

Extra Dimensions

For explanation of terms used and discussion of significant model dependence of following limits, see the “Extra Dimensions Review.” Limits are expressed in conventions of of Giudice, Rattazzi, and Wells as explained in the Review. Footnotes describe originally quoted limit. n indicates the number of extra dimensions.

Limits not encoded here are summarized in the “Extra Dimensions Review.”

EXTRA DIMENSIONS

Written December 2005 by G.F. Giudice (CERN) and J.D. Wells (MCTP/Michigan).

I Introduction

The idea of using extra spatial dimensions to unify different forces started in 1914 with Nordstöm, who proposed a 5-dimensional vector theory to simultaneously describe electromagnetism and a scalar version of gravity. After the invention of general relativity, in 1919 Kaluza noticed that the 5-dimensional generalization of Einstein theory can simultaneously describe gravitational and electromagnetic interactions. The role of gauge invariance and the physical meaning of the compactification of extra dimensions was elucidated by Klein. However, the Kaluza-Klein (KK) theory failed in its original purpose because of internal inconsistencies and was essentially abandoned until the advent of supergravity in the late 70's. Higher-dimensional theories were reintroduced in physics to exploit the special properties that supergravity and superstring theories possess for particular values of space-time dimensions. More recently it was realized [1,2] that extra dimensions with a fundamental scale of order TeV^{-1} could address the M_W - M_{Pl} hierarchy problem and therefore have direct implications for collider experiments. Here we will review [3] the proposed scenarios with experimentally accessible extra dimensions.

II Gravity in Flat Extra Dimensions

II.1 Theoretical Setup

Following ref. [1], let us consider a D -dimensional spacetime with $D = 4 + \delta$, where δ is the number of extra spatial dimensions. The space is factorized into $R^4 \times M_\delta$ (meaning that the 4-dimensional part of the metric does not depend on extra-dimensional coordinates), where M_δ is a δ -dimensional compact space with finite volume V_δ . For concreteness, we will consider a δ -dimensional torus of radius R , for which $V_\delta = (2\pi R)^\delta$. Standard Model (SM) fields are assumed to be localized on a $(3 + 1)$ -dimensional subspace. This assumption can be realized in field theory, but it is most natural [4] in the setting of string theory, where gauge and matter fields can be confined to live on “branes” (for a review see ref. [5]). On the other hand, gravity, which according to general relativity is described by the space-time geometry, extends to all D dimensions. The Einstein action takes the form

$$S_E = \frac{\bar{M}_D^{2+\delta}}{2} \int d^4x d^\delta y \sqrt{-\det g} \mathcal{R}(g), \quad (1)$$

where x and y describe ordinary and extra coordinates, respectively. The metric g , the scalar curvature \mathcal{R} , and the reduced Planck mass \bar{M}_D refer to the D -dimensional theory. The effective action for the 4-dimensional graviton is obtained by restricting the metric indices to 4 dimensions and by performing the integral in y . Because of the above-mentioned factorization hypothesis, the integral in y reduces to the volume V_δ and therefore the 4-dimensional reduced Planck mass is given by

$$\bar{M}_{\text{Pl}}^2 = \bar{M}_D^{2+\delta} V_\delta = \bar{M}_D^{2+\delta} (2\pi R)^\delta, \quad (2)$$

where $\bar{M}_{\text{Pl}} = M_{\text{Pl}}/\sqrt{8\pi} = 2.4 \times 10^{18}$ GeV. The same formula can be obtained from Gauss’s law in extra dimensions [6].

Following ref. [7], we will consider $M_D = (2\pi)^{\delta/(2+\delta)} \bar{M}_D$ as the fundamental D -dimensional Planck mass.

The key assumption of ref. [1] is that the hierarchy problem is solved because the truly fundamental scale of gravity M_D (and therefore the ultraviolet cut-off of field theory) lies around the TeV region. From Eq. (2) it follows that the correct value of \bar{M}_{Pl} can be obtained with a large value of RM_D . The inverse compactification radius is therefore given by

$$R^{-1} = M_D (M_D/\bar{M}_{\text{Pl}})^{2/\delta}, \quad (3)$$

which corresponds to 4×10^{-4} eV, 20 keV, 7 MeV for $M_D = 1$ TeV and $\delta = 2, 4, 6$, respectively. In this framework, gravity is weak because it is diluted in a large space ($R \gg M_D^{-1}$). Of course a complete solution of the hierarchy problem would require a dynamical explanation for the radius stabilization at a large value.

A D -dimensional bosonic field can be expanded in Fourier modes in the extra coordinates

$$\phi(x, y) = \sum_{\vec{n}} \frac{\varphi^{(\vec{n})}(x)}{\sqrt{V_\delta}} \exp\left(i \frac{\vec{n} \cdot \vec{y}}{R}\right). \quad (4)$$

The sum is discrete because of the finite size of the compactified space. The fields $\varphi^{(\vec{n})}$ are called the n^{th} KK excitations (or modes) of ϕ , and correspond to particles propagating in 4 dimensions with masses $m_{(\vec{n})}^2 = |\vec{n}|^2/R^2 + m_0^2$, where m_0 is the mass of the zero mode. The D -dimensional graviton can then be recast as a tower of KK states with increasing mass. However, since R^{-1} in Eq. (3) is smaller than the typical energy resolution in collider experiments, the mass distribution of KK gravitons is practically continuous.

Although each KK graviton has a purely gravitational coupling suppressed by \bar{M}_{Pl}^{-1} , inclusive processes in which we sum

over the large number of available gravitons have cross sections suppressed only by powers of M_D . Indeed, for scatterings with typical energy E , we expect $\sigma \sim E^\delta/M_D^{2+\delta}$, as evident from power-counting in D dimensions. Processes involving gravitons are therefore detectable in collider experiments if M_D is in the TeV region.

The astrophysical considerations described in sect. II.6 set very stringent bounds on M_D for $\delta < 4$, in some cases even ruling out the possibility of observing any signal at the LHC. However, these bounds disappear if there are no KK gravitons lighter than about 100 MeV. Variations of the original model exist [8,9] in which the light KK gravitons receive small extra contributions to their masses, sufficient to evade the astrophysical bounds. Notice that collider experiments are nearly insensitive to such modifications of the infrared part of the KK graviton spectrum, since they mostly probe the heavy graviton modes. Therefore, in the context of these variations, it is important to test at colliders extra-dimensional gravity also for low values of δ , and even for $\delta = 1$ [9]. In addition to these direct experimental constraints, the proposal of gravity in flat extra dimensions has dramatic cosmological consequences and requires a rethinking of the thermal history of the universe for temperatures as low as the MeV scale.

II.2 Collider Signals in Linearized Gravity

By making a derivative expansion of Einstein gravity, one can construct an effective theory describing KK graviton interactions, which is valid for energies much smaller than M_D [7,10,11]. With the aid of this effective theory, it is possible to make predictions for graviton-emission processes at colliders. Since the produced gravitons interact with matter only with rates suppressed by inverse powers of \bar{M}_{Pl} , they will

remain undetected leaving a “missing-energy” signature. Extra-dimensional gravitons have been searched for in the processes $e^+e^- \rightarrow \gamma \cancel{E}$ and $e^+e^- \rightarrow Z \cancel{E}$ at LEP, and $p\bar{p} \rightarrow \text{jet} + \cancel{E}_T$ and $p\bar{p} \rightarrow \gamma + \cancel{E}_T$ at the Tevatron. The combined LEP 95% CL limits are [12] $M_D > 1.60, 1.20, 0.94, 0.77, 0.66$ TeV for $\delta = 2, \dots, 6$ respectively. Experiments at the LHC will improve the sensitivity. However, the theoretical predictions for the graviton-emission rates should be applied with care to hadron machines. The effective theory results are valid only for center-of-mass energy of the parton collision much smaller than M_D .

The effective theory under consideration also contains the full set of higher-dimensional operators, whose coefficients are however not calculable, because they depend on the ultraviolet properties of gravity. This is in contrast with graviton emission, which is a calculable process within the effective theory because it is linked to the infrared properties of gravity. The higher-dimensional operators are the analogue of the contact interactions described in ref. [13]. Of particular interest is the dimension-8 operator mediated by tree-level graviton exchange [7,11,14]

$$\mathcal{L}_{\text{int}} = \pm \frac{4\pi}{\Lambda_T^4} \mathcal{T}, \quad \mathcal{T} = \frac{1}{2} \left(T_{\mu\nu} T^{\mu\nu} - \frac{1}{\delta + 2} T_\mu^\mu T_\nu^\nu \right), \quad (5)$$

where $T_{\mu\nu}$ is the energy momentum tensor. (There exist several alternate definitions in the literature for the cutoff in Eq. (5) including M_{TT} used in the Listings, where $M_{TT}^4 = (2/\pi)\Lambda_T^4$.) This operator gives anomalous contributions to many high-energy processes. The 95% CL limit from Bhabha scattering and diphoton production at LEP is [15] $\Lambda_T > 1.29$ (1.12) TeV for constructive (destructive) interference, corresponding to the

\pm signs in Eq. (5). The analogous limit from Drell-Yan and diphotons at Tevatron is [16] $\Lambda_T > 1.43$ (1.27) TeV.

