

## 2. ASTROPHYSICAL CONSTANTS

**Table 2.1.** Revised 2000 by D.E. Groom (LBNL). The figures in parentheses after some values give the one-standard deviation uncertainties in the last digit(s). Physical constants are from Ref. 1. While every effort has been made to obtain the most accurate current values of the listed quantities, the table does not represent a critical review or adjustment of the constants, and is not intended as a primary reference.

Quantity	Symbol, equation	Value	Reference, footnote
speed of light	$c$	299 792 458 m s <sup>-1</sup>	defined[2]
Newtonian gravitational constant	$G_N$	6.673(10) × 10 <sup>-11</sup> m <sup>3</sup> kg <sup>-1</sup> s <sup>-2</sup>	[3]
astronomical unit (mean ⊕-☉ distance)	au	149 597 870 660(20) m	[4, 5]
tropical year (equinox to equinox) (2001.0)	yr	31 556 925.2 s	[4]
sidereal year (fixed star to fixed star) (2001.0)		31 558 149.8 s	[4]
mean sidereal day (2001.0)		23 <sup>h</sup> 56 <sup>m</sup> 04 <sup>s</sup> .090 53	[4]
Jansky	Jy	10 <sup>-26</sup> W m <sup>-2</sup> Hz <sup>-1</sup>	
Planck mass	$\sqrt{hc/G_N}$	1.2210(9) × 10 <sup>19</sup> GeV/c <sup>2</sup> = 2.176 7(16) × 10 <sup>-8</sup> kg	[1]
parsec (1 AU/1 arc sec)	pc	3.085 677 580 7(4) × 10 <sup>16</sup> m = 3.262...ly	[6]
light year (deprecated unit)	ly	0.306 6... pc = 0.946 1... × 10 <sup>16</sup> m	
Schwarzschild radius of the Sun	$2G_N M_\odot/c^2$	2.953 250 08 km	[7]
solar mass	$M_\odot$	1.988 9(30) × 10 <sup>30</sup> kg	[8]
solar equatorial radius	$R_\odot$	6.961 × 10 <sup>8</sup> m	[4]
solar luminosity	$L_\odot$	(3.846 ± 0.008) × 10 <sup>26</sup> W	[9]
Schwarzschild radius of the Earth	$2G_N M_\oplus/c^2$	<b>8.870 056 22 mm</b>	[10]
Earth mass	$M_\oplus$	5.974(9) × 10 <sup>24</sup> kg	[11]
Earth mean equatorial radius	$R_\oplus$	6.378 140 × 10 <sup>6</sup> m	[4]
luminosity conversion	$L$	3.02 × 10 <sup>28</sup> × 10 <sup>-0.4 M<sub>bol</sub></sup> W (M <sub>bol</sub> = absolute bolometric magnitude = bolometric magnitude at 10 pc)	[12]
flux conversion	$\mathcal{F}$	2.52 × 10 <sup>-8</sup> × 10 <sup>-0.4 m<sub>bol</sub></sup> W m <sup>-2</sup> (m <sub>bol</sub> = apparent bolometric magnitude)	from above
$v_\odot$ around center of Galaxy	$\Theta_\odot$	220(20) km s <sup>-1</sup>	[13]
solar distance from galactic center	$R_\odot$	8.0(5) kpc	[14]
Hubble expansion rate <sup>†</sup>	$H_0$	100 h <sub>0</sub> km s <sup>-1</sup> Mpc <sup>-1</sup> = h <sub>0</sub> × (9.778 13 Gyr) <sup>-1</sup>	[15]
normalized Hubble expansion rate <sup>†</sup>	$h_0$	(0.71 ± 0.07) × $\frac{1.15}{0.95}$	[16, 17]
critical density of the universe <sup>†</sup>	$\rho_c = 3H_0^2/8\pi G_N$	2.775 366 27 × 10 <sup>11</sup> h <sub>0</sub> <sup>2</sup> M <sub>☉</sub> Mpc <sup>-3</sup> = 1.879(3) × 10 <sup>-29</sup> h <sub>0</sub> <sup>2</sup> g cm <sup>-3</sup> = 1.053 9(16) × 10 <sup>-5</sup> h <sub>0</sub> <sup>2</sup> GeV cm <sup>-3</sup>	
local disk density	$\rho_{\text{disk}}$	3–12 × 10 <sup>-24</sup> g cm <sup>-3</sup> ≈ 2–7 GeV/c <sup>2</sup> cm <sup>-3</sup>	[18]
local halo density	$\rho_{\text{halo}}$	2–13 × 10 <sup>-25</sup> g cm <sup>-3</sup> ≈ 0.1–0.7 GeV/c <sup>2</sup> cm <sup>-3</sup>	[19]
pressureless matter density of the universe <sup>†</sup>	$\Omega_M \equiv \rho_M/\rho_c$	0.15 ≲ Ω <sub>M</sub> ≲ 0.45	[16, 20]
scaled cosmological constant <sup>†</sup>	$\Omega_\Lambda = \Lambda c^2/3H_0^2$	0.6 ≲ Ω <sub>Λ</sub> ≲ 0.8	[16]
scale factor for cosmological constant <sup>†</sup>	$c^2/3H_0^2$	2.853 × 10 <sup>51</sup> h <sub>0</sub> <sup>-2</sup> m <sup>2</sup>	
Ω <sub>M</sub> + Ω <sub>Λ</sub> + ... [21]	Ω <sub>tot</sub> [21]	see footnote [22]	
age of the universe <sup>†</sup>	$t_0$	12–18 Gyr	[16]
cosmic background radiation (CBR) temperature <sup>†</sup>	$T_0$	2.725 ± 0.001 K	[23, 24]
solar velocity with respect to CBR		369.3 ± 2.5 km s <sup>-1</sup>	[24, 25]
energy density of CBR	$\rho_\gamma$	4.641 7 × 10 <sup>-34</sup> (T/2.725) <sup>4</sup> g cm <sup>-3</sup> = 0.260 38 (T/2.725) <sup>4</sup> eV cm <sup>-3</sup>	[12, 24]
energy density of relativistic particles (CBR + ν)	$\rho_R$	7.804 2 × 10 <sup>-34</sup> (T/2.725) <sup>4</sup> g cm <sup>-3</sup> = 0.437 78 (T/2.725) <sup>4</sup> eV cm <sup>-3</sup>	[12, 24]
number density of CBR photons	$n_\gamma$	410.50 (T/2.725) <sup>3</sup> cm <sup>-3</sup>	[12, 24]
entropy density/Boltzmann constant	$s/k$	2 889.2 (T/2.725) <sup>3</sup> cm <sup>-3</sup>	[12]

