8$	<sup>18</sup> DEANDREA	80	THEO	MS scheme
$5.49 \pm 0.39$	<sup>19</sup> BLUM	07	LATT	MS scheme
$3.9 \pm 0.5$	<sup>20</sup> AUBIN	04A	LATT	MS scheme

- 11 DURR 11 determine quark mass from a lattice computation of the meson spectrum using  $N_f=2+1$  dynamical flavors. The lattice simulations were done at the physical quark mass, so that extrapolation in the quark mass was not needed. The individual  $m_u$ ,  $m_d$  values are obtained using the lattice determination of the average mass  $m_{\rm ud}$  and of the ratio  $m_s/m_{\rm ud}$  and the value of  $Q=(m_s^2-m_{\rm ud}^2)/(m_d^2-m_u^2)$  as determined from  $\eta\to 3\pi$  decays.
- $^{12}$  BLUM 10 determines light quark masses using a QCD plus QED lattice computation of the electromagnetic mass splittings of the low-lying hadrons. The lattice simulations use  $^{2+1}$  dynamical quark flavors.
- $^{13}$  DAVIES 10 and MCNEILE 10 determine  $\overline{m}_{\mathcal{C}}(\mu)/\overline{m}_{\mathcal{S}}(\mu)=11.85\pm0.16$  using a lattice computation with  $N_f=2+1$  dynamical fermions of the pseudoscalar meson masses. Mass  $m_d$  is obtained from this using the value of  $m_{\mathcal{C}}$  from ALLISON 08 or MCNEILE 10 and the BAZAVOV 10 values for the light quark mass ratios,  $m_{\mathcal{S}}/\overline{m}$  and  $m_{\mathcal{U}}/m_{\mathcal{d}}$ .
- <sup>14</sup>DOMINGUEZ 09 use QCD finite energy sum rules for the two-point function of the divergence of the axial vector current computed to order  $\alpha_s^4$ .
- <sup>15</sup> JAMIN 06 determine  $m_d(2 \text{ GeV})$  by combining the value of  $m_s$  obtained from the spectral function for the scalar  $K\pi$  form factor with other determinations of the quark mass ratios.
- $^{16}$  MASON 06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate u and d quarks. Perturbative corrections were included at NNLO order. The quark masses  $m_u$  and  $m_d$  were determined from their  $(m_u + m_d)/2$  measurement and AUBIN 04A  $m_u/m_d$  value.
- <sup>17</sup> NARISON 06 uses sum rules for  $e^+e^- \rightarrow$  hadrons to order  $\alpha_s^3$  to determine  $m_s$  combined with other determinations of the quark mass ratios.
- $^{18}$  DEANDREA 08 determine  $m_u-m_d$  from  $\eta\to 3\pi^0$  , and combine with the PDG 06 lattice average value of  $m_u+m_d=7.6\pm 1.6$  to determine  $m_u$  and  $m_d$  .
- $^{19}\,\mathrm{BLUM}$  07 determine quark masses from the pseudoscalar meson masses using a QED plus QCD lattice computation with two dynamical quark flavors.
- <sup>20</sup> AUBIN 04A perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with continuum estimate of electromagnetic effects in the kaon masses, and one-loop perturbative renormalization constant.



### $\overline{m} = (m_u + m_d)/2$

See the comments for the u quark above.

d-QUARK MASS (MeV)

We have normalized the  $\overline{\rm MS}$  masses at a renormalization scale of  $\mu=2$  GeV. Results quoted in the literature at  $\mu=1$  GeV have been rescaled by dividing by 1.35. The values of "Our Evaluation" were determined in part via Figures 1 and 2.