Graviton loops can be even more important than tree-level exchange, because they can generate operators of dimension lower than 8. For simple graviton loops, there is only one dimension-6 operator that can be generated (excluding Higgs fields in the external legs) [18,19],

$$\mathcal{L}_{\text{int}} = \pm \frac{4\pi}{\Lambda_\Upsilon^2} \Upsilon, \quad \Upsilon = \frac{1}{2} \left(\sum_{f=q,\ell} \bar{f} \gamma_\mu \gamma_5 f \right)^2. \quad (6)$$

Here the sum extends over all quarks and leptons in the theory. The 95% CL combined LEP limit [20] from lepton-pair processes is $\Lambda_\Upsilon > 17.2$ (15.1) TeV for constructive (destructive) interference, and $\Lambda_\Upsilon > 15.3$ (11.5) TeV is obtained from $\bar{b}b$ production. Limits from graviton emission and effective operators cannot be compared in a model-independent way, unless one introduces some well-defined cutoff procedure (see, *e.g.* ref. [19])

II.3 The Transplanckian Regime

The use of linearized Einstein gravity, discussed in sect. II.2, is valid for processes with typical center-of-mass energy $\sqrt{s} \ll M_D$. The physics at $\sqrt{s} \sim M_D$ can be described only with knowledge of the underlying quantum-gravity theory. Toy models have been used to mimic possible effects of string theory at colliders [21]. Once we access the transplanckian region $\sqrt{s} \gg M_D$, a semiclassical description of the scattering process becomes adequate. Indeed, in the transplanckian limit, the Schwarzschild radius for a colliding system with center-of-mass energy \sqrt{s} in $D = 4 + \delta$ dimensions,

$$R_S = \left[\frac{2^\delta \pi^{(\delta-3)/2}}{\delta + 2} \Gamma\left(\frac{\delta + 3}{2}\right) \frac{\sqrt{s}}{M_D^{\delta+2}} \right]^{1/(\delta+1)}, \quad (7)$$

is larger than the D -dimensional Planck length M_D^{-1} . Therefore, quantum-gravity effects are subleading with respect to classical gravitational effects (described by R_S).

If the impact parameter b of the process satisfies $b \gg R_S$, the transplanckian collision is determined by linear semiclassical gravitational scattering. The corresponding cross sections have been computed [22] in the eikonal approximation, valid in the limit of small deflection angle. The collider signal at the LHC is a dijet final state, with features characteristic of gravity in extra dimensions.

When $b < R_S$, we expect gravitational collapse and black-hole formation [23,24] (see ref. [25] and references therein). The black-hole production cross section is estimated to be of order the geometric area $\sigma \sim \pi R_S^2$. This estimate has large uncertainties due, for instance, to the unknown amount of gravitational radiation emitted during collapse. Nevertheless, for M_D close to the weak scale, the black-hole production rate at the LHC is large. For example, the production cross section of 6 TeV black holes is about 10 pb, for $M_D = 1.5$ TeV. The produced black-hole emits thermal radiation with Hawking temperature $T_H = (\delta + 1)/(4\pi R_S)$ until it reaches the Planck phase (where quantum-gravity effects become important). A black hole of initial mass M_{BH} completely evaporates with lifetime $\tau \sim M_{BH}^{(\delta+3)/(\delta+1)} / M_D^{2(\delta+2)/(\delta+1)}$, which typically is 10^{-26} – 10^{-27} s for $M_D = 1$ TeV. The black hole can be easily detected because it emits a significant fraction of visible (*i.e.* non-gravitational) radiation, although the precise amount is not known in the general case of D dimensions. Computations exist [26] for the grey-body factors, which describe the distortion of the emitted radiation from pure black-body caused by the strong gravitational background field.

To trust the semiclassical approximation, the typical energy of the process has to be much larger than M_D . Given the present constraints on extra-dimensional gravity, it is clear that the maximum energy available at the LHC allows, at best, to only marginally access the transplanckian region. If gravitational scattering and black-hole production are observed at the LHC, it is likely that significant quantum-gravity (or string-theory) corrections will affect the semiclassical calculations or estimates. In the context of string theory, it is possible that the production of string-balls [27] dominates over black holes.

If M_D is around the TeV scale, transplanckian collisions would regularly occur in the interaction of high-energy cosmic rays with the earth's atmosphere and could be observed in present and future cosmic ray experiments [28,29].

II.4 Graviscalars

After compactification, the D -dimensional graviton contains KK towers of spin-2 gravitational states (as discussed above), of spin-1 “graviphoton” states, and of spin-0 “graviscalar” states. In most processes, the graviphotons and graviscalars are much less important than their spin-2 counterparts. A single graviscalar tower is coupled to SM fields through the trace of the energy momentum tensor. The resulting coupling is however very weak for SM particles with small masses.

Perhaps the most accessible probe of the graviscalars would be through their allowed mixing with the Higgs boson [30] in the induced curvature-Higgs term of the 4-dimensional action. This can be recast as a contribution to the decay width of the SM Higgs boson into an invisible channel. Although the invisible branching fraction is a free parameter of the theory, it is more likely to be important when the SM Higgs boson width is particularly narrow ($m_H \lesssim 140$ GeV). The collider phenomenology

of invisibly decaying Higgs bosons investigated in the literature is applicable here (see ref. [31] and references therein).

II.5 Tests of the Gravitational Force Law

The theoretical developments in gravity with large extra dimensions have further stimulated interest in experiments looking for possible deviations from the gravitational inverse-square law (for a review, see ref. [32]) . Such deviations are usually parametrized by a modified newtonian potential of the form

$$V(r) = -G_N \frac{m_1 m_2}{r} [1 + \alpha \exp(-r/\lambda)] \quad (8)$$

The experimental limits on the parameters α and λ are summarized in fig. 1, taken from ref. [33].

For gravity with δ extra dimensions, in the case of toroidal compactifications, the parameter α is given by $\alpha = 8 \delta/3$ and λ is the Compton wavelength of the first graviton Kaluza-Klein mode, equal to the radius R . From the results shown in fig. 1, one finds $R < 130$ (160) μm at 95% CL for $\delta = 2$ (1) which, using Eq. (3), becomes $M_D > 1.9$ TeV for $\delta = 2$. This bound is weaker than the astrophysical bounds discussed in sect. II.6, which actually exclude the occurrence of any visible signal in planned tests of Newton's law. However, in the context of higher-dimensional theories, other particles like light gauge bosons, moduli or radions could mediate detectable modifications of Newton's law, without running up against the astrophysical limits.

II.6 Astrophysical Bounds

Because of the existence of the light and weakly-coupled KK gravitons, gravity in extra dimensions is strongly constrained by several astrophysical considerations (see ref. [34] and references therein). The requirement that KK gravitons do not carry away more than half of the energy emitted by the supernova

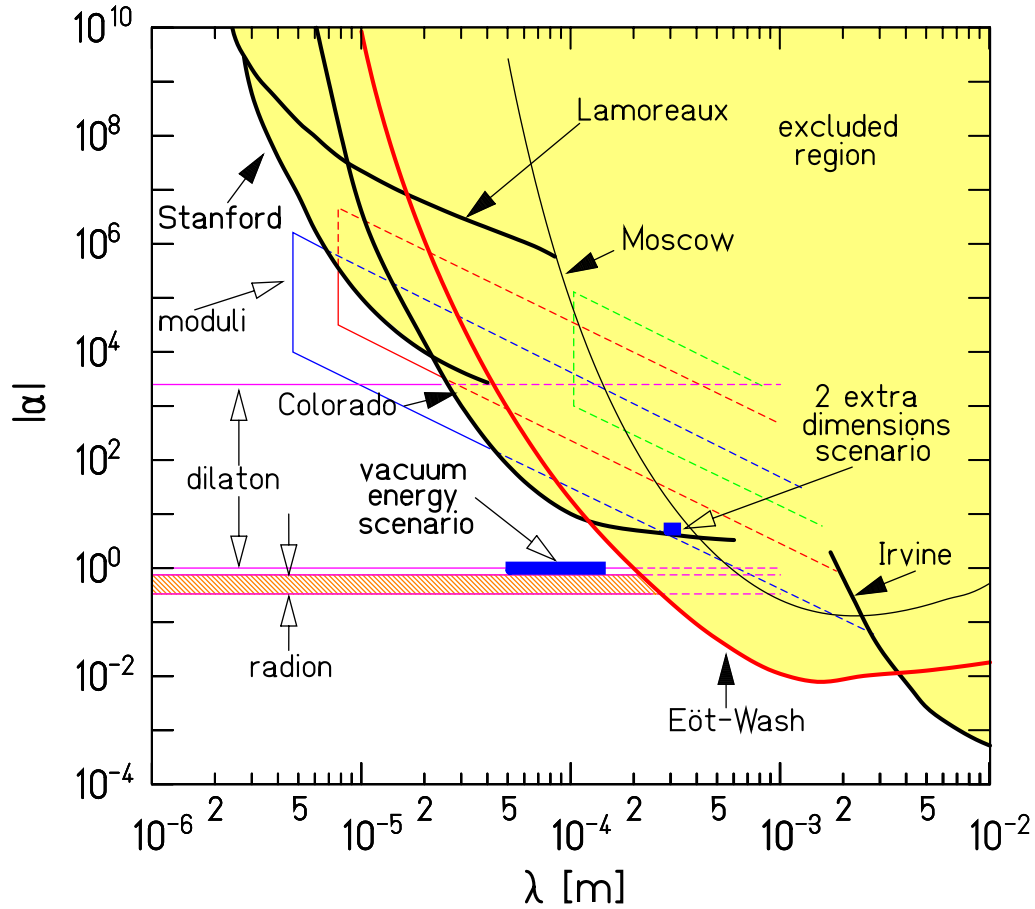


Figure 1: Experimental limits on α and λ of Eq. (8), which parametrize deviations from Newton's law. From ref. [33]. See full-color version on color pages at end of book.

SN1987A gives the bounds [35] $M_D > 14$ (1.6) TeV for $\delta = 2$ (3). KK gravitons produced by all supernovæ in the universe lead to a diffuse γ ray background generated by the graviton decays into photons. Measurements by the EGRET satellite imply [36] $M_D > 38$ (4.1) TeV for $\delta = 2$ (3). Most of the KK gravitons emitted by supernova remnants and neutron stars are gravitationally trapped. The gravitons forming this

halo occasionally decay, emitting photons. Limits on γ rays from neutron-star sources imply [34] $M_D > 200$ (16) TeV for $\delta = 2$ (3). The decay products of the gravitons forming the halo can hit the surface of the neutron star, providing a heat source. The low measured luminosities of some pulsars imply [34] $M_D > 750$ (35) TeV for $\delta = 2$ (3). These bounds are valid only if the graviton KK mass spectrum below about 100 MeV is not modified by distortions of the compactification space (see sect. II.1).

