

## $\tau$ -LEPTON DECAY PARAMETERS

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The purpose of the measurements of the decay parameters (*i.e.*, Michel parameters) of the  $\tau$  is to determine the structure (spin and chirality) of the current mediating its decays.

**Leptonic Decays:** The Michel parameters are extracted from the energy spectrum of the charged daughter lepton  $\ell = e, \mu$  in the decays  $\tau \rightarrow \ell \nu_\ell \nu_\tau$ . Ignoring radiative corrections, neglecting terms of order  $(m_\ell/m_\tau)^2$  and  $(m_\tau/\sqrt{s})^2$ , and setting the neutrino masses to zero, the spectrum in the laboratory frame reads

$$\frac{d\Gamma}{dx} = \frac{G_{\tau\ell}^2 m_\tau^5}{192 \pi^3} \times \left\{ f_0(x) + \rho f_1(x) + \eta \frac{m_\ell}{m_\tau} f_2(x) - P_\tau [\xi g_1(x) + \xi \delta g_2(x)] \right\}, \quad (1)$$

with

$$\begin{aligned} f_0(x) &= 2 - 6x^2 + 4x^3 \\ f_1(x) &= -\frac{4}{9} + 4x^2 - \frac{32}{9}x^3 & g_1(x) &= -\frac{2}{3} + 4x - 6x^2 + \frac{8}{3}x^3 \\ f_2(x) &= 12(1-x)^2 & g_2(x) &= \frac{4}{9} - \frac{16}{3}x + 12x^2 - \frac{64}{9}x^3. \end{aligned}$$

The integrated decay width is given by

$$\Gamma = \frac{G_{\tau\ell}^2 m_\tau^5}{192 \pi^3} \left( 1 + 4\eta \frac{m_\ell}{m_\tau} \right). \quad (2)$$

The situation is similar to muon decays  $\mu \rightarrow e \nu_e \nu_\mu$ . The generalized matrix element with the couplings  $g_{\varepsilon\mu}^\gamma$  and their relations to the Michel parameters  $\rho, \eta, \xi$ , and  $\delta$  have been described in the “Note on Muon Decay Parameters”. The Standard Model expectations are 3/4, 0, 1, and 3/4, respectively. For more details, see Ref. 1.

**Hadronic Decays:** In the case of hadronic decays  $\tau \rightarrow h \nu_\tau$ , with  $h = \pi, \rho$ , or  $a_1$ , the ansatz is restricted to purely vectorial currents. The matrix element is

$$\frac{G_{\tau h}}{\sqrt{2}} \sum_{\lambda=R,L} g_\lambda \langle \bar{\Psi}_\omega(\nu_\tau) | \gamma^\mu | \Psi_\lambda(\tau) \rangle J_\mu^h \quad (3)$$

with the hadronic current  $J_\mu^h$ . The neutrino chirality  $\omega$  is uniquely determined from  $\lambda$ . The spectrum depends only on a single parameter  $\xi_h$

$$\frac{d\Gamma}{d\vec{x}} = f(\vec{x}) + \xi_h P_\tau g(\vec{x}) , \quad (4)$$

with  $f$  and  $g$  being channel-dependent functions of the observables  $\vec{x}$  (see Ref. 2). The parameter  $\xi_h$  is related to the couplings through

$$\xi_h = |g_L|^2 - |g_R|^2 . \quad (5)$$

$\xi_h$  is the negative of the chirality of the  $\tau$  neutrino in these decays. In the Standard Model,  $\xi_h = 1$ . Also included are measurements of the neutrino helicity which coincide with  $\xi_h$ , if the neutrino is massless (ASNER 00, ACKERSTAFF 97R, AKERS 95P, ALBRECHT 93C, and ALBRECHT 90I).