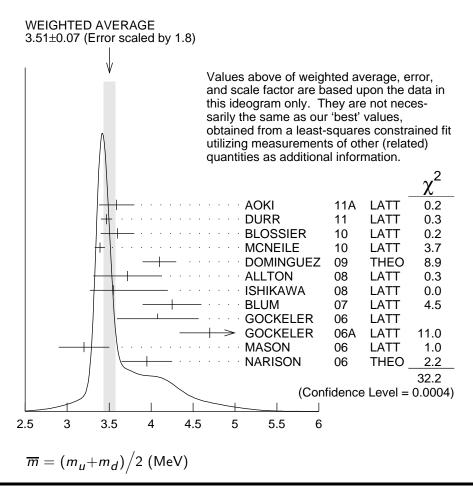
VALUE (MeV)		DOCUMENT ID		TECN	COMMENT
$\begin{array}{cc} 3.5 & +0.7 \\ -0.2 \end{array}$	OUR EVALUATION	ON See the ideog	ram l	pelow.	
$3.59 \pm 0.21$ $3.469 \pm 0.047$ $3.6 \pm 0.2$ $3.39 \pm 0.06$ $4.1 \pm 0.2$	±0.048	21 AOKI 22 DURR 23 BLOSSIER 24 MCNEILE 25 DOMINGUEZ 26 ALLTON	11 10 10 09		MS scheme MS scheme MS scheme MS scheme MS scheme
$3.72 \pm 0.41$ $3.55 + 0.65$ $-0.28$ $4.25 \pm 0.35$ $4.08 \pm 0.25$ $4.7 \pm 0.2$ $3.2 \pm 0.3$ $3.95 \pm 0.3$	±0.42 ±0.3	27 ISHIKAWA 28 BLUM 29 GOCKELER 30 GOCKELER 31 MASON 32 NARISON	08 08 07 06 06A 06 06	LATT LATT LATT LATT LATT LATT THEO	MS scheme  MS scheme

• • • We do not use the following data for averages, fits, limits, etc. • • •

$3.40 \pm 0.07$	<sup>24</sup> DAVIES	10	LATT	MS scheme
$3.85 \pm 0.12 \pm 0.4$	<sup>33</sup> BLOSSIER	80	LATT	MS scheme
$\geq 4.85 \pm 0.20$	<sup>34</sup> DOMINGUEZ.	08в	THEO	MS scheme
$4.026 \pm 0.048$	<sup>35</sup> NAKAMURA	80	LATT	MS scheme
$2.8 \pm 0.3$	<sup>36</sup> AUBIN	04	LATT	MS scheme
$4.29 \pm 0.14 \pm 0.65$	<sup>37</sup> AOKI	03	LATT	MS scheme
$3.223 \pm 0.3$	<sup>38</sup> AOKI	<b>03</b> B	LATT	MS scheme
$4.4 \pm 0.1 \pm 0.4$	<sup>39</sup> BECIREVIC	03	LATT	MS scheme
$4.1 \pm 0.3 \pm 1.0$	<sup>40</sup> CHIU	03	LATT	MS scheme

- $^{21}$  AOKI 11A determine quark masses from a lattice computation of the hadron spectrum using  $N_f=2+1$  dynamical flavors of domain wall fermions.
- $^{22}$  DURR 11 determine quark mass from a lattice computation of the meson spectrum using  $N_f=2+1$  dynamical flavors. The lattice simulations were done at the physical quark mass, so that extrapolation in the quark mass was not needed.
- <sup>23</sup> BLOSSIER 10 determines quark masses from a computation of the hadron spectrum using  $N_f$ =2 dynamical twisted-mass Wilson fermions.
- <sup>24</sup> DAVIES 10 and MCNEILE 10 determine  $\overline{m}_{\mathcal{C}}(\mu)/\overline{m}_{\mathcal{S}}(\mu)=11.85\pm0.16$  using a lattice computation with  $N_f=2+1$  dynamical fermions of the pseudoscalar meson masses. Mass  $\overline{m}$  is obtained from this using the value of  $m_{\mathcal{C}}$  from ALLISON 08 or MCNEILE 10 and the BAZAVOV 10 values for the light quark mass ratio,  $m_{\mathcal{S}}/\overline{m}$ .
- <sup>25</sup> DOMINGUEZ 09 use QCD finite energy sum rules for the two-point function of the divergence of the axial vector current computed to order  $\alpha_s^4$ .
- <sup>26</sup> ALLTON 08 use a lattice computation of the  $\pi$ , K, and  $\Omega$  masses with 2+1 dynamical flavors of domain wall quarks, and non-perturbative renormalization.
- <sup>27</sup> ISHIKAWA 08 use a lattice computation of the light meson spectrum with 2+1 dynamical flavors of  $\mathcal{O}(a)$  improved Wilson quarks, and one-loop perturbative renormalization.
- <sup>28</sup> BLUM 07 determine quark masses from the pseudoscalar meson masses using a QED plus QCD lattice computation with two dynamical quark flavors.
- $^{29}$  GOCKELER 06 use an unquenched lattice computation of the axial Ward Identity with  $N_f=2$  dynamical light quark flavors, and non-perturbative renormalization, to obtain  $\overline{m}(2~{\rm GeV})=4.08\pm0.25\pm0.19\pm0.23~{\rm MeV},$  where the first error is statistical, the second and third are systematic due to the fit range and force scale uncertainties, respectively. We have combined the systematic errors linearly.
- $^{30}$  GOCKELER 06A use an unquenched lattice computation of the pseudoscalar meson masses with  $N_f=2$  dynamical light quark flavors, and non-perturbative renormalization.
- MASON 06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate u and d quarks. Perturbative corrections were included at NNLO order.
- $^{32}$  NARISON 06 uses sum rules for  $e^+e^- \to {\rm hadrons}$  to order  $\alpha_s^3$  to determine  $m_s$  combined with other determinations of the quark mass ratios.
- 33 BLOSSIER 08 use a lattice computation of pseudoscalar meson masses and decay constants with 2 dynamical flavors and non-perturbative renormalization.
- 34 DOMINGUEZ-CLARIMON 08B obtain an inequality from sum rules for the scalar two-point correlator.
- 35 NAKAMURA 08 do a lattice computation using quenched domain wall fermions and non-perturbative renormalization.
- <sup>36</sup> AUBIN 04 perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with one-loop perturbative renormalization constant.
- <sup>37</sup> AOKI 03 uses quenched lattice simulation of the meson and baryon masses with degenerate light quarks. The extrapolations are done using quenched chiral perturbation theory.