III Gravity in Warped Extra Dimensions

III.1 Theoretical Setup

In the proposal of ref. [2], the M_W - M_{Pl} hierarchy is explained using an extra-dimensional analogy of the classical gravitational redshift in curved space, as we illustrate below. The setup consists of a 5-dimensional space in which the fifth dimension is compactified on S^1/Z_2 , *i.e.* a circle projected into a segment by identifying points of the circle opposite with respect to a given diameter. Each end-point of the segment (the “fixed-points” of the orbifold projection) is the location of a 3-dimensional brane. The two branes have equal but opposite tensions. We will refer to the negative-tension brane as the infrared (IR) brane, where SM fields are assumed to be localized, and the positive-tension brane as the ultraviolet (UV) brane. The bulk cosmological constant is fine-tuned such that the effective cosmological constant in the 3-dimensional space exactly cancels.

The solution of the Einstein equation in vacuum gives the metric corresponding to the line element

$$ds^2 = \exp(-2k|y|) \eta_{\mu\nu} dx^\mu dx^\nu - dy^2. \quad (9)$$

Here y is the 5th coordinate, with the UV and IR branes located at $y = 0$ and $y = \pi R$, respectively; R is the compactification radius and k is the AdS curvature. The 4-dimensional metric in Eq. (9) is modified with respect to the flat Minkowski metric $\eta_{\mu\nu}$ by the factor $\exp(-2k|y|)$. This shows that the 5-dimensional space is not factorized, meaning that the 4-dimensional metric depends on the extra-dimensional coordinate y . This feature is key to the desired effect.

As is known from general relativity, the energy of a particle travelling through a gravitational field is redshifted by an amount proportional to $|g_{00}|^{-1/2}$, where g_{00} is the time-component of the metric. Analogously, energies (or masses) viewed on the IR brane ($y = \pi R$) are red-shifted with respect to their values at the UV brane ($y = 0$) by an amount equal to the warp factor $\exp(-\pi k R)$, as shown by Eq. (9):

$$m_{IR} = m_{UV} \exp(-\pi k R). \quad (10)$$

A mass $m_{UV} \sim \mathcal{O}(\bar{M}_{\text{Pl}})$ on the UV brane corresponds to a mass on the IR brane with a value $m_{IR} \sim \mathcal{O}(M_{\text{W}})$, if $R \simeq 12k^{-1}$. A radius moderately larger than the fundamental scale k is therefore sufficient to reproduce the large hierarchy between the Planck and Fermi scales. A simple and elegant mechanism to stabilize the radius exists [38], by adding a scalar particle with a bulk mass and different potential terms on the two branes.

The effective theory describing the interaction of the KK modes of the graviton is characterized by two mass parameters, which we take to be m_1 and Λ_π . Both are a warp-factor smaller than the UV scale, and therefore they are naturally of order the weak scale. The parameter m_1 is the mass of the first KK

graviton mode, from which the mass m_n of the generic n^{th} mode is determined,

$$m_n = \frac{x_n}{x_1} m_1. \quad (11)$$

Here x_n is the n^{th} root of the Bessel function J_1 ($x_1 = 3.83$, $x_2 = 7.02$ and, for large n , $x_n = (n + 1/4)\pi$). The parameter Λ_π determines the strength of the coupling of the KK gravitons $h_{\mu\nu}^{(n)}$ with the energy momentum tensor $T_{\mu\nu}$,

$$\mathcal{L} = -\frac{T^{\mu\nu}}{M_{\text{Pl}}} h_{\mu\nu}^{(0)} - \frac{T^{\mu\nu}}{\Lambda_\pi} \sum_{n=1}^{\infty} h_{\mu\nu}^{(n)}. \quad (12)$$

In the approach discussed in sect. II.1, M_{Pl} appears to us much larger than the weak scale because gravity is diluted in a large space. In the approach described in this section, the explanation lies instead in the non-trivial configuration of the gravitational field: the zero-mode graviton wavefunction is peaked around the UV brane and it has an exponentially small overlap with the IR brane where we live. The extra dimensions discussed in sect. II.1 are large and “nearly flat”; the graviton excitations are very weakly coupled and have a mass gap that is negligibly small in collider experiments. Here, instead, the gravitons have a mass gap of $\sim \text{TeV}$ size and become strongly-coupled at the weak scale.

III.2 Collider Signals

The KK excitations of the graviton, possibly being of order the TeV scale, are subject to experimental discovery at high-energy colliders. As discussed above, KK graviton production cross-sections and decay widths are set by the first KK mass m_1 and the graviton-matter interaction scale Λ_π . Some studies use m_1 and k as the independent parameters, and so it is helpful

to keep in mind that the relationships between all of these parameters are

$$\frac{m_n}{\Lambda_\pi} = \frac{kx_n}{\bar{M}_{\text{Pl}}}, \quad \Lambda_\pi = \bar{M}_{\text{Pl}} \exp(-\pi kR), \quad (13)$$

where again the x_n values are the zeros of the J_1 Bessel function. Resonant and on-shell production of the n^{th} KK gravitons leads to characteristic peaks in the dilepton and diphoton invariant-mass spectra and it is probed at colliders for $\sqrt{s} \geq m_n$. Current limits from dimuon, dielectron, and diphoton channels at CDF and DØ give the 95% CL limits $\Lambda_\pi > 4.3(2.6)$ TeV for $m_1 = 500(700)$ GeV [16,17].

Contact interactions arising from integrating out heavy KK modes of the graviton generate the dimension-8 operator \mathcal{T} , analogous to the one in Eq. (5) in the flat extra dimensions case. Although searches for effects of these non-renormalizable operators cannot confirm directly the existence of a heavy spin-2 state, they nevertheless provide a good probe of the model [39,40].

Searches for direct production of KK excitations of the graviton and contact interactions induced by gravity in compact extra-dimensional warped space can continue at the LHC. With the large increase in energy, one expects prime regions of the parameter space up to $m_n, \Lambda_\pi \sim 10$ TeV [39] to be probed.

If SM states are in the AdS bulk, KK graviton phenomenology becomes much more model dependent. Present limits and future collider probes of the masses and interaction strengths of the KK gravitons to matter fields are significantly reduced [41] in some circumstances, and each specific model of SM fields in the AdS bulk should be analyzed on a case-by-case basis.

For warped metrics, black-hole production is analogous the case discussed in sect. II.3, as long the radius of the black hole is

smaller than the AdS radius $1/k$, when the space is effectively flat. For heavier black holes, the production cross section is expected to grow with energy only as $\log^2 E$, saturating the Froissart bound [37].

III.3 The Radion

The size of the warped extra-dimensional space is controlled by the value of the radion, a scalar field corresponding to an overall dilatation of the extra coordinates. Stabilizing the radion is required for a viable theory, and known stabilization mechanisms often imply that the radion is less massive than the KK excitations of the graviton [38], thus making it perhaps the lightest beyond-the-SM particle in this scenario.

The coupling of the radion r to matter is $\mathcal{L} = -rT/\Lambda_\varphi$, where T is the trace of the energy momentum tensor and $\Lambda_\varphi = \sqrt{24}\Lambda_\pi$ is expected to be near the weak scale. The relative couplings of r to the SM fields are similar to, but not exactly the same as those of the Higgs boson. The partial widths are generally smaller by a factor of v/Λ_φ compared to SM Higgs decay widths, where $v = 246$ GeV is the vacuum expectation value of the SM Higgs doublet. On the other hand, the trace anomaly that arises in the SM gauge groups by virtue of quantum effects enhances the couplings of the radion to gluons and photons over the naive v/Λ_φ rescaling of the Higgs couplings to these same particles. Thus, for example, one finds that the radion's large coupling to gluons [30,43] enables a sizeable cross section even for Λ_φ large compared to m_W .

Another subtlety of the radion is its ability to mix with the Higgs boson through the curvature-scalar interaction [30],

$$S_{mix} = -\xi \int d^4x \sqrt{-\det g_{\text{ind}}} R(g_{\text{ind}}) H^+ H \quad (14)$$

where g_{ind} is the four-dimensional induced metric. With $\xi \neq 0$, there is neither pure Higgs boson nor pure radion mass eigenstate. Mixing between states enables decays of the heavier eigenstate into lighter eigenstates if kinematically allowed. Overall, the production cross sections, widths and relative branching fractions can all be affected significantly by the value of the mixing parameter ξ [30,42,43,44]. Despite the various permutations of couplings and branching fractions that the radion and the Higgs-radion mixed states can have into SM particles, the search strategies for these particles at high-energy colliders are similar to those of the SM Higgs boson.

IV Standard Model Fields in Flat Extra Dimensions

IV.1 TeV-Scale Compactification

Not only gravity, but also SM fields could live in an experimentally accessible higher-dimensional space [45]. This hypothesis could lead to unification of gauge couplings at a low scale [46]. In contrast with gravity, these extra dimensions must be at least as small as about TeV^{-1} in order to avoid incompatibility with experiment. The canonical extra-dimensional space of this type is a 5th dimension compactified on the interval S^1/Z_2 , where again the radius of the S^1 is denoted R , and the Z_2 symmetry identifies $y \leftrightarrow -y$ of the extra-dimensional coordinate. The two fixed points $y = 0$ and $y = \pi R$ define the end-points of the compactification interval.