**Combination of Measurements:** The individual measurements are combined, taking into account the correlations between the parameters. There is one fit, assuming universality between the two leptonic decays, and between all hadronic decays and a second fit without these assumptions. These are the values labeled 'OUR FIT' in the tables. The measurements show good agreement with the Standard Model. The  $\chi^2$  values with respect to the Standard model predictions are 25.8 for 41 degrees of freedom and 31.1 for 56 degrees of freedom, respectively. The correlations are reduced through this combination to less than 20%, with the exception of  $\rho$  and  $\eta$  which are correlated by +24%, for the fit with universality and by +43% for  $\tau \rightarrow \mu\nu_\mu\nu_\tau$ .

**Model-independent Analysis:** From the Michel parameters, limits can be derived on the couplings  $g_{\varepsilon\lambda}^\kappa$  without further module assumptions. In the Standard model  $g_{LL}^V = 1$  (leptonic decays), and  $g_L = 1$  (hadronic decays) and all other couplings vanish. First, the partial decay widths have to be compared to the Standard Model predictions to derive limits on the

normalization of the couplings  $A_x = G_{\tau x}^2/G_F^2$  with Fermi's constant  $G_F$ :

$$\begin{aligned}
 A_e &= 1.0012 \pm 0.0053 , \\
 A_\mu &= 1.007 \pm 0.025 , \\
 A_\pi &= 1.018 \pm 0.012 .
 \end{aligned}
 \tag{6}$$

Then limits on the couplings (95% CL) can be extracted (see Ref. 3 and Ref. 4). Without the assumption of universality, the limits given in Table 1 are derived.

**Table 1:** Coupling constants  $g_{\varepsilon\mu}^\gamma$ . 95% confidence level experimental limits. The limits include the quoted values of  $A_e$ ,  $A_\mu$ , and  $A_\pi$  and assume  $A_\rho = A_{a_1} = 1$ .

$\tau \rightarrow e\nu_e\nu_\tau$		
$ g_{RR}^S  < 0.72$	$ g_{RR}^V  < 0.18$	$ g_{RR}^T  \equiv 0$
$ g_{LR}^S  < 1.00$	$ g_{LR}^V  < 0.13$	$ g_{LR}^T  < 0.084$
$ g_{RL}^S  < 2.01$	$ g_{RL}^V  < 0.52$	$ g_{RL}^T  < 0.51$
$ g_{LL}^S  < 2.01$	$ g_{LL}^V  < 1.005$	$ g_{LL}^T  \equiv 0$
$\tau \rightarrow \mu\nu_\mu\nu_\tau$		
$ g_{RR}^S  < 0.76$	$ g_{RR}^V  < 0.19$	$ g_{RR}^T  \equiv 0$
$ g_{LR}^S  < 1.10$	$ g_{LR}^V  < 0.14$	$ g_{LR}^T  < 0.088$
$ g_{RL}^S  < 2.05$	$ g_{RL}^V  < 0.53$	$ g_{RL}^T  < 0.52$
$ g_{LL}^S  < 2.05$	$ g_{LL}^V  < 1.02$	$ g_{LL}^T  \equiv 0$
$\tau \rightarrow \pi\nu_\tau$		
$ g_R^V  < 0.22$	$ g_L^V  > 0.98$	
$\tau \rightarrow \rho\nu_\tau$		
$ g_R^V  < 0.10$	$ g_L^V  > 0.995$	
$\tau \rightarrow a_1\nu_\tau$		
$ g_R^V  < 0.27$	$ g_L^V  > 0.96$	

**Model-dependent Interpretation:** More stringent limits can be derived assuming specific models. For example, in the framework of a two Higgs doublet model, the measurements correspond to a limit of  $m_{H^\pm} > 1.8 \text{ GeV} \times \tan \beta$  on the mass of the charged Higgs boson, or a limit of 241 GeV on the mass of the second  $W$  boson in left-right symmetric models for arbitrary mixing (both 95% CL). See Ref. 4 and Ref. 5.

#### Footnotes and References

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