<sup>†</sup> Subscript 0 indicates present-day values.

## References:

1. P.J. Mohr and B.N. Taylor, “CODATA Recommended Values of the Fundamental Physical Constants: 1998,” *J. Phys. Chem. Ref. Data* **28**, 1713–1852 (1999).
2. B.W. Petley, *Nature* **303**, 373 (1983).
3. The value of  $G_N$  [1] is the same as in Ref. 26, but the quoted error is 12 times larger. See *Measurement, Science, and Technology* **10**, No. 6 (June 1999), special section: “The gravitational constant: Theory and experiment 200 years after Cavendish.”  
In the context of the scale dependence of field theoretic quantities, it should be remarked that absolute lab measurements of  $G_N$  have been performed on scales of 0.01–1.0 m.
4. *The Astronomical Almanac for the year 2001*, U.S. Government Printing Office, Washington, and Her Majesty’s Stationary Office, London (1999).
5. JPL Planetary Ephemerides, E. Myles Standish, Jr., private communication (1989).
6. 1 AU divided by  $\pi/648\,000$ ; quoted error is from the JPL Planetary Ephemerides value of the AU [5].
7. Product of  $2/c^2$  and the heliocentric gravitational constant [4]. The given 9-place accuracy seems consistent with uncertainties in defining the earth’s orbital parameters.
8. Obtained from the heliocentric gravitational constant [4] and  $G_N$  [3]. The error is the 1500 ppm standard deviation of  $G_N$ .
9. 1996 mean total solar irradiance (TSI) =  $1367.5 \pm 2.7$  [27]; the solar luminosity is  $4\pi \times (1 \text{ AU})^2$  times this quantity. This value increased by 0.036% between the minima of solar cycles 21 and 22. It was modulated with an amplitude of 0.039% during solar cycle 21 [28].  
Sackmann *et al.* [29] use TSI =  $1370 \pm 2 \text{ W m}^{-2}$ , but conclude that the solar luminosity ( $L_\odot = 3.853 \times 10^{26} \text{ J s}^{-1}$ ) has an uncertainty of 1.5%. Their value comes from three 1977–83 papers, and they comment that the error is based on scatter among the reported values, which is substantially in excess of that expected from the individual quoted errors.  
The conclusion of the 1971 review by Thekaekara and Drummond [30] ( $1353 \pm 1\% \text{ W m}^{-2}$ ) is often quoted [31]. The conversion to luminosity is not given in the Thekaekara and Drummond paper, and we cannot exactly reproduce the solar luminosity given in Ref. 31.  
Finally, a value based on the 1954 spectral curve due to Johnson [32] ( $1395 \pm 1\% \text{ W m}^{-2}$ , or  $L_\odot = 3.92 \times 10^{26} \text{ J s}^{-1}$ ) has been used widely, and may be the basis for the higher value of the solar luminosity and the corresponding lower value of the solar absolute bolometric magnitude (4.72) still common in the literature [12].
10. Product of  $2/c^2$ , the heliocentric gravitational constant from Ref. 4, and the earth/sun mass ratio, also from Ref. 4. The given 9-place accuracy appears to be consistent with uncertainties in actually defining the earth’s orbital parameters.
11. Obtained from the geocentric gravitational constant [4] and  $G_N$  [3]. The error is the 1500 ppm standard deviation of  $G_N$ .
12. E.W. Kolb and M.S. Turner, *The Early Universe*, Addison-Wesley (1990).