Let us first consider the case in which gauge fields live in extra dimensions, while matter and Higgs fields are confined to a 3-brane. The masses M_n of the gauge-boson KK excitations are related to the masses M_0 of the zero-mode normal gauge bosons by

$$M_n^2 = M_0^2 + \frac{n^2}{R^2}. \quad (15)$$

The KK excitations of the vector bosons have couplings to matter a factor of $\sqrt{2}$ larger than the zero modes ($g_n = \sqrt{2}g$). Therefore, if the first KK excitation is \sim TeV, tree-level virtual effects of the KK gauge bosons can have a significant effect on precision electroweak observables and high-energy processes such as $e^+e^- \rightarrow f\bar{f}$. In this theory one expects that observables will be shifted with respect to their SM value by an amount proportional to [47]

$$V = 2 \sum_n \left(\frac{g_n^2}{g^2} \right) \frac{M_Z^2 R^2}{n^2} \sim \frac{2}{3} \pi^2 M_Z^2 R^2 \quad (16)$$

More complicated compactifications lead to more complicated representations of V . A global fit to all relevant observables, including precision electroweak data, Tevatron, HERA and LEP2 results, shows that $R^{-1} \gtrsim 6.8$ TeV is required [48,49]. The LHC with 100 pb^{-1} integrated luminosity would be able to search nearly as high as $R^{-1} \sim 16$ TeV [48].

Fermions can also be promoted to live in the extra dimensions. Although fermions are vector-like in 5-dimension, chiral states in 4-dimensions can be obtained by using the Z_2 symmetry of the orbifold. An interesting possibility to explain the observed spectrum of quark and lepton masses is to assume that different fermions are localized in different points of the extra dimension. Their different overlap with the Higgs wavefunction can generate a hierarchical structure of Yukawa couplings [50], although there are strong bounds on the non-universal couplings of fermions to the KK gauge bosons from flavor-violating processes [51].

The case in which all SM particles uniformly propagate in the bulk of an extra-dimensional space is referred to as Universal Extra Dimensions (UED) [52]. The absence of a reference brane that breaks translation invariance in the extra dimensional

direction implies extra-dimensional momentum conservation. After compactification and after inclusion of boundary terms at the fixed points, the conservation law preserves only a discrete Z_2 parity (called KK-parity). The KK-parity of the n^{th} KK mode of each particle is $(-1)^n$. Thus, in UED, the first KK excitations can only be pair-produced and their virtual effect comes only from loop corrections. Therefore the ability to search for and constrain parameter space is diminished. The result is that for one extra dimension the limit on R^{-1} is between 300 and 500 GeV depending on the Higgs mass [53].

Because of KK-parity conservation, the lightest KK state is stable. Thus, one interesting consequence of UED is the possibility of the lightest KK state comprising the dark matter. After including radiative corrections [54], it is found that the lightest KK state is the first excitation of the hypercharge gauge boson $B^{(1)}$. It can constitute the cold dark matter of the universe if its mass is approximately 600 GeV [55], well above current collider limits. The LHC should be able to probe UED up to $R^{-1} \sim 1.5$ TeV [56], and thus possibly confirm the UED dark matter scenario.

An interesting and ambitious approach is to use extra dimensions to explain the hierarchy problem through Higgs-gauge unification [57]. The SM Higgs doublet is interpreted as the extra-dimensional component of an extended gauge symmetry acting in more than four dimensions, and the weak scale is protected by the extra-dimensional gauge symmetry. There are several obstacles to make this proposal fully realistic, but ongoing research is trying to overcome them.

IV.2 Grand Unification in Extra Dimensions

Extra dimensions offer a simple and elegant way to break GUT symmetries [58] by appropriate field boundary conditions

in compactifications on orbifolds. In this case the size of the relevant extra dimensions is much smaller than what has been considered so far, with compactification radii that are typically $\mathcal{O}(M_{\text{GUT}})$. This approach has several attractive features (for a review, see ref. [59]) . The doublet-triplet splitting problem [60] is solved by projecting out the unwanted light Higgs triplet in the compactification. In the same way one can eliminate the dangerous supersymmetric $d = 5$ proton-decay operators, or even forbid proton decay [61]. However, the prospects for proton-decay searches are not necessarily bleak. Because of the effect of the KK modes, the unification scale can be lowered to 10^{14} – 10^{15} GeV, enhancing the effect of $d = 6$ operators. The prediction for the proton lifetime is model-dependent.

V Standard Model Fields in Warped Extra Dimensions

V.1 Extra Dimensions and Strong Dynamics at the Weak Scale

In the original warped model of ref. [2], all SM fields are confined on the IR brane, although to solve the hierarchy problem it is sufficient that only the Higgs field lives on the brane. The variation in which SM fermions and gauge bosons are bulk fields is interesting because it links warped extra dimensions to technicolor-like models with strong dynamics at the weak scale. This connection comes from the AdS/CFT correspondence [62], which relates the properties of AdS₅, 5-dimensional gravity with negative cosmological constant, to a strongly-coupled 4-dimensional conformal field theory (CFT). In the correspondence, the motion along the 5th dimension is interpreted as the renormalization-group flow of the 4-dimensional theory, with the UV brane playing the role of the Planck-mass cutoff and the IR brane as the breaking of the conformal invariance. Local gauge symmetries acting on the bulk of AdS₅

correspond to global symmetries of the 4-dimensional theory. The original warped model of ref. [2] is then reinterpreted as an “almost CFT,” whose couplings run very slowly with the renormalization scale until the TeV scale is reached, where the theory develops a mass gap. In the variation in which SM fields, other than the Higgs, are promoted to the bulk, these fields correspond to elementary particles coupled to the CFT. Around the TeV scale the theory becomes strongly-interacting, producing a composite Higgs, which breaks electroweak symmetry. Notice the similarity with walking technicolour [63].

The most basic version of this theory is in conflict with electroweak precision measurements. To reduce the contribution to the ρ parameter, it is necessary to introduce an approximate global symmetry, a custodial $SU(2)$ under which the generators of $SU(2)_L$ transform as a triplet. Using the AdS/CFT correspondence, this requires the extension of the electroweak gauge symmetry to $SU(2)_L \times SU(2)_R \times U(1)$ in the bulk of the 5-dimensional theory [64]. Models along these lines have been constructed. The composite Higgs can be lighter than the strongly-interacting scale in models in which it is a pseudo-Goldstone boson [65]. Nevertheless, electroweak data provide strong constraints on such models.

When SM fermions are promoted to 5 dimensions, they become non-chiral and can acquire a bulk mass. The fermions are localized in different positions along the 5th dimension, with an exponential dependence on the value of the bulk mass (in units of the AdS curvature). Since the masses of the ordinary zero-mode SM fermions depend on their wavefunction overlap with the Higgs (localized on the IR brane), large hierarchies in the mass spectrum of quarks and leptons can be obtained from order-unity variations of the bulk masses [66]. This mechanism

can potentially explain the fermion mass pattern, and it can lead to new effects in flavour-changing processes, especially those involving the third-generation quarks [67]. The smallness of neutrino masses can also be explained, if right-handed neutrinos propagate in the bulk [68].

V.2 Higgsless Models

Extra dimensions offer new possibilities for breaking gauge symmetries. Even in the absence of physical scalars, electroweak symmetry can be broken by field boundary conditions on compactified spaces. The lightest KK modes of the gauge bosons corresponding to broken generators acquire masses equal to R^{-1} , the inverse of the compactification radius, now to be identified with M_W . In the ordinary 4-dimensional case, the SM without a Higgs boson violates unitarity at energies $E \sim 4\pi M_W/g \sim 1$ TeV. On the other hand, in extra dimensions, the breaking of unitarity in the longitudinal- W scattering amplitudes is delayed because of the contribution of the heavy KK gauge-boson modes [69]. The largest effect is obtained for one extra dimension, where the violation of unitarity occurs around $E \sim 12\pi^2 M_W/g \sim 10$ TeV. This is conceivably a large enough scale to render the strong dynamics, which is eventually responsible for unitarization, invisible to the processes measured by LEP experiments.

These Higgsless models, in their minimal version, are inconsistent with observations, because they predict new W gauge bosons with masses nM_W (with $n \geq 2$ integers) [70]. Warping the 5th dimension has a double advantage [71]. The excited KK modes of the gauge bosons can all have masses in the TeV range, making them compatible with present collider limits. Also, by enlarging the bulk gauge symmetry to $SU(2)_L \times SU(2)_R \times U(1)$, one can obtain an approximate custodial symmetry, as described

above, to tame tree-level corrections to ρ . If quarks and leptons are extended to the bulk, they can obtain masses through the electroweak-breaking effect on the boundaries. However at present, there is no model that reproduces the top quark mass and is totally consistent with electroweak data [72].

VI. Supersymmetry in Extra Dimensions

Extra dimensions have a natural home within string theory. Similarly, string theory and supersymmetry are closely connected, as the latter is implied by the former in most constructions. Coexistence between extra dimensions and supersymmetry is often considered a starting point for string model building. From a low-energy model-building point of view, perhaps the most compelling reason to introduce extra dimensions with supersymmetry lies in the mechanism of supersymmetry breaking.

When the field periodic boundary conditions on the compactified space are twisted using an R -symmetry, different zero modes for bosons and fermions are projected out and supersymmetry is broken. This is known as the Scherk-Schwarz mechanism of supersymmetry breaking [73]. In the simplest approach [74], a 5th dimension with $R^{-1} \sim 1 \text{ TeV}$ is introduced in which the non-chiral matter (gauge and Higgs multiplets) live. The chiral matter (quark and lepton multiplets) live on the three-dimensional spatial boundary. S^1/Z_2 compactification of the 5th dimension, which simultaneously employs the Scherk-Schwarz mechanism generates masses for the bulk fields (gauginos and higgsinos) of order R^{-1} . Boundary states (squarks and sleptons) get mass from loop corrections, and are parametrically smaller in value. The right-handed slepton is expected to be the lightest supersymmetric particle (LSP), which being charged is not a good dark matter candidate. Thus, this theory likely

requires R -parity violation in order to allow this charged LSP to decay and not cause cosmological problems.

