

b

$$I(J^P) = 0(\frac{1}{2}^+)$$

Charge = $-\frac{1}{3}$ e Bottom = -1

b-QUARK MASS

The first value is the “running mass” $\overline{m}_b(\mu = \overline{m}_b)$ in the $\overline{\text{MS}}$ scheme, and the second value is the $1S$ mass, which is half the mass of the $\Upsilon(1S)$ in perturbation theory. For a review of different quark mass definitions and their properties, see EL-KHADRA 02. The $1S$ mass is better suited for use in analyzing B decays than the $\overline{\text{MS}}$ mass because it gives a stable perturbative expansion. We have converted masses in other schemes to the $\overline{\text{MS}}$ mass and $1S$ mass using two-loop QCD perturbation theory with $\alpha_s(\mu = \overline{m}_b) = 0.22$. The range 4.1–4.4 for the $\overline{\text{MS}}$ mass corresponds to 4.6–4.9 for the $1S$ mass and 4.7–5.0 GeV for the pole mass.

$\overline{\text{MS}} \text{ MASS (GeV)}$	$1S \text{ MASS (GeV)}$	<i>DOCUMENT ID</i>	<i>TECN</i>
4.20 ±0.07 OUR EVALUATION	of $\overline{\text{MS}}$ Mass		
4.70 ±0.07 OUR EVALUATION	of $1S$ Mass		
4.19 ± 0.40	4.66 ± 0.45	¹ ABDALLAH	06D DLPH
4.205 ± 0.058	4.68 ± 0.06	² BOUGHEZAL	06 THEO
4.19 ± 0.06	4.66 ± 0.07	³ PINEDA	06 THEO
4.4 ± 0.3	4.9 ± 0.3	^{4,5} GRAY	05 LATT
4.22 ± 0.06	4.72 ± 0.07	⁶ AUBERT	04X THEO
4.17 ± 0.03	4.68 ± 0.03	⁷ BAUER	04 THEO
4.22 ± 0.11	4.72 ± 0.12	^{5,8} HOANG	04 THEO
4.25 ± 0.11	4.76 ± 0.12	^{5,9} MCNEILE	04 LATT
4.22 ± 0.09	4.74 ± 0.10	¹⁰ BAUER	03 THEO
4.19 ± 0.05	4.66 ± 0.05	¹¹ BORDES	03 THEO
4.20 ± 0.09	4.67 ± 0.10	¹² CORCELLA	03 THEO
4.33 ± 0.10	4.84 ± 0.11	^{5,13} DEDIVITIIS	03 LATT
4.24 ± 0.10	4.72 ± 0.11	¹⁴ EIDEMULLER	03 THEO
4.207 ± 0.031	4.682 ± 0.035	¹⁵ ERLER	03 THEO
4.33 ± 0.06 ± 0.10	4.82 ± 0.07 ± 0.11	¹⁶ MAHMOOD	03 THEO
4.346 ± 0.070	4.837 ± 0.078	¹⁷ PENIN	02 THEO
3.95 ± 0.57	4.40 ± 0.63	¹⁸ ABBIENDI	01S OPAL
4.21 ± 0.05	4.69 ± 0.06	¹⁹ KUHN	01 THEO
4.05 ± 0.06	4.51 ± 0.07	²⁰ NARISON	01B THEO
4.210 ± 0.090 ± 0.025	4.69 ± 0.100 ± 0.028	²¹ PINEDA	01 THEO
4.7 ± 0.74	5.23 ± 0.82	²² BARATE	00V ALEP
4.20 ± 0.06	4.71 ± 0.03	²³ HOANG	00 THEO
• • • We do not use the following data for averages, fits, limits, etc. • • •			
4.437 $^{+0.045}_{-0.029}$	4.938 $^{+0.050}_{-0.032}$	²⁴ LUCHA	00 THEO
4.454 $^{+0.045}_{-0.029}$	4.957 $^{+0.050}_{-0.032}$	²⁴ PINEDA	00 THEO
4.25 ± 0.08	4.73 ± 0.09	²⁵ BENEKE	99 THEO
3.8 $^{+0.77}_{-2.0}$	4.23 $^{+0.86}_{-2.0}$	²⁶ BRANDENB...	99
4.25 ± 0.09	4.73 ± 0.10	²⁷ HOANG	99 THEO
4.2 ± 0.1	4.67 ± 0.11	²⁸ MELNIKOV	99 THEO

4.21 ± 0.11	4.69 ± 0.12	29 PENIN	99	THEO
3.91 ± 0.67	4.35 ± 0.75	30 ABREU	98I	DLPH
4.14 ± 0.04	4.61 ± 0.05	31 KUEHN	98	THEO
$4.15 \pm 0.05 \pm 0.20$	$4.62 \pm 0.06 \pm 0.22$	32 GIMENEZ	97	LATT
4.19 ± 0.06	4.66 ± 0.07	33 JAMIN	97	THEO
$4.16 \pm 0.32 \pm 0.60$	$4.63 \pm 0.36 \pm 0.67$	34 RODRIGO	97	THEO

¹ ABDALLAH 06D determine $m_b(M_Z) = 2.85 \pm 0.32$ GeV from Z -decay three-jet events containing a b -quark. We have converted this to $\bar{m}_b(\bar{m}_b)$ and m_b^{1S} .

² BOUGHEZAL 06 $\overline{\text{MS}}$ scheme result comes from the first moment of the hadronic production cross-section to order α_s^3 . We have converted it to the 1S scheme.

³ PINEDA 06 $\overline{\text{MS}}$ scheme result comes from a partial NNLL evaluation (complete at NNLO) of sum rules of the bottom production cross-section in e^+e^- annihilation. We have converted it to the 1S scheme.