- $^{38}$  The errors given in AOKI 03B were  $^{+0.046}_{-0.069}.$  We changed them to  $\pm 0.3$  for calculating the overall best values. AOKI 03B uses lattice simulation of the meson and baryon masses with two dynamical light quarks. Simulations are performed using the  $\mathcal{O}(a)$  improved Wilson action.
- BECIREVIC 03 perform quenched lattice computation using the vector and axial Ward identities. Uses  $\mathcal{O}(a)$  improved Wilson action and nonperturbative renormalization.
- <sup>40</sup> CHIU 03 determines quark masses from the pion and kaon masses using a lattice simulation with a chiral fermion action in quenched approximation.



#### $m_u/m_d$ MASS RATIO

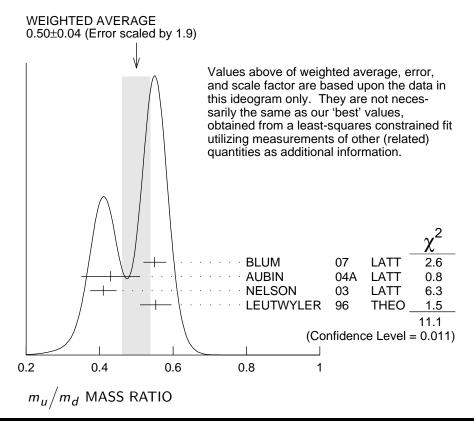
VALUE	DOCUMENT ID		TECN	COMMENT
0.38-0.58 OUR EVALUATION	See the ideogram b	elow.		
$0.550 \pm 0.031$	<sup>41</sup> BLUM	07	LATT	
$0.43 \pm 0.08$	<sup>42</sup> AUBIN	04A	LATT	
$0.410 \pm 0.036$	<sup>43</sup> NELSON	03	LATT	
$0.553 \pm 0.043$	<sup>44</sup> LEUTWYLER	96	THEO	Compilation

 $<sup>^{41}\,\</sup>mathrm{BLUM}$  07 determine quark masses from the pseudoscalar meson masses using a QED plus QCD lattice computation with two dynamical quark flavors.

<sup>&</sup>lt;sup>42</sup> AUBIN 04A perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with continuum estimate of electromagnetic effects in the kaon masses.

 $^{43}$  NELSON 03 computes coefficients in the order  $p^4$  chiral Lagrangian using a lattice calculation with three dynamical flavors. The ratio  $m_u/m_d$  is obtained by combining this with the chiral perturbation theory computation of the meson masses to order  $p^4$ .