By allowing all supersymmetric fields to propagate in the bulk of a $S_1/Z_2 \times Z'_2$ compactified space, it is possible to construct a model [75] with an interesting feature. Since supersymmetry is only broken non-locally, there are no quadratic divergences (except for a Fayet-Iliopoulos term [76]) and the Higgs mass is calculable. In the low-energy effective theory there is a single Higgs doublet, two superpartners for each SM particle, and the stop is the LSP, requiring a small amount of R -parity breaking.

Supersymmetry in warped space is also an interesting possibility. Again, one can consider [77] the case of chiral fields confined to our ordinary 3+1 dimensions, and gravity and gauge fields living in the 5-dimensional bulk space. Rather than being TeV^{-1} size, the 5th dimension is strongly warped to generate the supersymmetry-breaking scale. In this case, the tree-level mass of the gravitino is $\sim 10^{-3}$ eV and the masses of the gauginos are $\sim \text{TeV}$. The sleptons and squarks get mass at one loop from gauge interactions and thus are diagonal in flavor space, creating no additional FCNC problems. It has also been proposed [78] that an approximately supersymmetric Higgs sector confined on the IR brane could coexist with non-supersymmetric SM fields propagating in the bulk of the warped space.

In conclusion, we should reiterate that an important general consequence of extra dimensional theories is retained in supersymmetric extensions: KK excitations of the graviton and/or gauge fields are likely to be accessible at the LHC if the scale of compactification is directly related to solving the hierarchy problem. Any given extra-dimensional theory has many aspects to it, but we should keep in mind that the KK excitation

spectrum is the most generic and most robust aspect of the idea to test in experiments.

References

1. N. Arkani-Hamed *et al.*, Phys. Lett. **B429**, 263 (1998).
2. L. Randall and R. Sundrum, Phys. Rev. Lett. **83**, 3370 (1999).
3. For other reviews, see V. A. Rubakov, Phys. Usp. **44**, 871 (2001);
J. Hewett and M. Spiropulu, Ann. Rev. Nucl. and Part. Sci. **52**, 397 (2002);
R. Rattazzi, *Proc. of Cargese School of Particle Physics and Cosmology*, Corsica, France, 4-16 Aug 2003;
C. Csaki, [hep-ph/0404096](#);
R. Sundrum, [hep-th/0508134](#).
4. I. Antoniadis *et al.*, Phys. Lett. **B436**, 257 (1998).
5. J. Polchinski, “Lectures on D-branes,” [hep-th/9611050](#).
6. N. Arkani-Hamed *et al.*, Phys. Rev. **D59**, 086004 (1999).
7. G. F. Giudice *et al.*, Nucl. Phys. **B544**, 3 (1999).
8. N. Kaloper *et al.*, Phys. Rev. Lett. **85**, 928 (2000);
K. R. Dienes, Phys. Rev. Lett. **88**, 011601 (2002).
9. G. F. Giudice *et al.*, Nucl. Phys. **B706**, 455 (2005).
10. E. A. Mirabelli *et al.*, Phys. Rev. Lett. **82**, 2236 (1999).
11. T. Han *et al.*, Phys. Rev. **D59**, 105006 (1999).
12. LEP Exotica Working Group, LEP Exotica WG 2004-03.
13. K. Hagiwara *et al.*, “Searches for Quark and Lepton Compositeness,” in this *Review*.
14. J. L. Hewett, Phys. Rev. Lett. **82**, 4765 (1999).
15. D. Bourilkov, [hep-ex/0103039](#).
16. G. Landsberg [D0 and CDF Collaboration], [hep-ex/0412028](#).
17. V. M. Abazov *et al.* [D0 Collaboration], Phys. Rev. Lett. **95**, 091801 (2005).
18. R. Contino *et al.*, JHEP **106**, 005 (2001).

19. G. F. Giudice and A. Strumia, Nucl. Phys. **B663**, 377 (2003).
20. LEP Working Group LEP2FF/02-03.
21. E. Dudas and J. Mourad, Nucl. Phys. **B575**, 3 (2000);
S. Cullen *et al.*, Phys. Rev. **D62**, 055012 (2000);
P. Burikham *et al.*, Phys. Rev. **D71**, 016005 (2005);
[Erratum-*ibid.*, **71**, 019905 (2005)].
22. G. F. Giudice *et al.*, Nucl. Phys. **B630**, 293 (2002).
23. S. B. Giddings and S. Thomas, Phys. Rev. **D65**, 056010 (2002).
24. S. Dimopoulos and G. Landsberg, Phys. Rev. Lett. **87**, 161602 (2001).
25. P. Kanti, Int. J. Mod. Phys. **A19**, 4899 (2004).
26. P. Kanti and J. March-Russell, Phys. Rev. **D66**, 024023 (2002);
Phys. Rev. **D67**, 104019 (2003).
27. S. Dimopoulos and R. Emparan, Phys. Lett. **B526**, 393 (2002).
28. J. L. Feng and A. D. Shapere, Phys. Rev. Lett. **88**, 021303 (2002).
29. R. Emparan *et al.*, Phys. Rev. **D65**, 064023 (2002).
30. G. F. Giudice *et al.*, Nucl. Phys. **B595**, 250 (2001).
31. D. Dominici, hep-ph/0503216.
32. E. G. Adelberger *et al.*, Ann. Rev. Nucl. and Part. Sci. **53**, 77 (2003).
33. C. D. Hoyle *et al.*, Phys. Rev. **D70**, 042004 (2004).
34. S. Hannestad and G. G. Raffelt, Phys. Rev. Lett. **88**, 071301 (2002).
35. C. Hanhart *et al.*, Phys. Lett. **B509**, 1 (2002).
36. S. Hannestad and G. Raffelt, Phys. Rev. Lett. **87**, 051301 (2001).
37. S. B. Giddings, Phys. Rev. **D67**, 126001 (2003).
38. W. D. Goldberger and M. B. Wise, Phys. Rev. Lett. **83**, 4922 (1999).

39. H. Davoudiasl *et al.*, Phys. Rev. Lett. **84**, 2080 (2000).
40. K. Cheung, [hep-ph/0409028](#).
41. H. Davoudiasl *et al.*, Phys. Rev. **D63**, 075004 (2001).
42. C. Csaki *et al.*, Phys. Rev. **D63**, 065002 (2001).
43. D. Dominici *et al.*, Nucl. Phys. **B671**, 243 (2003).
44. K. Cheung *et al.*, Phys. Rev. **D69**, 075011 (2004).
45. I. Antoniadis, Phys. Lett. **B246**, 377 (1990).
46. K. R. Dienes *et al.*, Phys. Lett. **B436**, 55 (1998);
K. R. Dienes *et al.*, Nucl. Phys. **B537**, 47 (1999).
47. T. G. Rizzo and J. D. Wells, Phys. Rev. **D61**, 016007 (2000).
48. K. Cheung and G. Landsberg, Phys. Rev. **D65**, 076003 (2002).
49. R. Barbieri *et al.*, Nucl. Phys. **B703**, 127 (2004).
50. N. Arkani-Hamed and M. Schmaltz, Phys. Rev. **D61**, 033005 (2000).
51. A. Delgado *et al.*, JHEP **0001**, 030 (2000).
52. T. Appelquist *et al.*, Phys. Rev. **D64**, 035002 (2001).
53. T. Appelquist and H. U. Yee, Phys. Rev. **D67**, 055002 (2003).
54. H. C. Cheng *et al.*, Phys. Rev. **D66**, 036005 (2002).
55. G. Servant and T. M. P. Tait, Nucl. Phys. **B650**, 391 (2003);
F. Burnell and G. D. Kribs, [hep-ph/0509118](#);
K. Kong and K. T. Matchev, [hep-ph/0509119](#).
56. H. C. Cheng *et al.*, Phys. Rev. **D66**, 056006 (2002).
57. N. S. Manton, Nucl. Phys. **B158**, 141 (1979).
58. Y. Kawamura, Prog. Theor. Phys. **105**, 999 (2001).
59. L. J. Hall and Y. Nomura, Annals Phys. **306**, 132 (2003).
60. S. Raby, “Grand Unified Theories,” in this *Review*.
61. G. Altarelli and F. Feruglio, Phys. Lett. **B5111**, 257 (2001);
L. J. Hall and Y. Nomura, Phys. Rev. **D64**, 055003 (2001).

62. J. M. Maldacena, Adv. Theor. Math. Phys. **2**, 231 (1998) [Int. J. Theor. Phys. **38**, 1113 (1999)].
63. R.S. Chivukula *et al.*, “Technicolor,” in this *Review*.
64. K. Agashe *et al.*, JHEP **0308**, 050 (2003).
65. K. Agashe *et al.*, Nucl. Phys. **B719**, 165 (2005).
66. T. Gherghetta and A. Pomarol, Nucl. Phys. **B586**, 141 (2000);
S. J. Huber and Q. Shafi, Phys. Lett. **B498**, 256 (2001).
67. K. Agashe *et al.*, Phys. Rev. **D71**, 016002 (2005).
68. Y. Grossman and M. Neubert, Phys. Lett. **B474**, 361 (2000).
69. R. S. Chivukula *et al.*, Phys. Lett. **B525**, 175 (2002).
70. C. Csaki *et al.*, Phys. Rev. **D69**, 055006 (2004).
71. C. Csaki *et al.*, Phys. Rev. Lett. **92**, 101802 (2004).
72. R. Barbieri *et al.*, Phys. Lett. **B591**, 141 (2004);
G. Cacciapaglia *et al.*, Phys. Rev. **D70**, 075014 (2004).
73. J. Scherk and J. H. Schwarz, Phys. Lett. **B82**, 60 (1979).
74. A. Pomarol and M. Quiros, Phys. Lett. **B438**, 255 (1998);
A. Delgado *et al.*, Phys. Rev. **D60**, 095008 (1999).
75. R. Barbieri *et al.*, Phys. Rev. **D63**, 105007 (2001).
76. D. M. Ghilencea *et al.*, Nucl. Phys. **B619**, 385 (2001).
77. T. Gherghetta and A. Pomarol, Nucl. Phys. **B602**, 3 (2001).
78. T. Gherghetta and A. Pomarol, Phys. Rev. **D67**, 085018 (2003).