⁴ GRAY 05 determines $\bar{m}_b(\bar{m}_b)$ from a lattice computation of the γ spectrum. The simulations have 2+1 dynamical light flavors. The b quark is implemented using NRQCD.

⁵ We have converted m_b to the 1S scheme.

⁶ AUBERT 04X obtain m_b from a fit to the hadron mass and lepton energy distributions in semileptonic B decay. The paper quotes values in the kinetic scheme. The $\overline{\text{MS}}$ value has been provided by the BABAR collaboration, and we have converted this to the 1S scheme.

⁷ BAUER 04 determine m_b , m_c and $m_b - m_c$ by a global fit to inclusive B decay spectra.

⁸ HOANG 04 determines m_b (\bar{m}_b) from moments at order α_s^2 of the bottom production cross-section in e^+e^- annihilation.

⁹ MCNEILE 04 use lattice QCD with dynamical light quarks and a static heavy quark to compute the masses of heavy-light mesons.

¹⁰ BAUER 03 determine the b quark mass by a global fit to B decay observables. The experimental data includes lepton energy and hadron invariant mass moments in semileptonic $B \rightarrow X_c \ell \nu_\ell$ decay, and the inclusive photon spectrum in $B \rightarrow X_s \gamma$ decay. The theoretical expressions used are of order $1/m^3$, and $\alpha_s^2 \beta_0$.

¹¹ BORDES 03 determines m_b using QCD finite energy sum rules to order α_s^2 .

¹² CORCELLA 03 determines \bar{m}_b using sum rules computed to order α_s^2 . Includes charm quark mass effects.

¹³ DEDIVITIIS 03 use a quenched lattice computation of heavy-heavy and heavy-light meson masses.

¹⁴ EIDEMULLER 03 determines \bar{m}_b and \bar{m}_c using QCD sum rules.

¹⁵ ERLER 03 determines \bar{m}_b and \bar{m}_c using QCD sum rules. Includes recent BES data.

¹⁶ MAHMOOD 03 determines m_b^{1S} by a fit to the lepton energy moments in $B \rightarrow X_c \ell \nu_\ell$ decay. The theoretical expressions used are of order $1/m^3$ and $\alpha_s^2 \beta_0$. We have converted their result to the $\overline{\text{MS}}$ scheme.

¹⁷ PENIN 02 determines \bar{m}_b from the spectrum of the γ system.

¹⁸ ABBIENDI 01S find $\bar{m}_b(M_Z)$ to be 2.67 ± 0.4 GeV from an analysis of $Z \rightarrow b$ decays.

¹⁹ KUHN 01 uses an analysis of the e^+e^- total cross section to hadrons.

²⁰ NARISON 01B uses pseudoscalar sum rules in the B and D meson channels.

²¹ PINEDA 01 uses the $\gamma(1S)$ system to determine the quark mass. The errors are due to theory, and the uncertainty in α_s .

²² BARATE 00V obtain the b quark mass $\bar{m}_b(M_Z) = 3.27 \pm 0.22(\text{stat}) \pm 0.22(\text{exp}) \pm 0.38(\text{had}) \pm 0.16(\text{thy})$ from an analysis of event shape variables in Z decays. We have converted this to $\mu = \bar{m}_b$.

²³ HOANG 00 uses a NNLO calculation of the vacuum polarization function to determine spectral moments of the masses and electronic decay widths of the γ mesons.

- ²⁴ LUCHA 00, PINEDA 00 obtain the b -quark mass from a perturbative calculation of the γ spectrum and decay widths to order α_s^4 .
- ²⁵ BENEKE 99 uses a calculation of the $b\bar{b}$ production cross section and the mass of the γ meson at NNLO.
- ²⁶ BRANDENBURG 99 obtain a b -quark mass of $\overline{m}_b(M_Z) = 2.56 \pm 0.27^{+0.28+0.49}_{-0.38-1.48}$ from a study of three-jet events at the Z . We have converted this to $\mu = \overline{m}_b$.
- ²⁷ HOANG 99 uses a NNLO calculation of the vacuum polarization function to determine spectral moments of the masses and electronic decay widths of the γ mesons.
- ²⁸ MELNIKOV 99 compute the quark mass using γ sum rules at NNLO.
- ²⁹ PENIN 99 compute the quark mass using γ sum rules at NNLO.
- ³⁰ ABREU 98I determines the $\overline{\text{MS}}$ mass $\overline{m}_b = 2.67 \pm 0.25 \pm 0.34 \pm 0.27$ GeV at $\mu = M_Z$ from three jet heavy quark production at LEP. ABREU 98I have rescaled the result to $\mu = \overline{m}_b$ using $\alpha_s = 0.118 \pm 0.003$.
- ³¹ KUEHN 98 uses a calculation of the vacuum polarization function, including resumming threshold effects, to determine spectral moments of the masses of the γ mesons. We have converted their extracted value of 4.75 ± 0.04 for the pole mass to the $\overline{\text{MS}}$ scheme.
- ³² GIMENEZ 97 uses lattice computations of the B -meson propagator and the B -meson binding energy Λ in the HQET. Their systematic (second) error for the $\overline{\text{MS}}$ mass is an estimate of the effects of higher-order corrections in the matching of the HQET operators (renormalon effects).
- ³³ JAMIN 97 apply the QCD moment method to the γ system. They also find a pole mass of 4.60 ± 0.02 .
- ³⁴ RODRIGO 97 determines the $\overline{\text{MS}}$ mass $\overline{m}_b = 2.85 \pm 0.22 \pm 0.20 \pm 0.36$ GeV at $\mu = M_Z$ from three jet heavy quark production at LEP. We have rescaled the result.

***b*-QUARK REFERENCES**

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