<sup>44</sup> LEUTWYLER 96 uses a combined fit to  $\eta \to 3\pi$  and  $\psi' \to J/\psi$   $(\pi,\eta)$  decay rates, and the electromagnetic mass differences of the  $\pi$  and K.



#### s-QUARK MASS

See the comment for the u quark above.

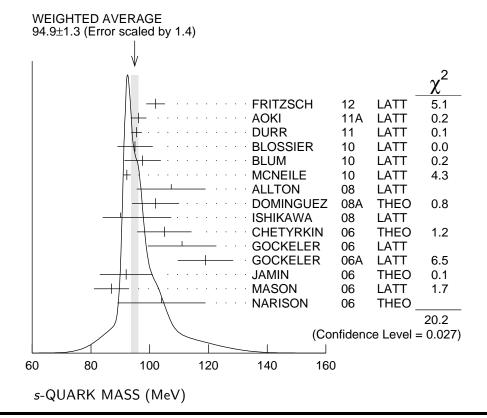
We have normalized the  $\overline{\rm MS}$  masses at a renormalization scale of  $\mu=2$  GeV. Results quoted in the literature at  $\mu=1$  GeV have been rescaled by dividing by 1.35.

VALUE (MeV)	DOCUMENT ID		TECN	COMMENT
95 $\pm$ 5 OUR EVALUATION		belo	w.	
$102 \pm 3 \pm 1$		12	LATT	MS scheme
96.2± 2.7	<sup>46</sup> AOKI			MS scheme
$95.5 \pm \ 1.1 \pm \ 1.5$	<sup>47</sup> DURR	11	LATT	MS scheme
$95 \pm 6$	<sup>48</sup> BLOSSIER		LATT	MS scheme
$97.6\pm\ 2.9\pm\ 5.5$	<sup>49</sup> BLUM	10		MS scheme
$92.2 \pm 1.3$	<sup>50</sup> MCNEILE	10	LATT	MS scheme
$107.3 \pm 11.7$	<sup>51</sup> ALLTON	80	LATT	MS scheme
102 ± 8	<sup>52</sup> DOMINGUEZ	08A	THEO	MS scheme
$90.1^{+17.2}_{-6.1}$	<sup>53</sup> ISHIKAWA	80	LATT	MS scheme