Limits on R from Deviations in Gravitational Force Law

This section includes limits on the size of extra dimensions from deviations in the Newtonian ($1/r^2$) gravitational force law at short distances. Deviations are parametrized by a gravitational potential of the form $V = -(G m m'/r) [1 + \alpha \exp(-r/R)]$. For δ toroidal extra dimensions of equal size, $\alpha = 8\delta/3$. Quoted bounds are for $\delta = 2$ unless otherwise noted.

VALUE (μm)	CL%	DOCUMENT ID	COMMENT
• • •			We do not use the following data for averages, fits, limits, etc. • • •
		¹ SMULLIN	05 Microcantilever

<130	95	2 HOYLE	04	Torsion pendulum
		3 CHIAVERINI	03	Microcantilever
\lesssim 200	95	4 LONG	03	Microcantilever
<190	95	5 HOYLE	01	Torsion pendulum
		6 HOSKINS	85	Torsion pendulum

¹ SMULLIN 05 search for new forces, and obtain bounds in the region with strengths $\alpha \simeq 10^3-10^8$ and length scales $R = 6-20 \mu\text{m}$. See their Figs. 1 and 16 for details on the bound. This work does not place limits on the size of extra flat dimensions.

² HOYLE 04 search for new forces, probing α down to 10^{-2} and distances down to $10\mu\text{m}$. Quoted bound on R is for $\delta = 2$. For $\delta = 1$, bound goes to $160 \mu\text{m}$. See their Fig. 34 for details on the bound.

³ CHIAVERINI 03 search for new forces, probing α above 10^4 and λ down to $3\mu\text{m}$, finding no signal. See their Fig. 4 for details on the bound. This bound does not place limits on the size of extra flat dimensions.

⁴ LONG 03 search for new forces, probing α down to 3, and distances down to about $10\mu\text{m}$. See their Fig. 4 for details on the bound.

⁵ HOYLE 01 search for new forces, probing α down to 10^{-2} and distances down to $20\mu\text{m}$. See their Fig. 4 for details on the bound. The quoted bound is for $\alpha \geq 3$.

⁶ HOSKINS 85 search for new forces, probing distances down to 4 mm. See their Fig. 13 for details on the bound. This bound does not place limits on the size of extra flat dimensions.

Limits on R from On-Shell Production of Gravitons: $\delta = 2$

This section includes limits on on-shell production of gravitons in collider and astrophysical processes. Bounds quoted are on R , the assumed common radius of the flat extra dimensions, for $\delta = 2$ extra dimensions. Studies often quote bounds in terms of derived parameter; experiments are actually sensitive to the masses of the KK gravitons: $m_{\vec{n}} = |\vec{n}|/R$. See the Review on "Extra Dimensions" for details. Bounds are given in μm for $\delta=2$.

VALUE (μm)	CL%	DOCUMENT ID	TECN	COMMENT
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
< 270	95	7 ABDALLAH	05B DLPH	$e^+ e^- \rightarrow \gamma G$
< 210	95	8 ACHARD	04E L3	$e^+ e^- \rightarrow \gamma G$
< 480	95	9 ACOSTA	04C CDF	$\bar{p}p \rightarrow jG$
< 0.00038	95	10 CASSE	04	Neutron star γ sources
< 610	95	11 ABAZOV	03 D0	$\bar{p}p \rightarrow jG$
< 0.96	95	12 HANNESTAD	03	Supernova cooling
< 0.096	95	13 HANNESTAD	03	Diffuse γ background
< 0.051	95	14 HANNESTAD	03	Neutron star γ sources
< 0.00016	95	15 HANNESTAD	03	Neutron star heating
< 300	95	16 HEISTER	03C ALEP	$e^+ e^- \rightarrow \gamma G$
		17 FAIRBAIRN	01	Cosmology
< 0.66	95	18 HANHART	01	Supernova cooling
		19 CASSISI	00	Red giants
<1300	95	20 ACCIARRI	99S L3	$e^+ e^- \rightarrow ZG$

Limits on R from On-Shell Production of Gravitons: $\delta \geq 3$

This section includes limits similar to those in the previous section, but for $\delta = 3$ extra dimensions. Bounds are given in nm for $\delta = 3$. Entries are also shown for papers examining models with $\delta > 3$.

<u>VALUE (nm)</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
< 3.5	95	⁷ ABDALLAH	05B DLPH	$e^+ e^- \rightarrow \gamma G$
< 2.9	95	⁸ ACHARD	04E L3	$e^+ e^- \rightarrow \gamma G$
	95	⁹ ACOSTA	04C CDF	$\bar{p}p \rightarrow jG$
< 0.0042	95	¹⁰ CASSE	04	Neutron star γ sources
< 6.1	95	¹¹ ABAZOV	03 D0	$\bar{p}p \rightarrow jG$
< 1.14	95	¹² HANNESTAD	03	Supernova cooling
< 0.025	95	¹³ HANNESTAD	03	Diffuse γ background
< 0.11	95	¹⁴ HANNESTAD	03	Neutron star γ sources
< 0.0026	95	¹⁵ HANNESTAD	03	Neutron star heating
< 3.9	95	¹⁶ HEISTER	03C ALEP	$e^+ e^- \rightarrow \gamma G$
		²¹ ACOSTA	02H CDF	$p\bar{p} \rightarrow \gamma G$
		¹⁷ FAIRBAIRN	01	Cosmology
< 0.8	95	¹⁸ HANHART	01	Supernova cooling
		¹⁹ CASSISI	00	Red giants
<18	95	²⁰ ACCIARRI	99s L3	$e^+ e^- \rightarrow ZG$

⁷ ABDALLAH 05B search for $e^+ e^- \rightarrow \gamma G$ at $\sqrt{s} = 180\text{--}209$ GeV to place bounds on the size of extra dimensions and the fundamental scale. Limits for all $\delta \leq 6$ are given in their Table 6. These limits supersede those in ABREU 00Z.

⁸ ACHARD 04E search for $e^+ e^- \rightarrow \gamma G$ at $\sqrt{s} = 189\text{--}209$ GeV to place bounds on the size of extra dimensions and the fundamental scale. See their Table 8 for limits with $\delta \leq 8$. These limits supersede those in ACCIARRI 99R.

⁹ ACOSTA 04C search for $\bar{p}p \rightarrow jG$ at $\sqrt{s} = 1.8$ TeV to place bounds on the size of extra dimensions and the fundamental scale. See their paper for bounds on $\delta = 4, 6$.

¹⁰ CASSE 04 obtain a limit on R from the gamma-ray emission of point γ sources that arises from the photon decay of gravitons around newly born neutron stars, applying the technique of HANNESTAD 03 to neutron stars in the galactic bulge. Limits for all $\delta \leq 7$ are given in their Table I.

¹¹ ABAZOV 03 search for $p\bar{p} \rightarrow jG$ at $\sqrt{s}=1.8$ TeV to place bounds on M_D for 2 to 7 extra dimensions, from which these bounds on R are derived. See their paper for bounds on intermediate values of δ . We quote results without the approximate NLO scaling introduced in the paper.

¹² HANNESTAD 03 obtain a limit on R from graviton cooling of supernova SN1987a. Limits for all $\delta \leq 7$ are given in their Tables V and VI.

¹³ HANNESTAD 03 obtain a limit on R from gravitons emitted in supernovae and which subsequently decay, contaminating the diffuse cosmic γ background. Limits for all $\delta \leq 7$ are given in their Tables V and VI. These limits supersede those in HANNESTAD 02.

¹⁴ HANNESTAD 03 obtain a limit on R from gravitons emitted in two recent supernovae and which subsequently decay, creating point γ sources. Limits for all $\delta \leq 7$ are given in their Tables V and VI. These limits are corrected in the published erratum.

¹⁵ HANNESTAD 03 obtain a limit on R from the heating of old neutron stars by the surrounding cloud of trapped KK gravitons. Limits for all $\delta \leq 7$ are given in their Tables V and VI. These limits supersede those in HANNESTAD 02.

¹⁶ HEISTER 03C use the process $e^+ e^- \rightarrow \gamma G$ at $\sqrt{s} = 189\text{--}209$ GeV to place bounds on the size of extra dimensions and the scale of gravity. See their Table 4 for limits with $\delta \leq 6$ for derived limits on M_D .

¹⁷ FAIRBAIRN 01 obtains bounds on R from over production of KK gravitons in the early universe. Bounds are quoted in paper in terms of fundamental scale of gravity. Bounds

depend strongly on temperature of QCD phase transition and range from $R < 0.13 \mu\text{m}$ to $0.001 \mu\text{m}$ for $\delta=2$; bounds for $\delta=3,4$ can be derived from Table 1 in the paper.

- ¹⁸ HANHART 01 obtain bounds on R from limits on graviton cooling of supernova SN 1987a using numerical simulations of proto-neutron star neutrino emission.
- ¹⁹ CASSISI 00 obtain rough bounds on M_D (and thus R) from red giant cooling for $\delta=2,3$. See their paper for details.
- ²⁰ ACCIARRI 99s search for $e^+ e^- \rightarrow Z G$ at $\sqrt{s}=189 \text{ GeV}$. Limits on the gravity scale are found in their Table 2, for $\delta \leq 4$.
- ²¹ ACOSTA 02H uses the process $p\bar{p} \rightarrow \gamma G$ at $\sqrt{s} = 1.8 \text{ TeV}$ to place bounds on R for $\delta=4,6$, and 8: $R < 24 \text{ nm}$, 55 fm , and 2.6 fm respectively. However the kinematics relevant to these bounds are probably outside the validity range of the effective theory.