13. F.J. Kerr and D. Lynden-Bell, *Mon. Not. R. Astr. Soc.* **221**, 1023–1038 (1985). “On the basis of this review these [ $R_0 = 8.5 \pm 1.1 \text{ kpc}$  and  $\Theta_0 = 220 \pm 20 \text{ km s}^{-1}$ ] were adopted by resolution of IAU Commission 33 on 1985 November 21 at Delhi”.
14. M.J. Reid, *Annu. Rev. Astron. Astrophys.* **31**, 345–372 (1993). Note that  $\Theta_0$  from the 1985 IAU Commission 33 recommendations is adopted in this review, although the new value for  $R_0$  is smaller.
15. Conversion using length of tropical year.
16. M. Fukugita & C.J. Hogan, “Global Cosmological Parameters:  $H_0$ ,  $\Omega_M$ , and  $\Lambda$ ,” Sec. 17 of this *Review*.
17. The final uncertainty arises from dichotomous estimates of the distance to the Large Magellanic Cloud.
18. G. Gilmore, R.F.G. Wyse, and K. Kuijken, *Annu. Rev. Astron. Astrophys.* **27**, 555 (1989).
19. E.I. Gates, G. Gyuk, and M.S. Turner (*Astrophys. J.* **449**, L133 (1995)) find the local halo density to be  $9.2^{+3.8}_{-3.1} \times 10^{-25} \text{ g cm}^{-3}$ , but also comment that previously published estimates are in the range  $1-10 \times 10^{-25} \text{ g cm}^{-3}$ .  
The value  $0.3 \text{ GeV}/c^2$  has been taken as “standard” in several papers setting limits on WIMP mass limits, *e.g.* in M. Mori *et al.*, *Phys. Lett.* **B289**, 463 (1992).
20. Fukugita & Hogan find a more restrictive limit,  $0.2 \lesssim \Omega_M \lesssim 0.4$ , if the Universe is flat.
21. In addition to the pressureless mass density  $\Omega_M$  and the scaled cosmological constant  $\Omega_\Lambda$ ,  $\Omega_{\text{tot}}$  contains very small contributions from the cosmic background radiation, the primordial neutrino energy density, and perhaps other sources.  $1 - \Omega_{\text{tot}}$  is the three-dimensional scalar curvature scaled by the squared inverse Hubble length, variously written as  $kc^2/(H_0 R(t_0))^2$  [12],  $Kc^2/H_0^2$  [36], and  $\Omega_k$ [37]. Thus  $\Omega_{\text{tot}} = 1$  indicates a flat universe.
22. First results from both BOOMERANG [33] and MAXIMA-1 [34] indicate  $\Omega_M + \Omega_\Lambda \approx 1$  with  $\approx 10\%$  uncertainties, providing the strongest evidence to date for a flat universe. See discussions elsewhere in this *Review* concerning the remarkable consistency of  $\Omega_M$  and  $\Omega_\Lambda$  measurements by different methods [16,24,35].
23. J. Mather *et al.*, *Astrophys. J.* **512**, 511 (1999). We quote a one standard deviation uncertainty.
24. G.F. Smoot & D. Scott, “Cosmic Background Radiation,” Sec. 19 of this *Review*.
25. C.H. Lineweaver *et al.*, *Astrophys. J.* **470**, 28 (1996). Dipole velocity is in the direction  $(\ell, b) = (264^\circ.31 \pm 0^\circ.04 \pm 0^\circ.16, +48^\circ.05 \pm 0^\circ.02 \pm 0^\circ.09)$ , or  $(\alpha, \delta) = (11^{\text{h}}11^{\text{m}}57^{\text{s}} \pm -7^\circ.22 \pm 0^\circ.08)$  (JD2000).
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33. P. de Bernardis *et al.*, *Nature* **404**, 955 (2000).
34. A. Balbi *et al.*, *astro-ph/0005124*, submitted to *Astrophys. J. Lett.*
35. E.W. Kolb and M.S. Turner, “Pocket Cosmology,” Sec. 15 of this *Review*.
36. S. Weinberg, *Gravitation and Cosmology*, John Wiley & Sons (1972).
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