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<sup>54</sup> CHETYRKIN
105 \pm 6 \pm 7
                                                                 THEO MS scheme
                                      <sup>55</sup> GOCKELER
111 \pm 6 \pm 10
                                                                 LATT
                                                                         MS scheme
                                      <sup>56</sup> GOCKELER
119 \pm 5
                                                          06A
                                                               LATT
             \pm 8
                                                                         MS scheme
                                      <sup>57</sup> JAMIN
                                                                 THEO MS scheme
 92 \pm 9
                                                           06
                                      <sup>58</sup> MASON
87 \pm 6
                                                           06
                                                                         MS scheme
                                      <sup>59</sup> NARISON
104 \pm 15
                                                                 THEO MS scheme
                                                          06
• • • We do not use the following data for averages, fits, limits, etc. • • •
                                      <sup>50</sup> DAVIES
 92.4 \pm 1.5
                                                           10
                                                                 LATT
                                                                         MS scheme
                                      <sup>60</sup> BLOSSIER
105 \pm 3 \pm 9
                                                           80
                                                                          MS scheme
                                      <sup>61</sup> NAKAMURA
                                                                         MS scheme
105.6 \pm 1.2
                                                          80
                                                                 LATT
                                      62 BLUM
119.5 \pm 9.3
                                                           07
                                                                         MS scheme
                                                                 LATT
                                      <sup>63</sup> NARISON
\geq 71 \pm 4, \leq 151 \pm 14
                                                                 THEO MS scheme
             ^{+16}_{-18}
                                      <sup>64</sup> BAIKOV
                                                                 THEO MS scheme
                                                           05
                                      <sup>65</sup> GAMIZ
 81
    \pm 22
                                                           05
                                                                 THEO MS scheme
                                      <sup>66</sup> GORBUNOV
                                                                 THEO MS scheme
125
                                                           05
     \pm 28
                                      <sup>67</sup> NARISON
 93 \pm 32
                                                           05
                                                                 THEO MS scheme
                                      <sup>68</sup> AUBIN
 76 \pm 8
                                                           04
                                                                 LATT
                                                                         MS scheme
                                      <sup>69</sup> AOKI
116 \pm 6 \pm 0.65
                                                           03
                                                                 LATT
                                                                         MS scheme
 84.5 + 12
                                      <sup>70</sup> AOKI
                                                                         MS scheme
                                                           03B
                                                               LATT
                                      <sup>71</sup> BECIREVIC
106
    \pm 2
                                                           03
                                                                LATT
                                                                         MS scheme
             \pm 8
                                      <sup>72</sup> CHIU
 92 \pm 9
                                                           03
                                                                LATT
                                                                         MS scheme
             \pm 16
                                      <sup>73</sup> GAMIZ
117 \pm 17
                                                          03
                                                                 THEO MS scheme
                                      <sup>74</sup> GAMIZ
103 \pm 17
                                                          03
                                                                THEO MS scheme
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- $^{45}$  FRITZSCH 12 determine  $m_{_S}$  using a lattice computation with  $N_f=2$  dynamical flavors.
- $^{46}$  AOKI 11A determine quark masses from a lattice computation of the hadron spectrum using  $N_f=2+1$  dynamical flavors of domain wall fermions.
- $^{47}$  DURR 11 determine quark mass from a lattice computation of the meson spectrum using  $N_f=2+1$  dynamical flavors. The lattice simulations were done at the physical quark mass, so that extrapolation in the quark mass was not needed.
- <sup>48</sup> BLOSSIER 10 determines quark masses from a computation of the hadron spectrum using  $N_f$ =2 dynamical twisted-mass Wilson fermions.
- $^{49}$  BLUM 10 determines light quark masses using a QCD plus QED lattice computation of the electromagnetic mass splittings of the low-lying hadrons. The lattice simulations use  $^{2+1}$  dynamical quark flavors.
- $^{50}$  DAVIES 10 and MCNEILE 10 determine  $\overline{m}_{\mathcal{C}}(\mu)/\overline{m}_{\mathcal{S}}(\mu)=11.85\pm0.16$  using a lattice computation with  $N_f=2+1$  dynamical fermions of the pseudoscalar meson masses. Mass  $m_{\mathcal{S}}$  is obtained from this using the value of  $m_{\mathcal{C}}$  from ALLISON 08 or MCNEILE 10.
- <sup>51</sup> ALLTON 08 use a lattice computation of the  $\pi$ , K, and  $\Omega$  masses with 2+1 dynamical flavors of domain wall quarks, and non-perturbative renormalization.
- <sup>52</sup> DOMINGUEZ 08A make determination from QCD finite energy sum rules for the pseudoscalar two-point function computed to order  $\alpha_s^4$ .
- <sup>53</sup> ISHIKAWA 08 use a lattice computation of the light meson spectrum with 2+1 dynamical flavors of  $\mathcal{O}(a)$  improved Wilson quarks, and one-loop perturbative renormalization.
- $^{54}$  CHETYRKIN 06 use QCD sum rules in the pseudoscalar channel to order  $\alpha_s^4$  .
- $^{55}$  GOCKELER 06 use an unquenched lattice computation of the axial Ward Identity with  $N_f=2$  dynamical light quark flavors, and non-perturbative renormalization, to obtain  $\overline{m}_{\rm S}(2~{\rm GeV})=111\pm 6\pm 4\pm 6~{\rm MeV},$  where the first error is statistical, the second and third are systematic due to the fit range and force scale uncertainties, respectively. We have combined the systematic errors linearly.
- $^{56}$  GOCKELER 06A use an unquenched lattice computation of the pseudoscalar meson masses with  $N_f=2$  dynamical light quark flavors, and non-perturbative renormalization.