Mass Limits on M_{TT}

This section includes limits on the cut-off mass scale, M_{TT} , of dimension-8 operators from KK graviton exchange in models of large extra dimensions. Ambiguities in the UV-divergent summation are absorbed into the parameter λ , which is taken to be $\lambda = \pm 1$ in the following analyses. Bounds for $\lambda = -1$ are shown in parenthesis after the bound for $\lambda = +1$, if appropriate. Different papers use slightly different definitions of the mass scale. The definition used here is related to another popular convention by $M_{TT}^4 = (2/\pi) \Lambda_T^4$, as discussed in the above Review on "Extra Dimensions." All bounds scale as $\lambda^{1/4}$, unless otherwise stated.

VALUE (TeV)	CL%	DOCUMENT ID	TECN	COMMENT
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
> 0.96 (> 0.93)	95	22 ABAZOV	05V D0	$p\bar{p} \rightarrow \mu^+ \mu^-$
> 0.78 (> 0.79)	95	23 CHEKANOV	04B ZEUS	$e^\pm p \rightarrow e^\pm X$
> 0.805 (> 0.956)	95	24 ABBIENDI	03D OPAL	$e^+ e^- \rightarrow \gamma\gamma$
> 0.7 (> 0.7)	95	25 ACHARD	03D L3	$e^+ e^- \rightarrow ZZ$
> 0.82 (> 0.78)	95	26 ADLOFF	03 H1	$e^\pm p \rightarrow e^\pm X$
> 1.28 (> 1.25)	95	27 GIUDICE	03 RVUE	
> 20.6 (> 15.7)	95	28 GIUDICE	03 RVUE	Dim-6 operators
> 0.80 (> 0.85)	95	29 HEISTER	03C ALEP	$e^+ e^- \rightarrow \gamma\gamma$
> 0.84 (> 0.99)	95	30 ACHARD	02D L3	$e^+ e^- \rightarrow \gamma\gamma$
> 1.2 (> 1.1)	95	31 ABBOTT	01 D0	$p\bar{p} \rightarrow e^+ e^-, \gamma\gamma$
> 0.60 (> 0.63)	95	32 ABBIENDI	00R OPAL	$e^+ e^- \rightarrow \mu^+ \mu^-$
> 0.63 (> 0.50)	95	32 ABBIENDI	00R OPAL	$e^+ e^- \rightarrow \tau^+ \tau^-$
> 0.68 (> 0.61)	95	32 ABBIENDI	00R OPAL	$e^+ e^- \rightarrow \mu^+ \mu^-, \tau^+ \tau^-$
		33 ABREU	00A DLPH	
> 0.649 (> 0.559)	95	34 ABREU	00S DLPH	$e^+ e^- \rightarrow \mu^+ \mu^-$
> 0.564 (> 0.450)	95	34 ABREU	00S DLPH	$e^+ e^- \rightarrow \tau^+ \tau^-$
> 0.680 (> 0.542)	95	34 ABREU	00S DLPH	$e^+ e^- \rightarrow \mu^+ \mu^-, \tau^+ \tau^-$
> 15–28	99.7	35 CHANG	00B RVUE	Electroweak
> 0.98	95	36 CHEUNG	00 RVUE	$e^+ e^- \rightarrow \gamma\gamma$
> 0.29–0.38	95	37 GRAESSER	00 RVUE	$(g-2)_\mu$
> 0.50–1.1	95	38 HAN	00 RVUE	Electroweak
> 2.0 (> 2.0)	95	39 MATHEWS	00 RVUE	$\bar{p}p \rightarrow jj$
> 1.0 (> 1.1)	95	40 MELE	00 RVUE	$e^+ e^- \rightarrow VV$
		41 ABBIENDI	99P OPAL	
		42 ACCIARRI	99M L3	
		43 ACCIARRI	99S L3	
> 1.412 (> 1.077)	95	44 BOURILKOV	99	$e^+ e^- \rightarrow e^+ e^-$

- 22 ABAZOV 05V use 246 pb^{-1} of data from $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ to search for deviations in the differential cross section to $\mu^+\mu^-$ from graviton exchange.
- 23 CHEKANOV 04B search for deviations in the differential cross section of $e^\pm p \rightarrow e^\pm X$ with 130 pb^{-1} of combined data and Q^2 values up to $40,000 \text{ GeV}^2$ to place a bound on M_{TT} .
- 24 ABBIENDI 03D use e^+e^- collisions at $\sqrt{s}=181\text{--}209$ to place bounds on the ultraviolet scale M_{TT} , which is equivalent to their definition of M_S .
- 25 ACHARD 03D look for deviations in the cross section for $e^+e^- \rightarrow ZZ$ from $\sqrt{s} = 200\text{--}209 \text{ GeV}$ to place a bound on M_{TT} .
- 26 ADLOFF 03 search for deviations in the differential cross section of $e^\pm p \rightarrow e^\pm X$ at $\sqrt{s}=301$ and 319 GeV to place bounds on M_{TT} .
- 27 GIUDICE 03 review existing experimental bounds on M_{TT} and derive a combined limit.
- 28 GIUDICE 03 place bounds on Λ_6 , the coefficient of the gravitationally-induced dimension-6 operator $(2\pi\lambda/\Lambda_6^2)(\sum \bar{f}\gamma_\mu\gamma^5 f)(\sum \bar{f}\gamma^\mu\gamma^5 f)$, using data from a variety of experiments. Results are quoted for $\lambda=\pm 1$ and are independent of δ .
- 29 HEISTER 03C use e^+e^- collisions at $\sqrt{s}=189\text{--}209 \text{ GeV}$ to place bounds on the scale of dim-8 gravitational interactions. Their M_S^\pm is equivalent to our M_{TT} with $\lambda=\pm 1$.
- 30 ACHARD 02 search for s -channel graviton exchange effects in $e^+e^- \rightarrow \gamma\gamma$ at $E_{\text{cm}} = 192\text{--}209 \text{ GeV}$.
- 31 ABBOTT 01 search for variations in differential cross sections to e^+e^- and $\gamma\gamma$ final states at the Tevatron.
- 32 ABBIENDI 00R uses e^+e^- collisions at $\sqrt{s}=189 \text{ GeV}$.
- 33 ABREU 00A search for s -channel graviton exchange effects in $e^+e^- \rightarrow \gamma\gamma$ at $E_{\text{cm}}=189\text{--}202 \text{ GeV}$.
- 34 ABREU 00S uses e^+e^- collisions at $\sqrt{s}=183$ and 189 GeV .
- 35 CHANG 00B derive 3σ limit on M_{TT} of $(28,19,15) \text{ TeV}$ for $\delta=(2,4,6)$ respectively assuming the presence of a torsional coupling in the gravitational action. Highly model dependent.
- 36 CHEUNG 00 obtains limits from anomalous diphoton production at OPAL due to graviton exchange. Original limit for $\delta=4$. However, unknown UV theory renders δ dependence unreliable. Original paper works in HLZ convention.
- 37 GRAESSER 00 obtains a bound from graviton contributions to $g-2$ of the muon through loops of 0.29 TeV for $\delta=2$ and 0.38 TeV for $\delta=4,6$. Limits scale as $\lambda^{1/2}$. However calculational scheme not well-defined without specification of high-scale theory. See the "Extra Dimensions Review."
- 38 HAN 00 calculates corrections to gauge boson self-energies from KK graviton loops and constrain them using S and T . Bounds on M_{TT} range from 0.5 TeV ($\delta=6$) to 1.1 TeV ($\delta=2$); see text. Limits have strong dependence, $\lambda^{\delta+2}$, on unknown λ coefficient.
- 39 MATHEWS 00 search for evidence of graviton exchange in CDF and $D\bar{D}$ dijet production data. See their Table 2 for slightly stronger δ -dependent bounds. Limits expressed in terms of $\tilde{M}_S^4 = M_{TT}^4/8$.
- 40 MELE 00 obtains bound from KK graviton contributions to $e^+e^- \rightarrow VV$ ($V=\gamma, W, Z$) at LEP. Authors use Hewett conventions.
- 41 ABBIENDI 99P search for s -channel graviton exchange effects in $e^+e^- \rightarrow \gamma\gamma$ at $E_{\text{cm}}=189 \text{ GeV}$. The limits $G_+ > 660 \text{ GeV}$ and $G_- > 634 \text{ GeV}$ are obtained from combined $E_{\text{cm}}=183$ and 189 GeV data, where G_\pm is a scale related to the fundamental gravity scale.
- 42 ACCIARRI 99M search for the reaction $e^+e^- \rightarrow \gamma G$ and s -channel graviton exchange effects in $e^+e^- \rightarrow \gamma\gamma, W^+W^-, ZZ, e^+e^-, \mu^+\mu^-, \tau^+\tau^-, q\bar{q}$ at $E_{\text{cm}}=183 \text{ GeV}$. Limits on the gravity scale are listed in their Tables 1 and 2.
- 43 ACCIARRI 99S search for the reaction $e^+e^- \rightarrow ZG$ and s -channel graviton exchange effects in $e^+e^- \rightarrow \gamma\gamma, W^+W^-, ZZ, e^+e^-, \mu^+\mu^-, \tau^+\tau^-, q\bar{q}$ at $E_{\text{cm}}=189 \text{ GeV}$. Limits on the gravity scale are listed in their Tables 1 and 2.

⁴⁴ BOURILKOV 99 performs global analysis of LEP data on e^+e^- collisions at $\sqrt{s}=183$ and 189 GeV. Bound is on Λ_T .

Direct Limits on Gravitational or String Mass Scale

This section includes limits on the fundamental gravitational scale and/or the string scale from processes which depend directly on one or the other of these scales.

VALUE (TeV)	DOCUMENT ID	TECN	COMMENT
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
$\gtrsim 1-2$	⁴⁵ ANCHORDOQ.02B	RVUE	Cosmic Rays
>0.49	⁴⁶ ACCIARRI	00P L3	$e^+e^- \rightarrow e^+e^-$
⁴⁵ ANCHORDOQUI 02B derive bound on M_D from non-observation of black hole production in high-energy cosmic rays. Bound is stronger for larger δ , but depends sensitively on threshold for black hole production.			
⁴⁶ ACCIARRI 00P uses e^+e^- collisions at $\sqrt{s}=183$ and 189 GeV. Bound on string scale M_S from massive string modes. M_S is defined in hep-ph/0001166 by $M_S(1/\pi)^{1/8}\alpha^{-1/4} = M$ where $(4\pi G)^{-1} = M^{n+2}R^n$.			

Limits on $1/R = M_C$

This section includes limits on $1/R = M_C$, the compactification scale in models with TeV extra dimensions, due to exchange of Standard Model KK excitations. See the "Extra Dimension Review" for discussion of model dependence.

VALUE (TeV)	CL%	DOCUMENT ID	TECN	COMMENT
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
>3.3	95	⁴⁷ CORNET	00	RVUE Electroweak
$>3.3-3.8$	95	⁴⁸ RIZZO	00	RVUE Electroweak
⁴⁷ CORNET 00 translates a bound on the coefficient of the 4-fermion operator $(\bar{\ell}\gamma_\mu\tau^a\ell)(\bar{\ell}\gamma^\mu\tau^a\ell)$ derived by Hagiwara and Matsumoto into a limit on the mass scale of KK W bosons.				
⁴⁸ RIZZO 00 obtains limits from global electroweak fits in models with a Higgs in the bulk (3.8 TeV) or on the standard brane (3.3 TeV).				

Limits on Kaluza-Klein Gravitons in Warped Extra Dimensions

This sections places limits on the mass of the first Kaluza-Klein excitation of the graviton in the warped extra dimension model of Randall and Sundrum. Experimental bounds depend strongly on the warp parameter, k . See the "Extra Dimensions" review for a full discussion.

VALUE	DOCUMENT ID	TECN	COMMENT
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
	⁴⁹ ABAZOV	05N D0	$p\bar{p} \rightarrow G \rightarrow \ell\ell, \gamma\gamma$
	⁵⁰ ABULENCIA	05A CDF	$p\bar{p} \rightarrow G \rightarrow \ell\bar{\ell}$

- 49 ABAZOV 05N use $p\bar{p}$ collisions at 1.96 TeV to search for KK gravitons in warped extra dimensions. They search for graviton resonances decaying to muons, electrons or photons, using 260 pb^{-1} of data. For warp parameter values of $k = 0.1, 0.05, \text{ and } 0.01$, the bounds on the gravitino mass are 785, 650 and 250 GeV respectively. See their Fig. 3 for more details.
- 50 ABULENCIA 05A use $p\bar{p}$ collisions at 1.96 TeV to search for KK gravitons in warped extra dimensions. They search for graviton resonances decaying to muons or electrons, using 200 pb^{-1} of data. For warp parameter values of $k = 0.1, 0.05, \text{ and } 0.01$, the bounds on the gravitino mass are 710, 510 and 170 GeV respectively.

Limits on Mass of Radion

This section includes limits on mass of radion, usually in context of Randall-Sundrum models. See the "Extra Dimension Review" for discussion of model dependence.

VALUE (GeV)	DOCUMENT ID	TECN	COMMENT
• • •	We do not use the following data for averages, fits, limits, etc. • • •		
> 35	51 ABBIENDI	05 OPAL	$e^+ e^- \rightarrow Z$ radion
> 120	52 MAHANTA	00	$Z \rightarrow$ radion $\ell\bar{\ell}$
	53 MAHANTA	00B	$p\bar{p} \rightarrow$ radion $\rightarrow \gamma\gamma$

- 51 ABBIENDI 05 use $e^+ e^-$ collisions at $\sqrt{s} = 91 \text{ GeV}$ and $\sqrt{s} = 189\text{--}209 \text{ GeV}$ to place bounds on the radion mass in the RS model. See their Fig. 5 for bounds that depend on the radion-Higgs mixing parameter ξ and on $\Lambda_W = \Lambda_\phi/\sqrt{6}$. No parameter-independent bound is obtained.
- 52 MAHANTA 00 obtain bound on radion mass in the RS model. Bound is from Higgs boson search at LEP I.
- 53 MAHANTA 00B uses $p\bar{p}$ collisions at $\sqrt{s} = 1.8 \text{ TeV}$; production via gluon-gluon fusion. Authors assume a radion vacuum expectation value of 1 TeV.

REFERENCES FOR Extra Dimensions

ABAZOV	05N	PRL 95 091801	V.M. Abazov <i>et al.</i>	(D0 Collab.)
ABAZOV	05V	PRL 95 161602	V.M. Abazov <i>et al.</i>	(D0 Collab.)
ABBIENDI	05	PL B609 20	G. Abbiendi <i>et al.</i>	(OPAL Collab.)
ABDALLAH	05B	EPJ C38 395	J. Abdallah <i>et al.</i>	(DELPHI Collab.)
ABULENCIA	05A	PRL 95 252001	A. Abulencia <i>et al.</i>	(CDF Collab.)
SMULLIN	05	PR D72 122001	S.J. Smullin <i>et al.</i>	
ACHARD	04E	PL B587 16	P. Achard <i>et al.</i>	(L3)
ACOSTA	04C	PRL 92 121802	D. Acosta <i>et al.</i>	(CDF Collab.)
CASSE	04	PRL 92 111102	M. Casse <i>et al.</i>	
CHEKANOV	04B	PL B591 23	S. Chekanov <i>et al.</i>	(ZEUS Collab.)
HOYLE	04	PR D70 042004	C.D. Hoyle <i>et al.</i>	(WASH)
ABAZOV	03	PRL 90 251802	V.M. Abazov <i>et al.</i>	(D0 Collab.)
ABBIENDI	03D	EPJ C26 331	G. Abbiendi <i>et al.</i>	(OPAL Collab.)
ACHARD	03D	PL B572 133	P. Achard <i>et al.</i>	(L3 Collab.)
ADLOFF	03	PL B568 35	C. Adloff <i>et al.</i>	(H1 Collab.)
CHIAVERINI	03	PRL 90 151101	J. Chiaverini <i>et al.</i>	
GIUDICE	03	NP B663 377	G.F. Giudice, A. Strumia	
HANNESTAD	03	PR D67 125008	S. Hannestad, G.G. Raffelt	
Also		PR D69 029901(erratum)	S. Hannestad, G.G. Raffelt	
HEISTER	03C	EPJ C28 1	A. Heister <i>et al.</i>	(ALEPH Collab.)
LONG	03	Nature 421 922	J.C. Long <i>et al.</i>	
ACHARD	02	PL B524 65	P. Achard <i>et al.</i>	(L3 Collab.)
ACHARD	02D	PL B531 28	P. Achard <i>et al.</i>	(L3 Collab.)
ACOSTA	02H	PRL 89 281801	D. Acosta <i>et al.</i>	(CDF Collab.)
ANCHORDOQ...	02B	PR D66 103002	L. Anchordoqui <i>et al.</i>	
HANNESTAD	02	PRL 88 071301	S. Hannestad, G. Raffelt	
ABBOTT	01	PRL 86 1156	B. Abbott <i>et al.</i>	(D0 Collab.)
FAIRBAIRN	01	PL B508 335	M. Fairbairn	

HANHART	01	PL B509 1	C. Hanhart <i>et al.</i>	
HOYLE	01	PRL 86 1418	C.D. Hoyle <i>et al.</i>	
ABBIENDI	00R	EPJ C13 553	G. Abbiendi <i>et al.</i>	(OPAL Collab.)
ABREU	00A	PL B491 67	P. Abreu <i>et al.</i>	(DELPHI Collab.)
ABREU	00S	PL B485 45	P. Abreu <i>et al.</i>	(DELPHI Collab.)
ABREU	00Z	EPJ C17 53	P. Abreu <i>et al.</i>	(DELPHI Collab.)
ACCIARRI	00P	PL B489 81	M. Acciarri <i>et al.</i>	(L3 Collab.)
CASSISI	00	PL B481 323	S. Cassisi <i>et al.</i>	
CHANG	00B	PRL 85 3765	L.N. Chang <i>et al.</i>	
CHEUNG	00	PR D61 015005	K. Cheung	
CORNET	00	PR D61 037701	F. Cornet, M. Relano, J. Rico	
GRAESSER	00	PR D61 074019	M.L. Graesser	
HAN	00	PR D62 125018	T. Han, D. Marfatia, R.-J. Zhang	
MAHANTA	00	PL B480 176	U. Mahanta, S. Rakshit	
MAHANTA	00B	PL B483 196	U. Mahanta, A. Datta	
MATHEWS	00	JHEP 0007 008	P. Mathews, S. Raychaudhuri, K. Sridhar	
MELE	00	PR D61 117901	S. Mele, E. Sanchez	
RIZZO	00	PR D61 016007	T.G. Rizzo, J.D. Wells	
ABBIENDI	99P	PL B465 303	G. Abbiendi <i>et al.</i>	(OPAL Collab.)
ACCIARRI	99M	PL B464 135	M. Acciarri <i>et al.</i>	(L3 Collab.)
ACCIARRI	99R	PL B470 268	M. Acciarri <i>et al.</i>	(L3 Collab.)
ACCIARRI	99S	PL B470 281	M. Acciarri <i>et al.</i>	(L3 Collab.)
BOURILKOV	99	JHEP 08 006	D. Bourilkov	
HOSKINS	85	PR D32 3084	J.K. Hoskins <i>et al.</i>	