- $^{57}$  JAMIN 06 determine  $\overline{m}_{s}$ (2 GeV) from the spectral function for the scalar  $K\pi$  form
- factor.  $58\,\mathrm{MASON}$  06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate u and d quarks. Perturbative corrections were included at NNLO order.
- $^{59}$  NARISON 06 uses sum rules for  $e^+e^- 
  ightarrow$  hadrons to order  $lpha_s^3$  .
- $^{60}\, ext{BLOSSIER}$  08 use a lattice computation of pseudoscalar meson masses and decay constants with 2 dynamical flavors and non-perturbative renormalization.
- $^{
  m 61}\,$ NAKAMURA 08 do a lattice computation using quenched domain wall fermions and non-perturbative renormalization.
- $^{62}\, ext{BLUM}$  07 determine quark masses from the pseudoscalar meson masses using a QED plus QCD lattice computation with two dynamical quark flavors.
- 63 NARISON 06 obtains the quoted range from positivity of the spectral functions. 64 BAIKOV 05 determines  $\overline{m}_s(M_\tau) = 100^{+5}_{-3}^{+5}_{-19}^{+17}$  from sum rules using the strange spectral function in  $\tau$  decay. The computations were done to order  $\alpha_s^3$ , with an estimate of the  $\alpha_{\rm c}^4$  terms. We have converted the result to  $\mu=$  2 GeV.
- $^{65}$  GAMIZ 05 determines  $\overline{m}_{\rm S}({
  m 2~GeV})$  from sum rules using the strange spectral function in  $\tau$  decay. The computations were done to order  $\alpha_s^2$ , with an estimate of the  $\alpha_s^3$  terms.
- $^{66}$  GORBUNOV 05 use hadronic tau decays to N $^3$ LO, including power corrections.
- $^{67}$  NARISON 05 determines  $\overline{m}_{\rm S}({\rm 2~GeV})$  from sum rules using the strange spectral function in  $\tau$  decay. The computations were done to order  $\alpha_s^3$ .
- $^{68}\,\mathrm{AUBIN}$  04 perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with one-loop perturbative renormalization constant.
- $^{69}\,\mathrm{AOKI}$  03 uses quenched lattice simulation of the meson and baryon masses with degenerate light quarks. The extrapolations are done using quenched chiral perturbation theory. Determines  ${\rm m}_s$  =113.8  $\pm$  2.3 $^{+}_{-2.9}$  using K mass as input and  ${\rm m}_s$ =142.3  $\pm$  5.8 $^{+}_{-0}$  using  $\phi$  mass as input. We have performed a weighted average of these values.
- $70\,\mathrm{AOKI}$  03B uses lattice simulation of the meson and baryon masses with two dynamical light quarks. Simulations are performed using the  $\mathcal{O}(a)$  improved Wilson action.
- $^{71}$ BECIREVIC 03 perform quenched lattice computation using the vector and axial Ward identities. Uses  $\mathcal{O}(a)$  improved Wilson action and nonperturbative renormalization. They also quote  $\overline{m}/m_s=24.3\pm0.2\pm0.6$ .
- $^{72}$  CHIU 03 determines quark masses from the pion and kaon masses using a lattice simulation with a chiral fermion action in quenched approximation.
- $^{73}$  GAMIZ 03 determines  $m_{S}$  from SU(3) breaking in the au hadronic width. The value of  $V_{\mu s}$  is chosen to satisfy ČKM unitarity.
- $^{74}$  GAMIZ 03 determines  $m_{_S}$  from SU(3) breaking in the au hadronic width. The value of  $V_{IIS}$  is taken from the PDG.



#### **OTHER LIGHT QUARK MASS RATIOS**

#### $m_s/m_d$ MASS RATIO

VALUE	<u>DOCUMENT ID</u>		<u>TECN</u> <u>COMMENT</u>	
17-22 OUR EVALUATION				
• • • We do not use the following	ig data for averages	, fits,	limits, etc. • • •	
20.0			THEO	
$18.9 \pm 0.8$	<sup>76</sup> LEUTWYLER	96	THEO Compilation	
21	<sup>77</sup> DONOGHUE			
18	<sup>78</sup> GERARD			
18 to 23	<sup>79</sup> LEUTWYLER	<b>90</b> B	THEO	

<sup>&</sup>lt;sup>75</sup> GAO 97 uses electromagnetic mass splittings of light mesons.

 $<sup>^{76}</sup>$  LEUTWYLER 96 uses a combined fit to  $\eta\to 3\pi$  and  $\psi'\to J/\psi~(\pi,\eta)$  decay rates, and the electromagnetic mass differences of the  $\pi$  and K

<sup>77</sup> DONOGHUE 92 result is from a combined analysis of meson masses,  $\eta \to 3\pi$  using second-order chiral perturbation theory including nonanalytic terms, and  $(\psi(2S) \to J/\psi(1S)\pi)/(\psi(2S) \to J/\psi(1S)\eta)$ .

<sup>78</sup> GERARD 90 uses large N and  $\eta$ - $\eta'$  mixing.

 $<sup>^{79}</sup>$  LEUTWYLER 90B determines quark mass ratios using second-order chiral perturbation theory for the meson and baryon masses, including nonanalytic corrections. Also uses Weinberg sum rules to determine  $L_7$ .

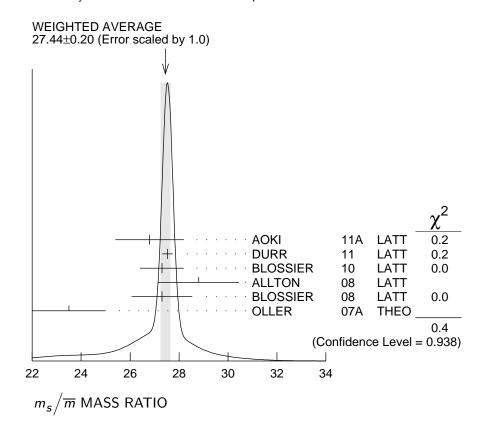
# $m_s/\overline{m}$ MASS RATIO $\overline{m} \equiv (m_u + m_d)/2$

$$\overline{m} \equiv (m_u + m_d)/2$$

VALUE	DOCUMENT ID		TECN
27.5 $\pm 1.0$ OUR EVALUATION	See the ideogram	n belov	w.
$26.8 \pm 1.4$	<sup>80</sup> AOKI	11A	LATT
$27.53 \pm 0.20 \pm 0.08$	<sup>81</sup> DURR	11	LATT
$27.3 \pm 0.9$	<sup>82</sup> BLOSSIER	10	LATT
$28.8 \pm 1.65$	<sup>83</sup> ALLTON	80	LATT
$27.3 \pm 0.3 \pm 1.2$	<sup>84</sup> BLOSSIER	80	LATT
$23.5 \pm 1.5$	<sup>85</sup> OLLER	07A	THEO
• • • We do not use the following	g data for averages	s, fits,	limits, etc. $ullet$
27.4 ±0.4	<sup>86</sup> AUBIN	04	LATT

 $<sup>^{80}\,\</sup>mathrm{AOKI}$  11A determine quark masses from a lattice computation of the hadron spectrum using  $N_f = 2 + 1$  dynamical flavors of domain wall fermions.

 $<sup>^{86}</sup>$  Three flavor dynamical lattice calculation of pseudoscalar meson masses.



 $<sup>^{81}</sup>$  DURR 11 determine quark mass from a lattice computation of the meson spectrum using  $N_f = 2 + 1$  dynamical flavors. The lattice simulations were done at the physical quark mass, so that extrapolation in the quark mass was not needed.

 $<sup>82\,\</sup>mathrm{BLOSSIER}$  10 determines quark masses from a computation of the hadron spectrum using  $N_f$ =2 dynamical twisted-mass Wilson fermions.

 $<sup>^{83}</sup>$  ALLTON 08 use a lattice computation of the  $\pi$ , K, and  $\Omega$  masses with 2+1 dynamical flavors of domain wall quarks, and non-perturbative renormalization.

 $<sup>^{84}\, \</sup>text{BLOSSIER}$  08 use a lattice computation of pseudoscalar meson masses and decay constants with 2 dynamical flavors and non-perturbative renormalization.

 $<sup>^{85}</sup>$  OLLER 07A use unitarized chiral perturbation theory to order  $p^4$ .

#### **Q MASS RATIO**

$$Q \equiv \sqrt{(m_s^2 - \overline{m}^2)/(m_d^2 - m_u^2)}; \quad \overline{m} \equiv (m_u + m_d)/2$$
ALUE

DOCUMENT ID

TECN

 $\bullet$   $\bullet$  We do not use the following data for averages, fits, limits, etc.  $\bullet$   $\bullet$ 

 $22.8\pm0.4$  \$87 MARTEMYA... 05 THEO  $22.7\pm0.8$  88 ANISOVICH 96 THEO

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 $<sup>^{87}\,\</sup>mathrm{MARTEMYANOV}$  05 determine Q from  $\eta \to ~3\pi$  decay.

<sup>&</sup>lt;sup>88</sup> ANISOVICH 96 find Q from  $\eta \to \pi^+\pi^-\pi^0$  decay using dispersion relations and chiral perturbation theory.